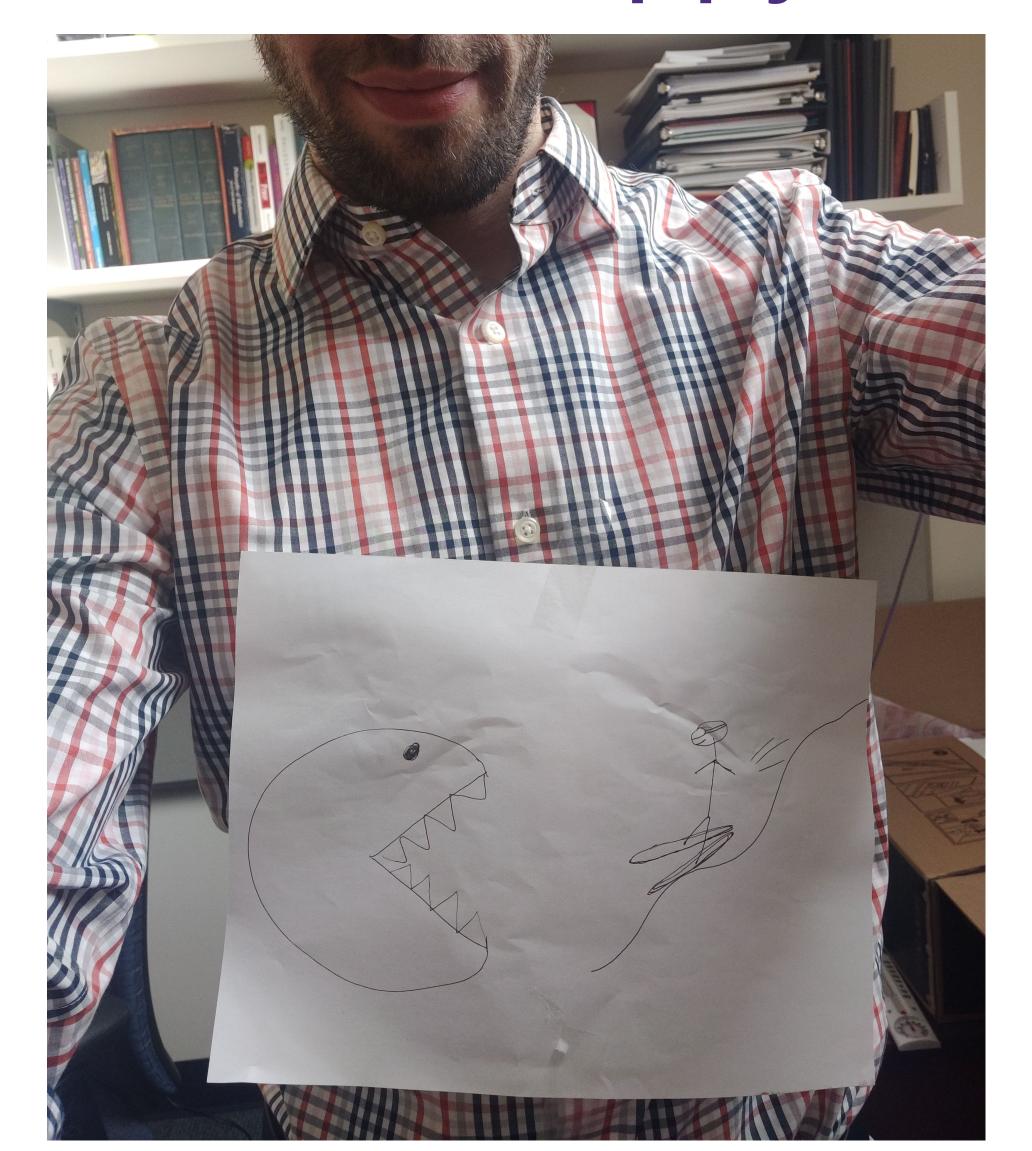
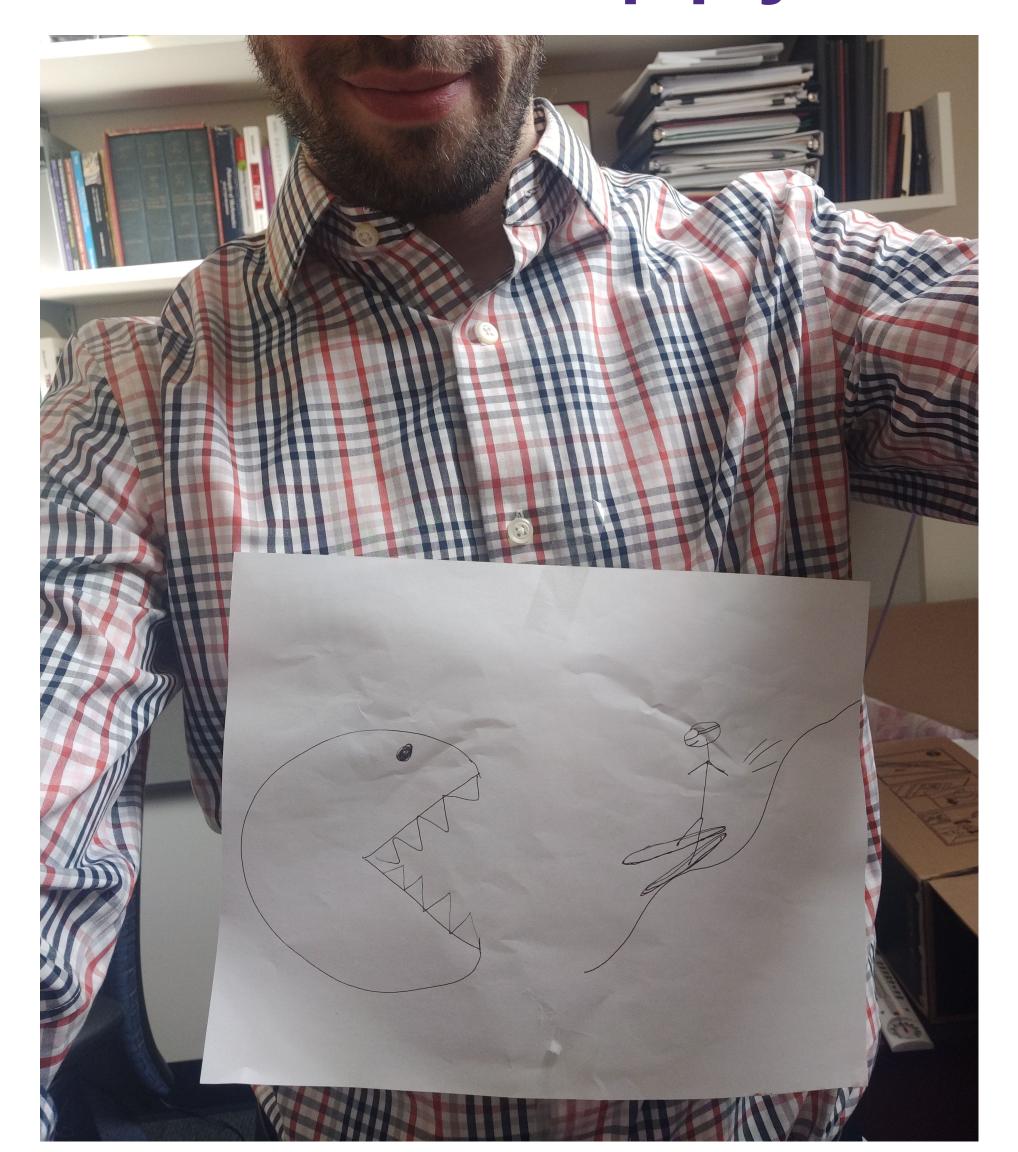
Computational Semantics

LING 571 — Deep Processing for NLP October 31, 2022

Announcements

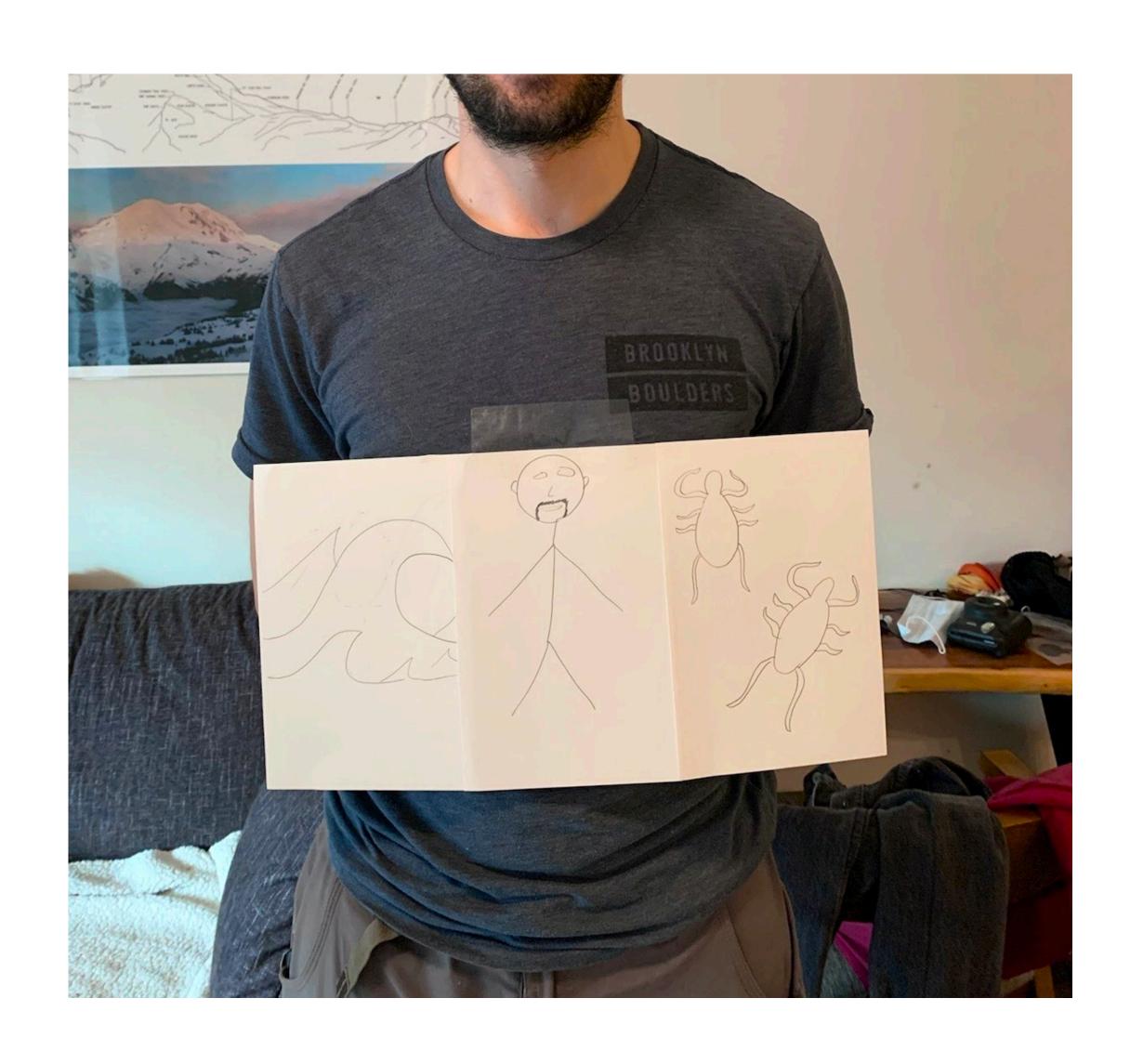
- No class on December 5
- Happy Halloween!!



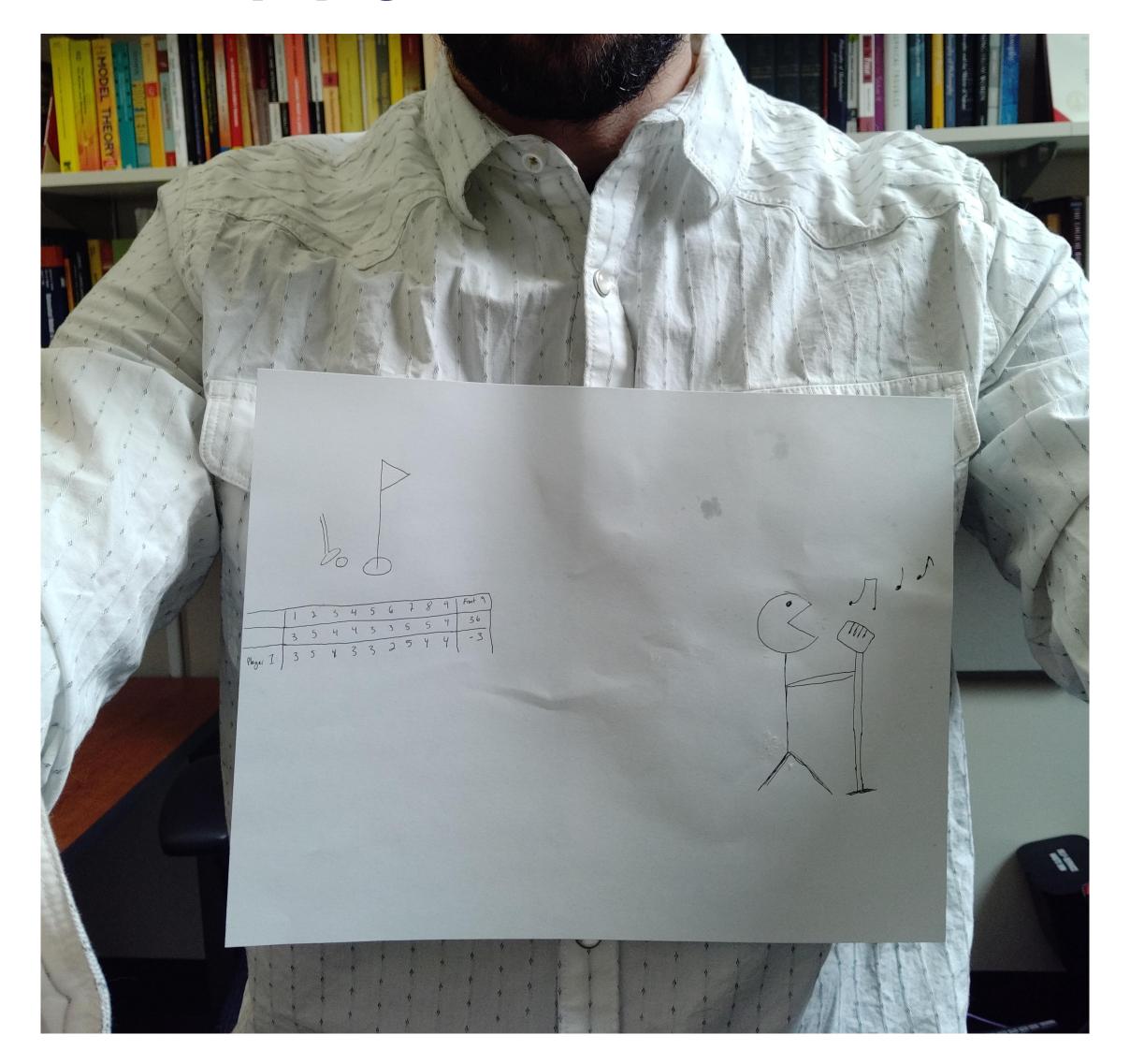


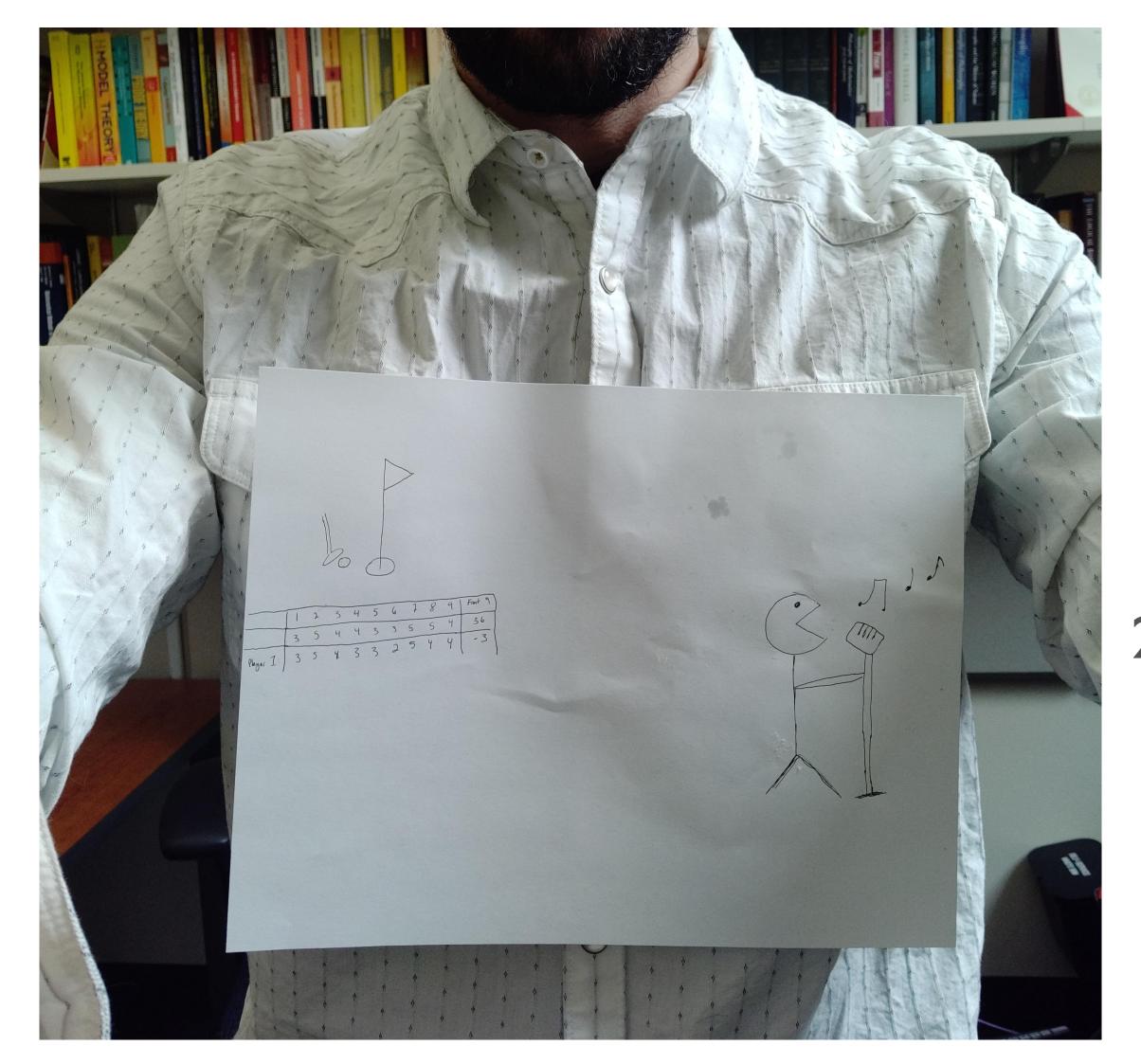
2019: Chomp + Ski = Chomsky





2020: Sea + Man + Ticks = Semantics





2021: par + sing = parsing



2022: ????

W What am I for Halloween? (one word, dad joke)

Total Results: 0



Varieties of Entailment in the News

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 - "We are talking on Zoom right now."
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 - The former, but not the latter, entails that we are talking right now.

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- Contrast:
 - "We are talking on Zoom right now."
 - "We are NOT talking on Zoom right now."
 - The former, but not the latter, entails that we are talking right now.
- Presuppositions (that there is a king) "project out" from negation (and other operators, like questions, conditionals, etc). Standard logical entailments do not.
 - Presuppositions must be true in order for a sentence to be true or false at all.

- "Some conferences were cancelled this year."
 - Seems to entail: "Not all conferences were cancelled this year."
 - But: can follow with "In fact, all of them were!" (In jargon: the implicature can be cancelled.)

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 - Common examples of scales: {some, all}, {or, and}, {may, must}, ...
- Trump's doctor when he was at the hospital with COVID-19:
 - Press: "Has he ever been on supplemental oxygen?"
 - Doc: "He hasn't had supplemental oxygen today or yesterday."

"Several students were told that the exam will be postponed."

- "Several students were told that the exam will be postponed."
 - There is an exam.

- "Several students were told that the exam will be postponed."
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 - A student was told that the exam will be postponed.

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 - The exam will be postponed.

- "Several students were told that the exam will be postponed."
 - There is an exam.
 - A student was told that the exam will be postponed.
 - The exam will be postponed.
 - Not every student was told that the exam will be postponed.

An Interesting Example

A top baseball prospect's Southern California scholarship was lost to the pandemic

https://www.washingtonpost.com/road-to-recovery/2020/11/02/tank-espalin-usc-indiana-baseball/

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"A prospect's scholarship": presupposes there is a scholarship Rest of headline: there is no more scholarship Complex compositional interaction between tense and presupposition

Roadmap

- First-order Logic: Syntax and Semantics
- Inference + Events
- Rule-to-rule Model
 - More lambda calculus

FOL Syntax + Semantics

Example Meaning Representation

A non-stop flight that serves Pittsburgh:

 $\exists x \; Flight(x) \land Serves(x, Pittsburgh) \land Non-stop(x)$

FOL Syntax Summary

```
Formula 

                                                                 Connective \rightarrow
                                   Atomic Formula
                                                                                                    \wedge | \vee | \Rightarrow
                           Formula Connective Formula
                                                                 Quantifier \rightarrow
                                                                                                      AI∃
                         Quantifier Variable, ... Formula
                                                                  Constant
                                                                                      Vegetarian Food \mid Maharani \mid \dots
                                      \neg Formula
                                                                   Variable \rightarrow
                                                                                                   x \mid y \mid \dots
                                                                  Predicate \rightarrow
                                      (Formula)
                                                                                              Serves \mid Near \mid ...
AtomicFormula \rightarrow
                                Predicate(Term,...)
                                                                  Function
                                                                                        LocationOf \mid CuisineOf \mid ...
                                Function(Term,...)
      Term
                                      Constant
                                       Variable
```

J&M p. 556 (3rd ed. 16.3)

Model-Theoretic Semantics

- A "model" represents a particular state of the world
- Our language has logical and non-logical elements.
 - Logical: Symbols, operators, quantifiers, etc
 - Non-Logical: Names, properties, relations, etc

Denotation

• Every non-logical element points to a fixed part of the model

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- Objects elements in the domain, denoted by terms
 - John, Farah, fire engine, dog, stop sign
- Properties sets of elements
 - red: {fire hydrant, apple,...}
- Relations sets of tuples of elements
 - CapitalCity: {(Washington, Olympia), (Yamoussokro, Cote d'Ivoire), (Ulaanbaatar, Mongolia),...}

via J&M, p. 554

Sample Domain 29

Objects

Matthew, Franco, Katie, Caroline Frasca, Med, Rio Italian, Mexican, Eclectic

a,b,c,d e,f,g h,i,j

via J&M, p. 554

Sample Domain 20

Objects

Matthew, Franco, Katie, Caroline

Frasca, Med, Rio

Italian, Mexican, Eclectic

a,b,c,d

e,f,g

h,i,j

Properties

Noisy Frasca, Med, and Rio are noisy

Noisy={*e,f,g*}

via J&M, p. 554

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Likes Matthew likes the Med

Katie likes the Med and Rio

Franco likes Frasca

Caroline likes the Med and Rio

Likes=
$$\{ \langle a, f \rangle, \langle c, f \rangle, \langle c, g \rangle, \langle b, e \rangle, \langle d, f \rangle, \langle d, g \rangle \}$$

Sample Domain 20

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Matthew, Franco, Katie, Caroline

Frasca, Med, Rio

Italian, Mexican, Eclectic

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Noisy={*e,f,g*}

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Likes Matthew likes the Med

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Franco likes Frasca

Caroline likes the Med and Rio

Serves Med serves eclectic

Rio serves Mexican Frasca serves Italian

Likes=
$$\{ \langle a, f \rangle, \langle c, f \rangle, \langle c, g \rangle, \langle b, e \rangle, \langle d, f \rangle, \langle d, g \rangle \}$$

Serves={
$$\langle c, f \rangle$$
, $\langle f, i \rangle$, $\langle e, h \rangle$ }

Events

- Initially, single predicate with some arguments
 - Serves(United, Houston)
 - Assume # of args = # of elements in subcategorization frame

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 - The flight arrived in Seattle
 - The flight arrived in Seattle on Saturday.
 - The flight arrived on Saturday.
 - The flight arrived in Seattle from SFO.
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- Variable number of arguments; many entailment relations here.

- Arity:
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 - $\exists e \ Arrival(e, Flight, Seattle, SFO) \land Time(e, Saturday)$

- Arity:
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- The flight arrived in Seattle from SFO on Saturday.
 - Davidsonian (Davidson 1967):
 - $\exists e \ Arrival(e, Flight, Seattle, SFO) \land Time(e, Saturday)$
 - Neo-Davidsonian (Parsons 1990):
 - $\exists e \ Arrival(e) \land Arrived(e, \ Flight) \land Destination(e, \ Seattle) \land Origin(e, \ SFO)$ $\land \ Time(e, \ Saturday)$

Why events?

 "Adverbial modification is thus seen to be logically on a par with adjectival modification: what adverbial clauses modify is not verbs but the events that certain verbs introduce." — Davidson

Neo-Davidsonian Events

- Neo-Davidsonian representation:
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Neo-Davidsonian Events

- Neo-Davidsonian representation:
 - Distill event to single argument for main predicate
 - Everything else is additional predication
- Pros
 - No fixed argument structure
 - Dynamically add predicates as necessary
 - No unused roles
 - Logical connections can be derived

Meaning Representation for Computational Semantics

- Requirements
 - Verifiability
 - Unambiguous representation
 - Canonical Form
 - Inference
 - Variables
 - Expressiveness
- Solution:
 - First-Order Logic
 - Structure
 - Semantics
 - Event Representation

Rule-to-Rule Model

Recap

- Meaning Representation
 - Can represent meaning in natural language in many ways
 - We are focusing on First-Order Logic (FOL)

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- Meaning Representation
 - Can represent meaning in natural language in many ways
 - We are focusing on First-Order Logic (FOL)
- Principle of compositionality
 - The meaning of a complex expression is a function of the meaning of its parts
- Lambda Calculus
 - λ-expressions denote functions
 - Can be nested
 - Reduction = function application

Semantics Reflects Syntax

Chiasmus:

Syntax affects Semantics!





Bowie playing Tesla

The Prestige (2006)

Tesla playing Bowie

SpaceX Falcon Heavy Test Launch (2/6/2018)

Chiasmus: Syntax affects Semantics!

• "Never let a fool kiss you or a kiss fool you" (Grothe, 2002)

• "Then you should say what you mean," the March Hare went on.

"I do," Alice hastily replied; "at least—at least I mean what I say—that's the same thing, you know."

"Not the same thing a bit!" said the Hatter. "Why, you might just as well say that 'I see what I eat' is the same thing as 'I eat what I see'!"

"You might just as well say," added the March Hare, "that 'I like what I get' is the same thing as 'I get what I like'!"

"You might just as well say," added the Dormouse, which seemed to be talking in his sleep, "that 'I breathe when I sleep' is the same thing as 'I sleep when I breathe'!"

-Alice in Wonderland, Lewis Carrol

• "Every Tesla is powered by a battery." — Ambiguous!

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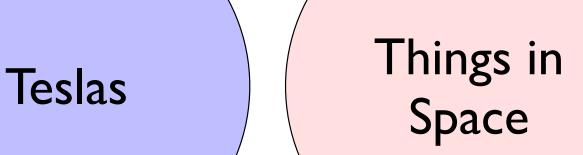
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State of known Universe: 02/05/2018

Ambiguity & Model

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Things in Space



 $\exists (\boldsymbol{x}).(Tesla(\boldsymbol{x}) \land HurtlingTowardsMars(\boldsymbol{x}))$

State of known Universe: 02/06/2018

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Things in Space



 $\exists (\boldsymbol{x}).(Tesla(\boldsymbol{x}) \land HurtlingTowardsMars(\boldsymbol{x}))$

Scope Ambiguity

- Potentially O(n!) scope interpretations ("scopings")
 - Where *n*=number of scope-taking operators.
 - (every, a, all, no, modals, negations, conditionals, ...)
- Different interpretations correspond to different syntactic parses!

Derivative of an alleged Groucho Marx-ism:

- Derivative of an alleged Groucho Marx-ism:
- In the US, a woman gives birth every fifteen minutes.

- Derivative of an alleged Groucho Marx-ism:
- In the US, a woman gives birth every fifteen minutes.
 - We must find her and put a stop to it.

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• Thank you scope ambiguity! (Not the same as attachment ambiguity.)

- "Boston voters have elected City Councilor Michelle Wu as mayor, the city's first woman and person of color elected to the post."
 - Source: https://www.npr.org/2021/11/02/1051720391/boston-mayor-michelle-wu-elected

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Integrating Semantics into Syntax

1. Pipeline System

- Feed parse tree and sentence to semantic analyzer
- How do we know which pieces of the semantics link to which part of the analysis?
- Need detailed information about sentence, parse tree
- Infinitely many sentences & parse trees
- Semantic mapping function per parse tree → intractable

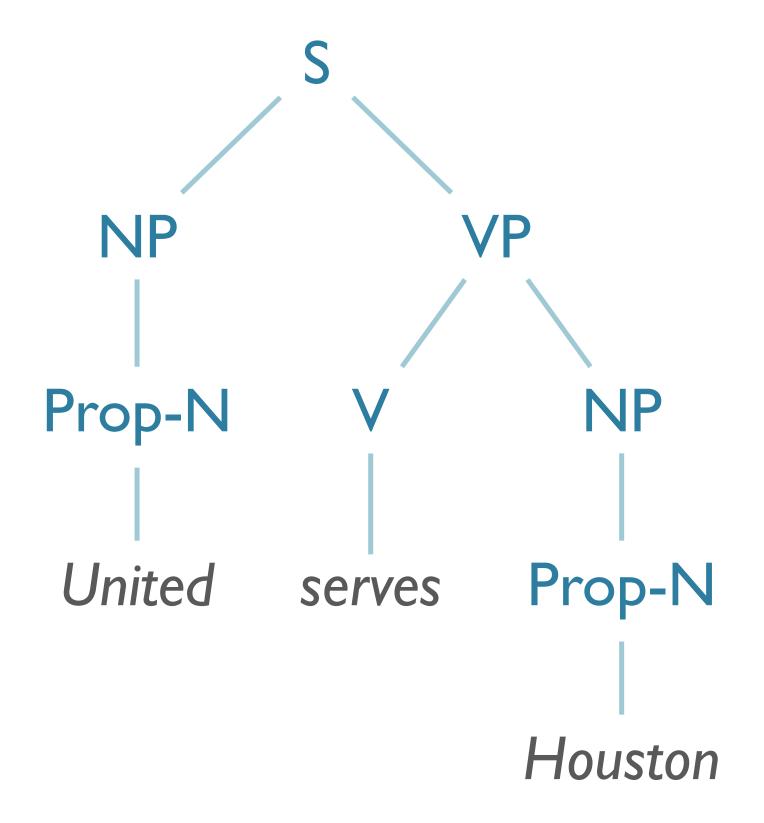
Integrating Semantics into Syntax

Integrating Semantics into Syntax

2. Integrate Directly into Grammar

- This is the "rule-to-rule" approach we've been implicitly examining and will now make more explicit
- Tie semantics to finite components of grammar (rules & lexicon)
- Augment grammar rules with semantic info
 - a.k.a. "attachments" specify how RHS elements compose to LHS

United serves Houston

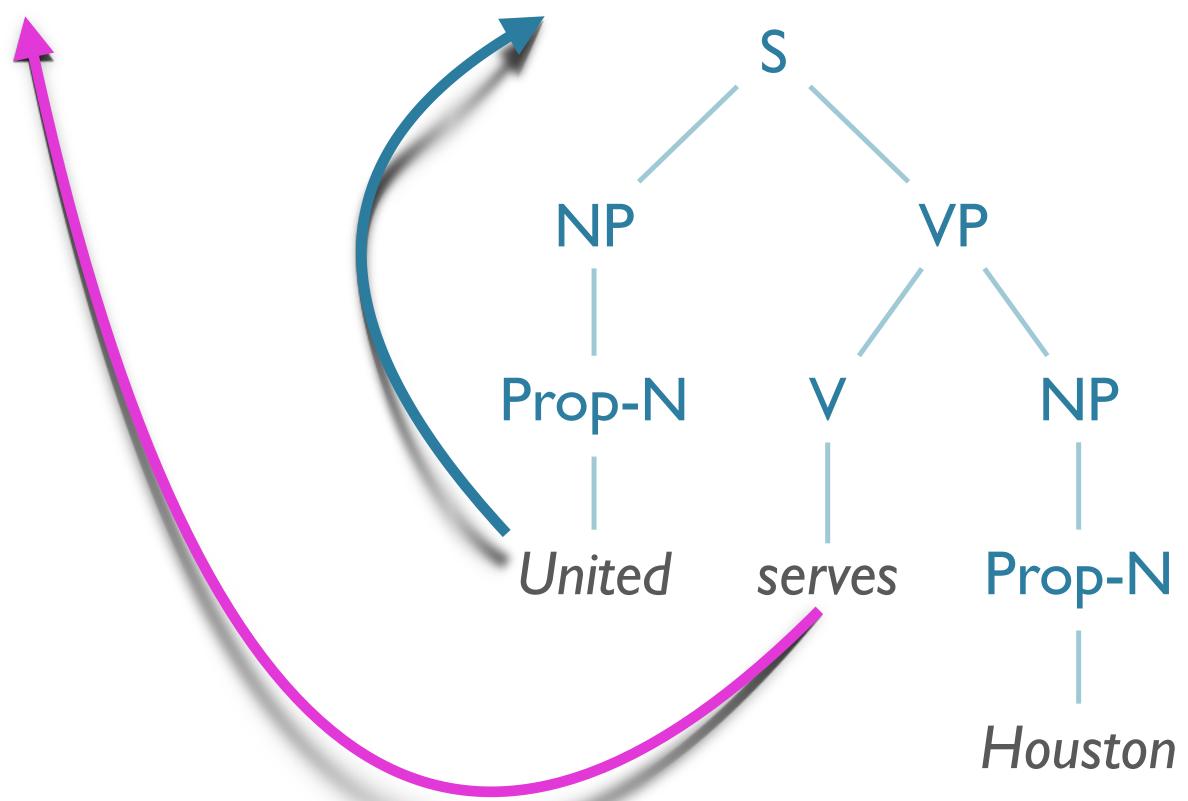


United serves Houston

 $\exists e(Serving(e) \land$ NP Prop-N NP United Prop-N serves Houston

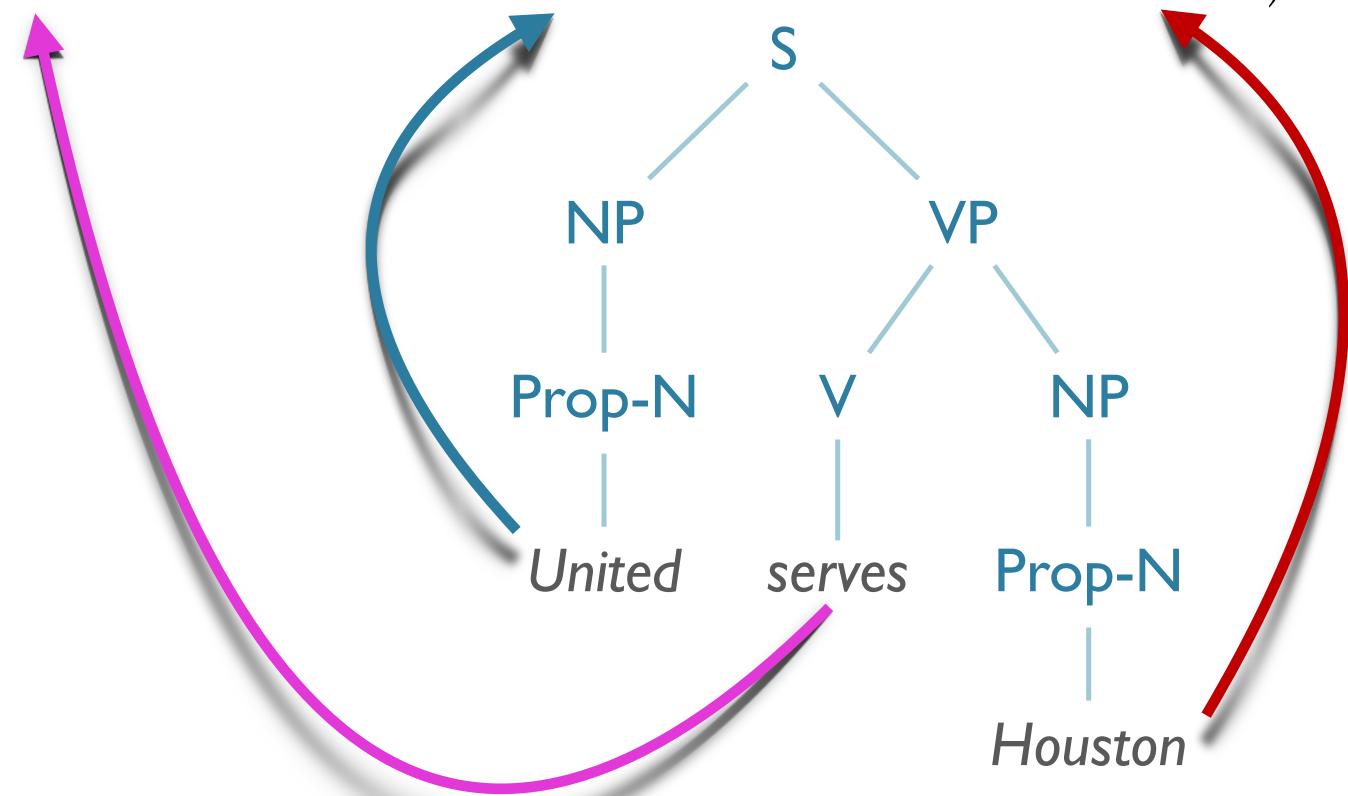
United serves Houston

 $\exists e(Serving(e) \land Server(e, United) \land$



United serves Houston

 $\exists e(Serving(e) \land Server(e, United) \land Served(e, Houston))$



Rule-to-rule Model

- Lambda Calculus and the Rule-to-Rule Hypothesis
 - λ-expressions can be attached to grammar rules
 - used to compute meaning representations from syntactic trees based on the principle of compositionality
 - Go up the tree, using reduction (function application) to compute meanings at non-terminal nodes

Semantic Attachments

Basic Structure:

$$A \rightarrow a_1, ..., a_n \{f(a_j.sem, ... a_k.sem)\}$$

Semantic Function

• In NLTK syntax (more later):

$$A \rightarrow a_1 \dots a_n[SEM=]$$

Attachments as SQL!

NLTK book, ch. 10

```
>>> nltk.data.show_cfg('grammars/book_grammars/sq10.fcfg')
% start S
S[SEM=(?np + WHERE + ?vp)] -> NP[SEM=?np] VP[SEM=?vp]
VP[SEM=(?v + ?pp)] -> IV[SEM=?v] PP[SEM=?pp]
VP[SEM=(?v + ?ap)] -> IV[SEM=?v] AP[SEM=?ap]
NP[SEM=(?det + ?n)] -> Det[SEM=?det] N[SEM=?n]
PP[SEM=(?p + ?np)] -> P[SEM=?p] NP[SEM=?np]
AP[SEM=?pp] -> A[SEM=?a] PP[SEM=?pp]
NP[SEM='Country="greece"'] -> 'Greece'
NP[SEM='Country="china"'] -> 'China'
Det[SEM='SELECT'] -> 'Which' | 'What'
N[SEM='City FROM city_table'] -> 'cities'
IV[SEM=''] -> 'are'
A[SEM=''] -> 'located'
P[SEM=''] -> 'in'
```

Attachments as SQL!

NLTK book, ch. 10

```
>>> nltk.data.show_cfg('grammars/book_grammars/sql0.fcfg')
% start S
S[SEM=(?np + WHERE + ?vp)] -> NP[SEM=?np] VP[SEM=?vp]
VP[SEM=(?v + ?pp)] -> IV[SEM=?v] PP[SEM=?pp]
VP[SEM=(?v + ?ap)] -> IV[SEM=?v] AP[SEM=?ap]
NP[SEM=(?det + ?n)] -> Det[SEM=?det] N[SEM=?n]
PP[SEM=(?p + ?np)] -> P[SEM=?p] NP[SEM=?np]
AP[SEM=?pp] -> A[SEM=?a] PP[SEM=?pp]
NP[SEM='Country="greece"'] -> 'Greece'
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```

'What cities are located in China'

parses[0]: SELECT City FROM city_table WHERE Country="china"

Semantic Attachments: Options

- Why not use SQL? Python?
 - Arbitrary power but hard to map to logical form
 - No obvious relation between syntactic, semantic elements
- Why Lambda Calculus?
 - First Order Predicate Calculus (FOPC) + function application is highly expressive, integrates well with syntax
 - Can extend our existing feature-based model, using unification
 - Can 'translate' FOL to target / task / downstream language (e.g. SQL)

Semantic Analysis Approach

- Semantic attachments:
 - Each CFG production gets semantic attachment
- Semantics of a phrase is function of combining the children
 - Complex functions need to have parameters
 - $Verb \rightarrow$ 'arrived'
 - Intransitive verb, so has one argument: subject
 - ...but we don't have this available at the preterminal level of the tree!

Defining Representations

- Proper Nouns
- Intransitive Verbs
- Transitive Verbs
- Quantifiers

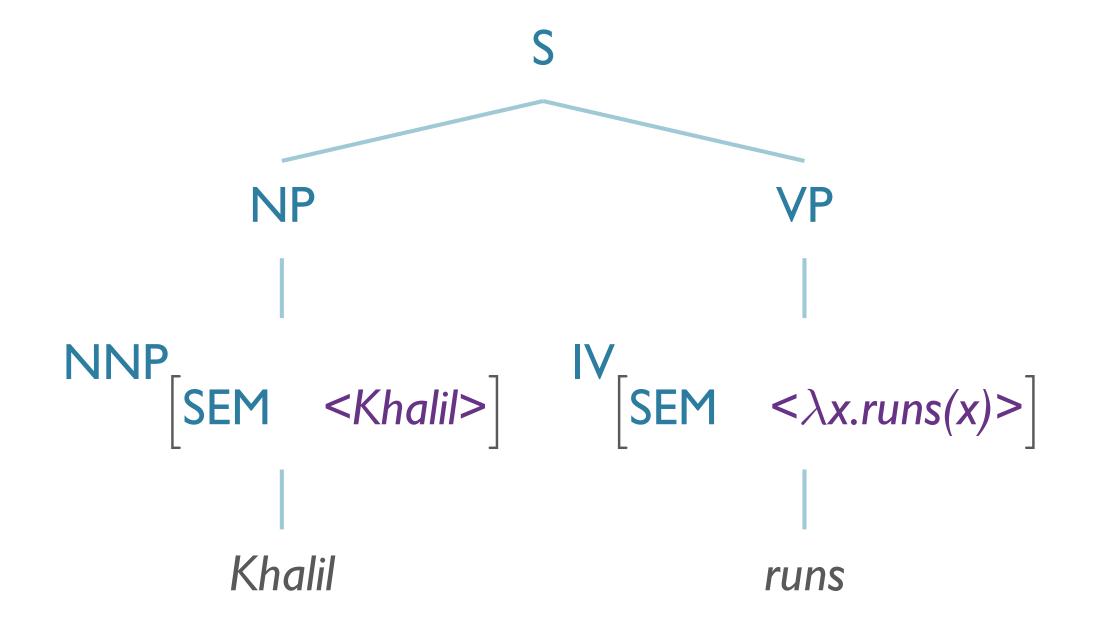
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 - NNP[SEM=<Khalil>] → 'Khalil'

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```
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```

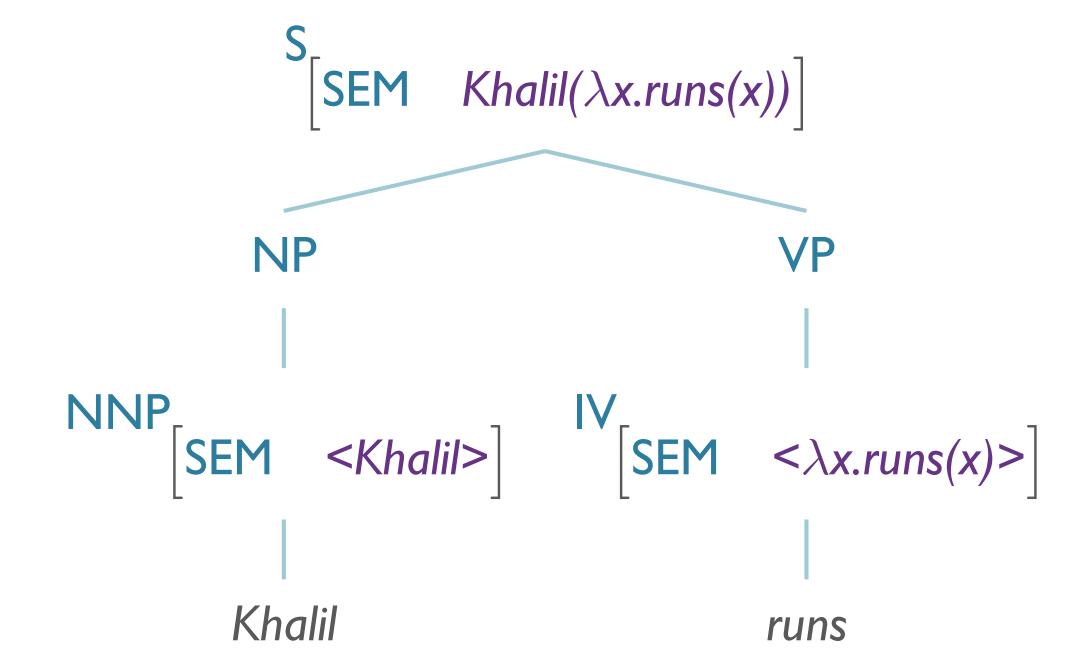
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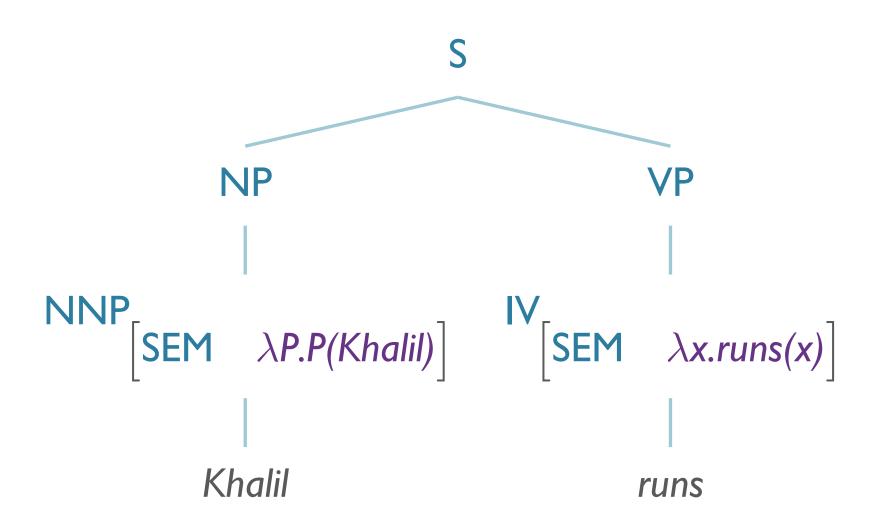
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```

```
[SEM | Khalil(\lambda x.runs(x))] \longrightarrow ERROR: Constant "Khalil" is not a function!
NP \qquad VP
| \qquad | \qquad | \qquad |
NNP[SEM | < Khalil >] \qquad [SEM | < \lambda x.runs(x) >]
| \qquad | \qquad | \qquad |
Khalil \qquad runs
```

- Instead, we use a dummy predicate:
- "Generalizing to the worst case" (cf. Montague; Partee on type-shifting)
 - I.e.: this move will also be necessary for a uniform semantic treatment of NPs, which can be individual-denoting (like names) or more complex (quantifiers)

- With the dummy predicate:
 - NNP[SEM=<\P.P(Khalil)>] → 'Khalil'

```
S[SEM=np?(vp?)] \rightarrow NP[SEM=np?] VP[SEM=vp?]
```



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```
S[SEM=np?(vp?)] → NP[SEM=np?] VP[SEM=vp?]
```

```
\begin{bmatrix} \mathsf{SEM} & \lambda P.P(Khalil)(\lambda x.runs(x)) \end{bmatrix} \\ \mathsf{NP} & \mathsf{VP} \\ | & | \\ \mathsf{NNP} \\ [\mathsf{SEM} & \lambda P.P(Khalil)] & \mathsf{IV} \\ \mathsf{SEM} & \lambda x.runs(x) \end{bmatrix} \\ | & | \\ \mathsf{Khalil} & \mathsf{runs} \end{bmatrix}
```

Proper Nouns & Intransitive Verbs

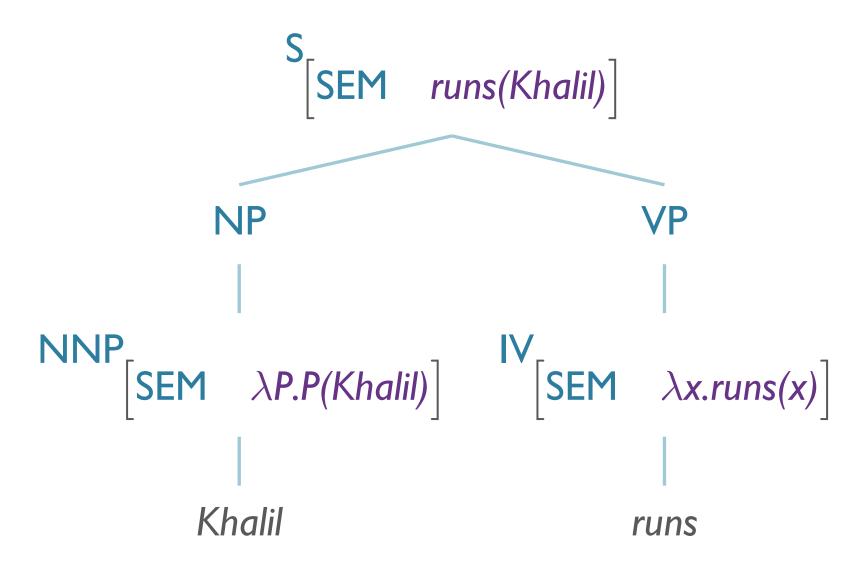
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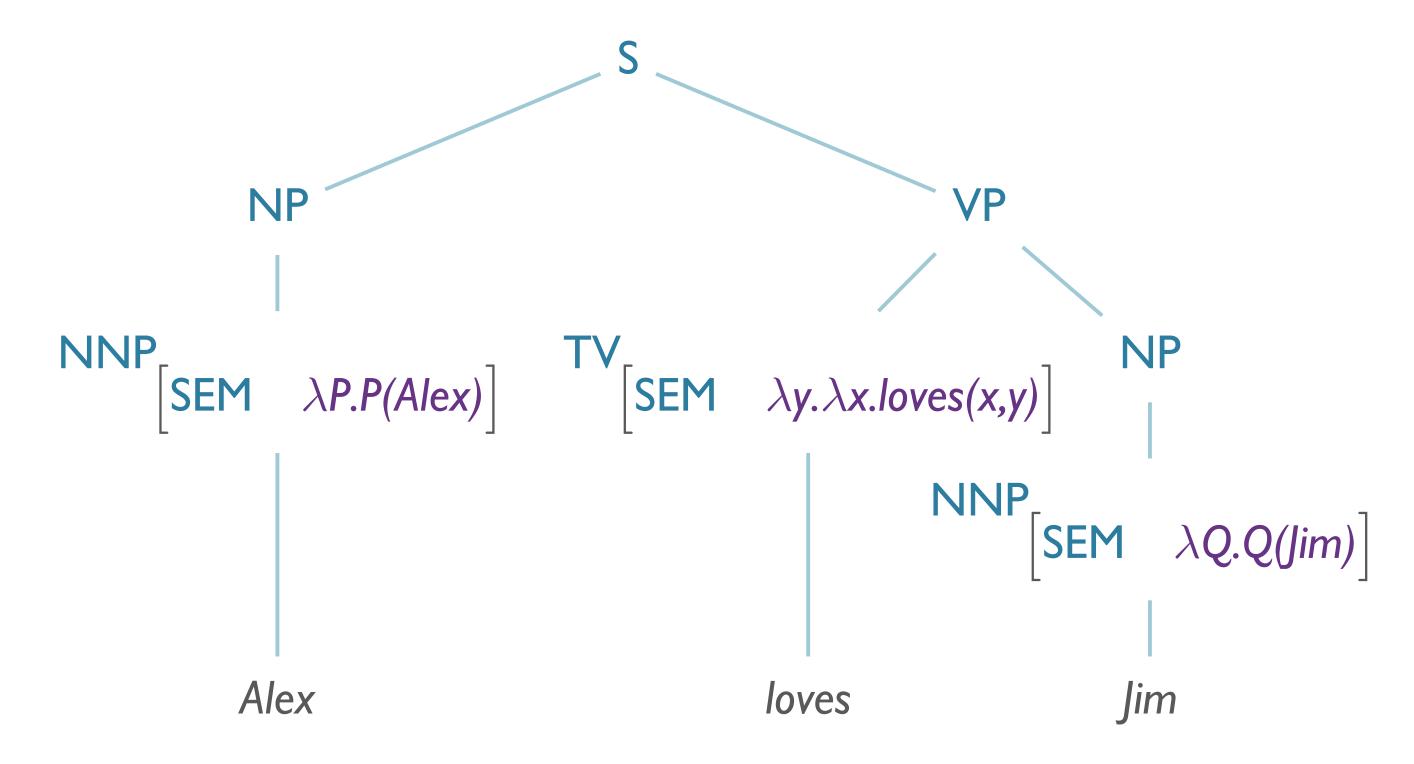
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- So, if we want to say "Alex loves Jim" we would intuitively want $\lambda y \cdot \lambda x \cdot loves(x, y)$
- ... going in linear order, we have one arg to the left and one to the right.

- So, if we want to say "Alex loves Jim" we would want $\lambda y \cdot \lambda x \cdot loves(x, y)$
- ...but going in linear order, we have one arg to the left and one to the right.



```
• TV(NP):
```

```
• \lambda y \cdot \lambda x \cdot loves(x, y) (\lambda Q \cdot Q(Jim))
```

50

```
    TV(NP):
    λy.λx.loves(x,y) (λQ.Q(Jim))
    λx.loves(x,λQ.Q(Jim))
```

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```

TV(NP):
λy.λx.loves(x,y) (λQ.Q(Jim))
λx.loves(x,λQ.Q(Jim))
→ Error! We can't reduce Jim.
Instead: λY x.Y(λy.loves(x,y))
("Continuation-passing")

```
TV(NP):
```

```
• \lambda \mathbf{Y} \times \mathbf{Y}(\lambda \mathbf{y}.loves(\mathbf{x}, \mathbf{y})) (\lambda \mathbf{Q}.\mathbf{Q}(\mathbf{Jim}))
```

```
TV(NP):
λΥ x.Υ(λγ.loves(x,γ)) (λQ.Q(Jim)) λΥ takes (λQ.Q(Jim))
λχ.(λQ.Q(Jim)(λχ.loves(x,γ))
```

• TV(NP):

```
• \lambda Y \times Y(\lambda Y \cdot \text{loves}(X,Y)) (\lambda Q \cdot Q(\text{Jim})) \lambda Y \text{ takes } (\lambda Q \cdot Q(\text{Jim}))
• \lambda X \cdot (\lambda Q \cdot Q(\text{Jim}) (\lambda X \cdot \text{loves}(X,Y)) \lambda Q \text{ takes } (\lambda Y \cdot \text{loves}(X,Y))
• \lambda X \cdot (\lambda Y \cdot \text{loves}(X,Y) (\text{Jim}))
```

• TV(NP):

```
λΥ x.Υ(λγ.loves(x,γ)) (λQ.Q(Jim))
λχ.(λQ.Q(Jim)(λχ.loves(x,γ))
λχ.(λQ.Q(Jim)(λχ.loves(x,γ))
λχ.(λγ.loves(x,γ)(Jim))
λχ.(loves(x,Jim))
```

```
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    λχ.(loves(x,Jim))
    NP(VP):
    λΡ.P(Alex)(λχ.(loves(x,Jim)))
```

```
λY takes (λQ.Q(Jim))
λQ takes (λy.loves(x,y))
λy takes (Jim)
```

TV(NP):
λΥ x.Υ(λγ.loves(x,γ)) (λQ.Q(Jim))
λχ.(λQ.Q(Jim)(λχ.loves(x,γ))
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• $\lambda x.(loves(x, Jim)(Alex))$

```
\lambda \mathbf{Y} takes (\lambda \mathbf{Q}.\mathbf{Q}(\mathbf{Jim}))
\lambda \mathbf{Q} takes (\lambda \mathbf{Y}.loves(\mathbf{X},\mathbf{Y}))
\lambda \mathbf{Y} takes (\mathbf{Jim})
```

```
\lambda_{\mathbf{P}} takes (\lambda_{\mathbf{x}}.(loves(\mathbf{x}, Jim)) \lambda_{\mathbf{x}} takes (Alex)
```

```
• TV(NP):
 • \lambda Y \times Y(\lambda y.loves(x,y)) (\lambda Q.Q(Jim))
 • \lambda x.(\lambda Q.Q(Jim)(\lambda x.loves(x,y))
 • \lambda x.(\lambda y.loves(x,y)(Jim))
 • \lambda x. (loves(x, Jim))
NP(VP):
 • \lambda P.P(Alex)(\lambda x.(loves(x,Jim)))
 • \lambda x.(loves(x, Jim)(Alex))
```

loves (Alex, Jim)

```
\lambda y takes (\lambda Q.Q(Jim))
\lambda Q takes (\lambda y.loves(x,y))
\lambda y takes (Jim)
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```
\lambda P takes (\lambda x.(loves(x, Jim)))
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Converting to an Event

- "x loves y," Originally:
 - $\lambda \mathbf{Y} \times \mathbf{Y}(\lambda \mathbf{y}.loves(\mathbf{x}, \mathbf{y}))$

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- as a Neo-Davidsonian event:
 - $\lambda \mathbf{Y} \times \mathbf{Y}(\lambda \mathbf{y}.\exists \mathbf{e} \text{ love}(\mathbf{e}) \land \text{ lover}(\mathbf{e},\mathbf{x}) \land \text{ loved}(\mathbf{e},\mathbf{y}))$

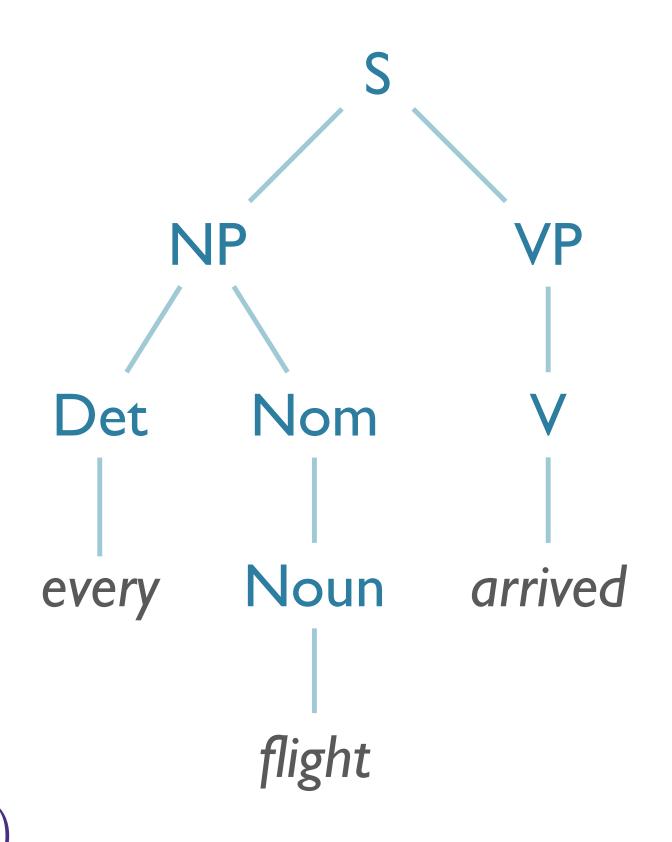
Quantifiers & Scope

Semantic Analysis Example

- Basic model
 - Neo-Davidsonian event-style model
 - Complex quantification

• Example: Every flight arrived

 $\forall \boldsymbol{x} \ Flight(\boldsymbol{x}) \Rightarrow \exists \boldsymbol{e} \ Arrived(\boldsymbol{e}) \land ArrivedThing(\boldsymbol{e}, \boldsymbol{x})$



- First intuitive approach:
 - Every flight = $\forall x \ Flight(x)$

55

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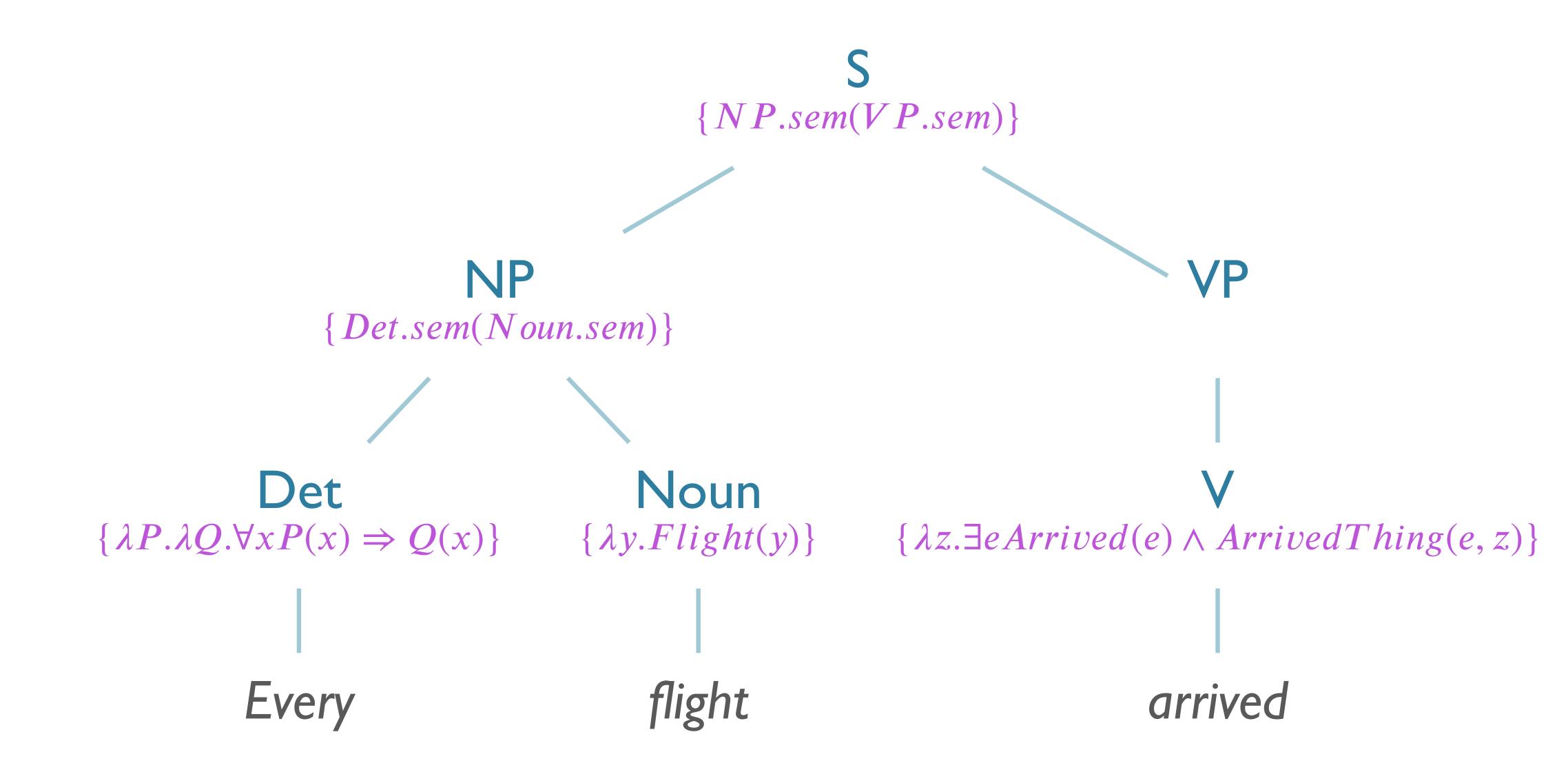
- "Every flight" is:
 - $\lambda Q. \forall x \ Flight(x) \Rightarrow Q(x)$
- ...so what is the representation for "every"?
 - $\bullet \quad \lambda \boldsymbol{P}.\lambda \boldsymbol{Q}. \forall \boldsymbol{x} \; \boldsymbol{P}(\boldsymbol{x}) \Rightarrow \boldsymbol{Q}(\boldsymbol{x})$

"A flight arrived"

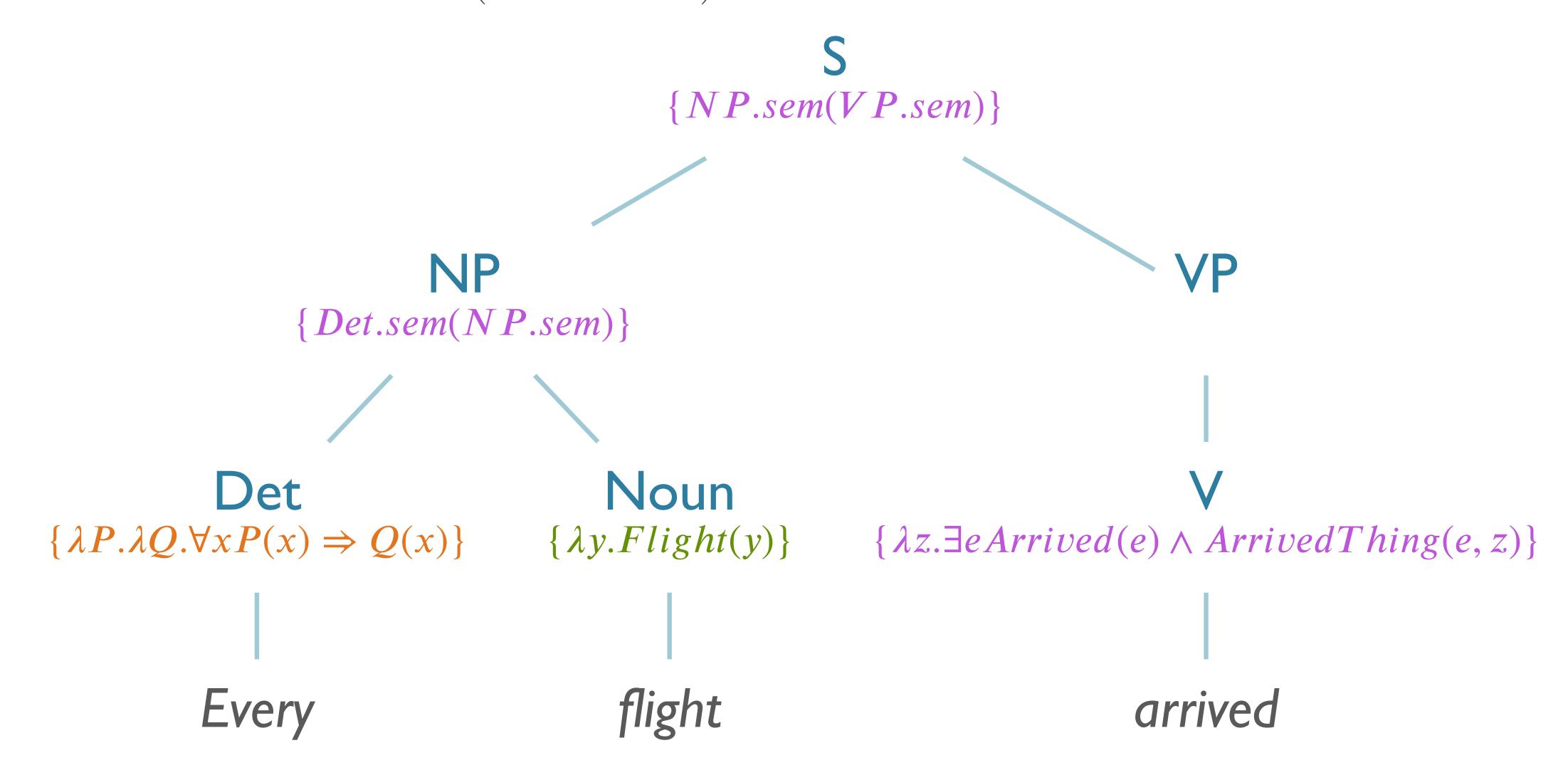
- We just need one item for truth value
 - So, start with ∃x…
 - $\lambda P.\lambda Q.\exists x P(x) \land Q(x)$

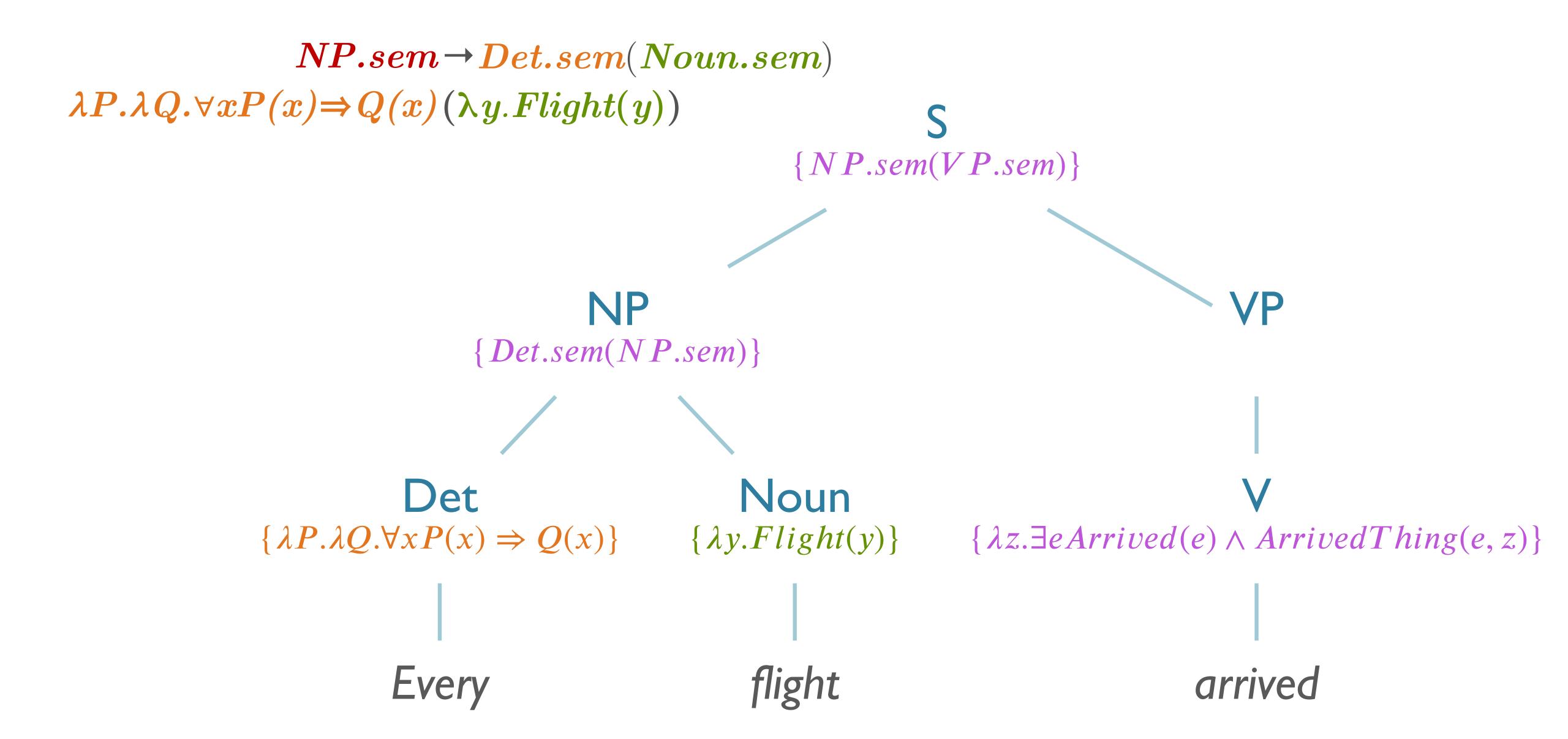
Creating Attachments

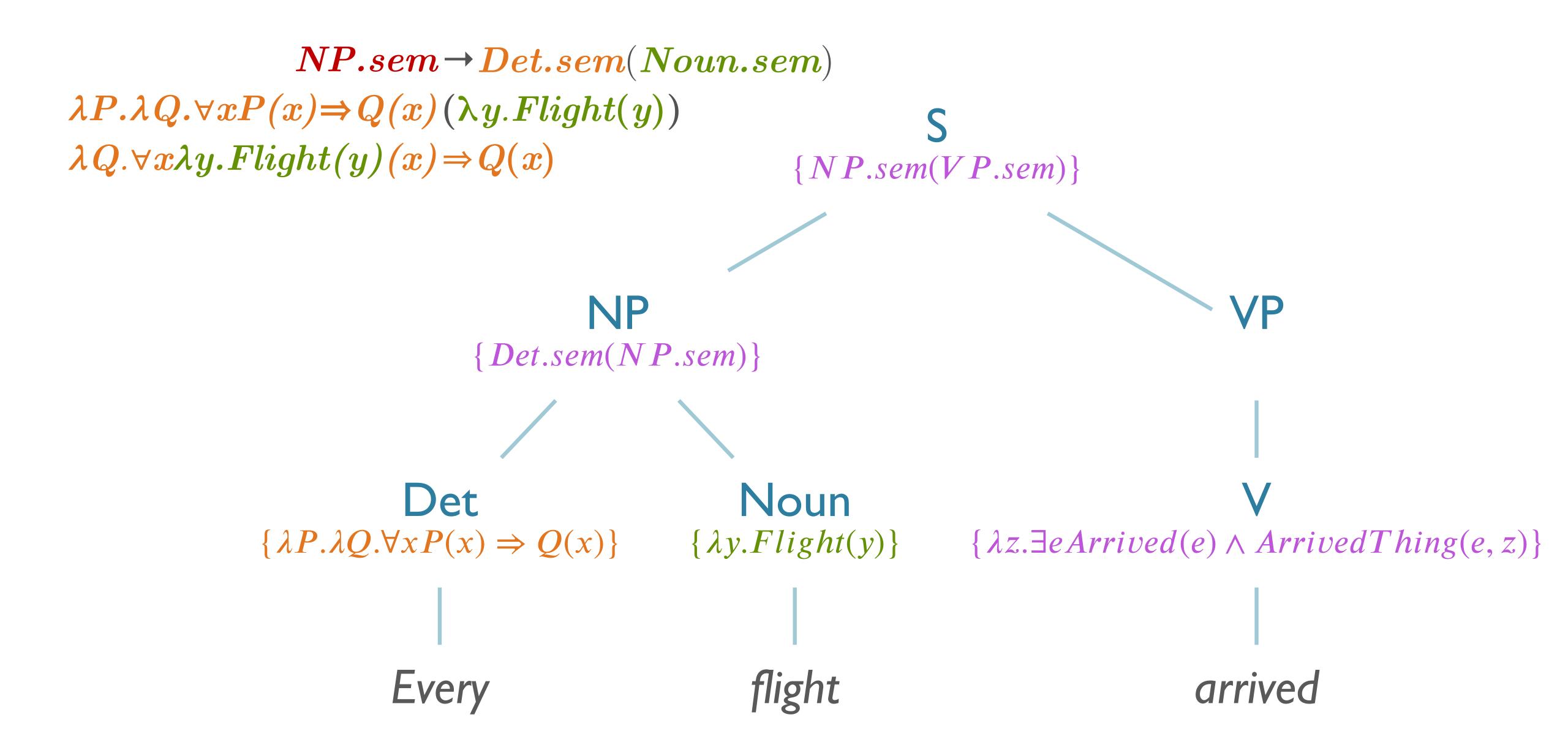
```
\{ \lambda P.\lambda Q. \forall \boldsymbol{x} P(\boldsymbol{x}) \Rightarrow Q(\boldsymbol{x}) \}
 Det
              \rightarrow 'Every'
                                                          \{ \lambda x.Flight(x) \}
Noun
              → 'flight'
                                       \{\lambda y. \exists eArrived(e) \land ArrivedThing(e, y)\}
             → 'arrived'
 Verb
  VP
                \rightarrow Verb
                                                            { Verb.sem }
                                                            { Noun.sem }
Nom
               \rightarrow Noun
                                                      \{NP.sem(VP.sem)\}
              \rightarrow NP VP
                                                     \{ Det.sem(Nom.sem) \}
             \rightarrow Det Nom
```

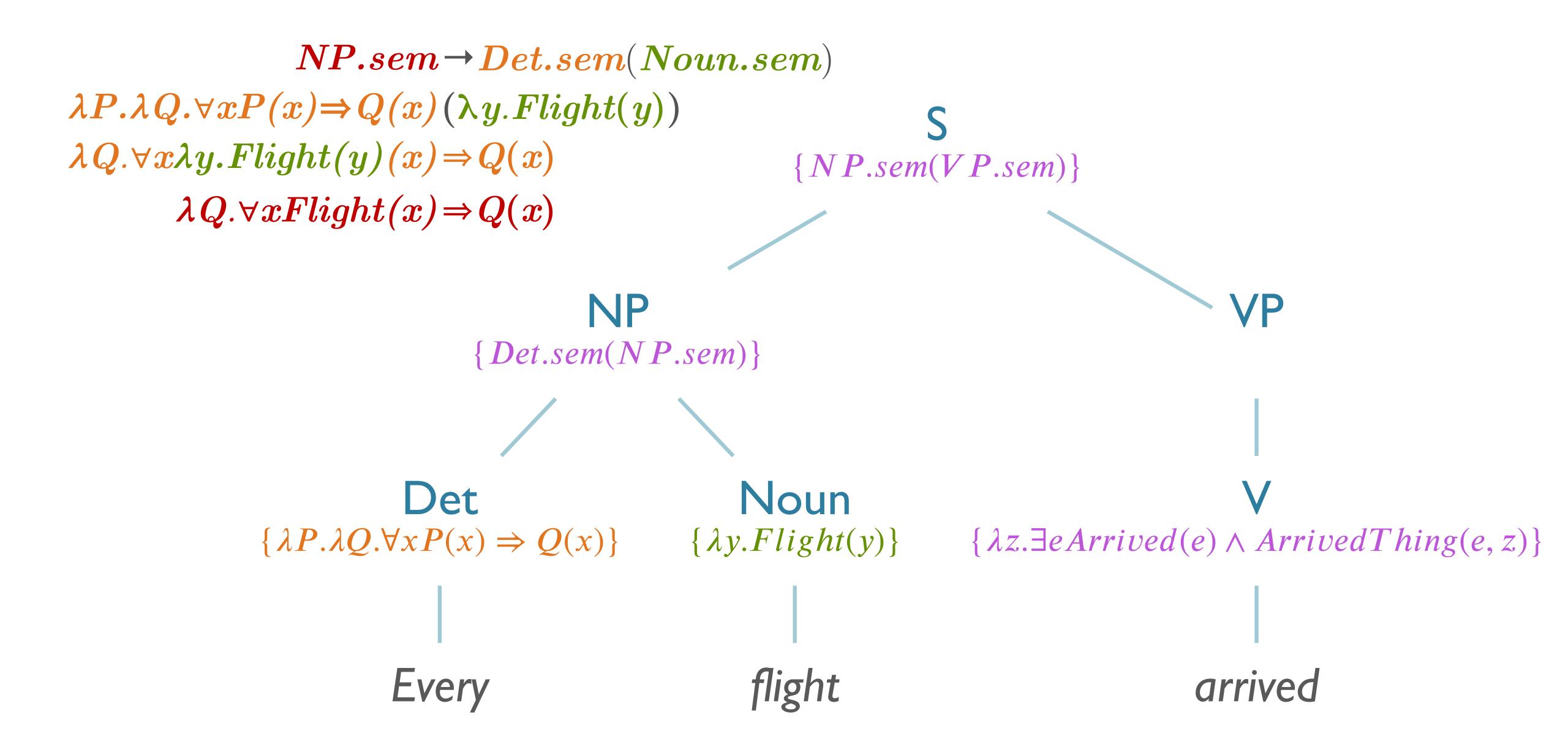


$NP.sem \rightarrow Det.sem(Noun.sem)$

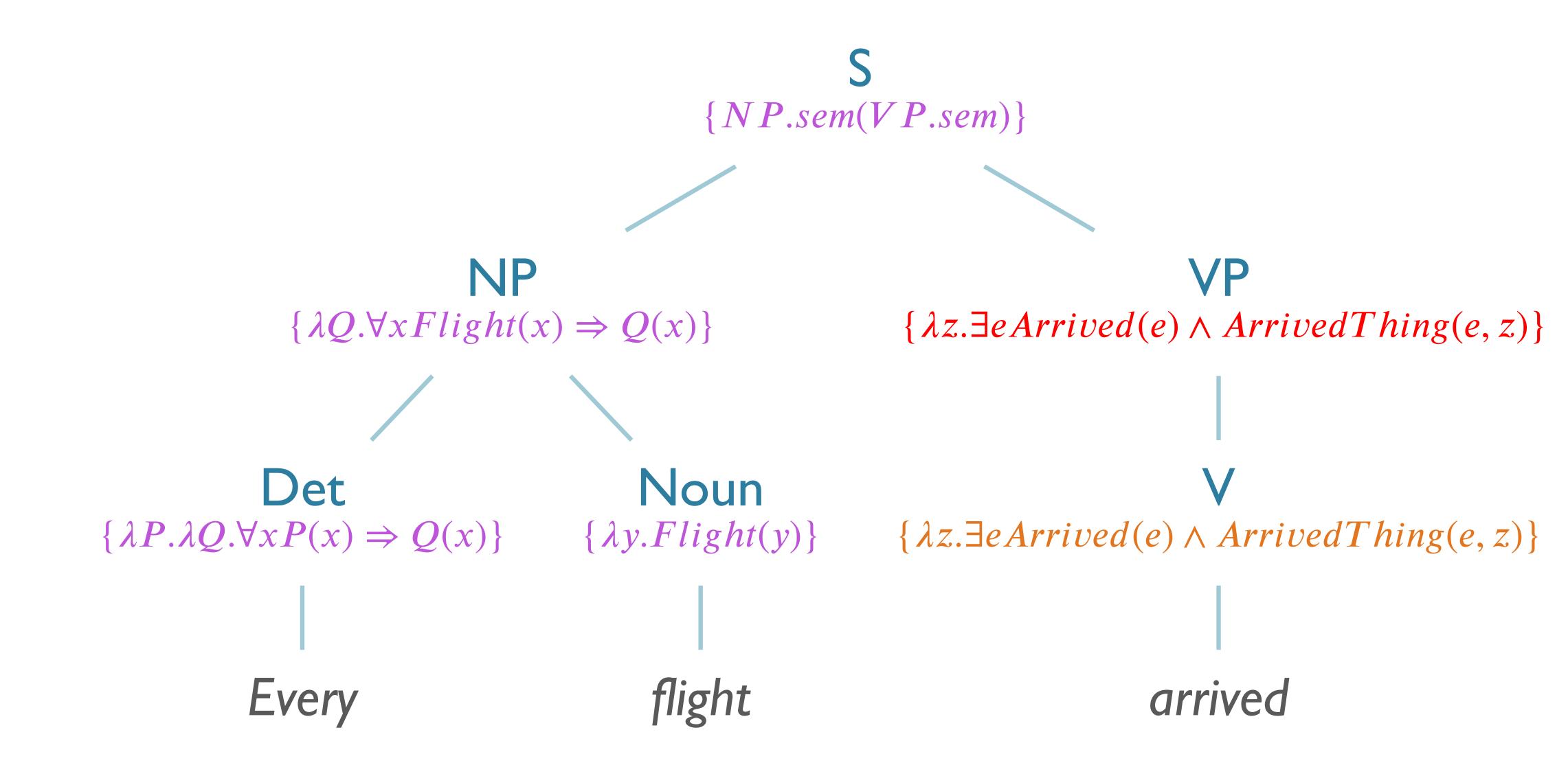


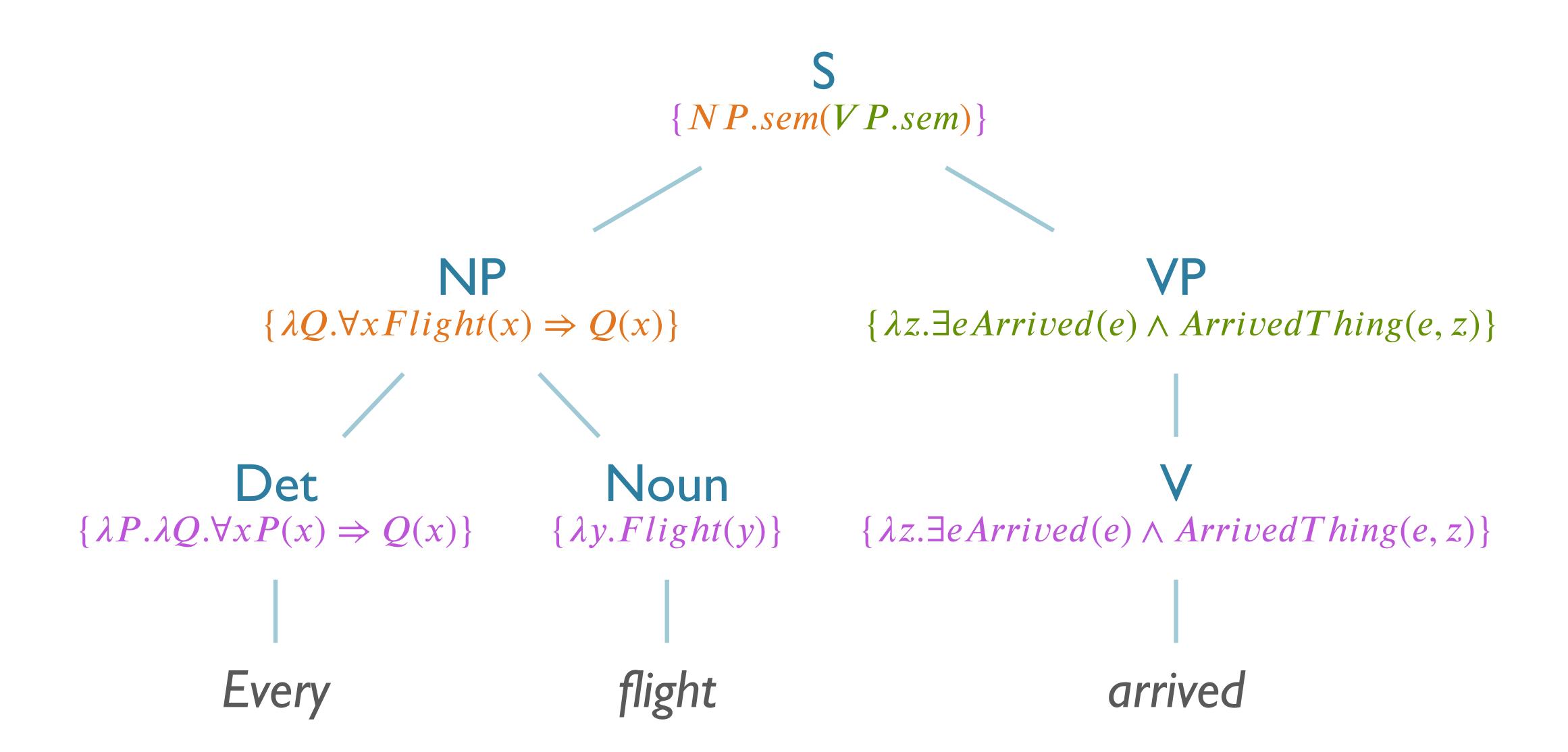






```
NP.sem \rightarrow Det.sem(Noun.sem)
\lambda P.\lambda Q. \forall x P(x) \Rightarrow Q(x) (\lambda y. Flight(y))
\lambda Q. \forall x \lambda y. Flight(y)(x) \Rightarrow Q(x)
                                                                           \{NP.sem(VP.sem)\}
           \lambda Q. \forall x Flight(x) \Rightarrow Q(x)
                                                      NP
                                     \{\lambda Q. \forall x Flight(x) \Rightarrow Q(x)\}
                                                                     Noun
                                   Det
                    \{\lambda P.\lambda Q. \forall x P(x) \Rightarrow Q(x)\}\ \{\lambda y. Flight(y)\}
                                                                                              \{\lambda z.\exists eArrived(e) \land ArrivedThing(e, z)\}
                                                                       flight
                                  Every
```





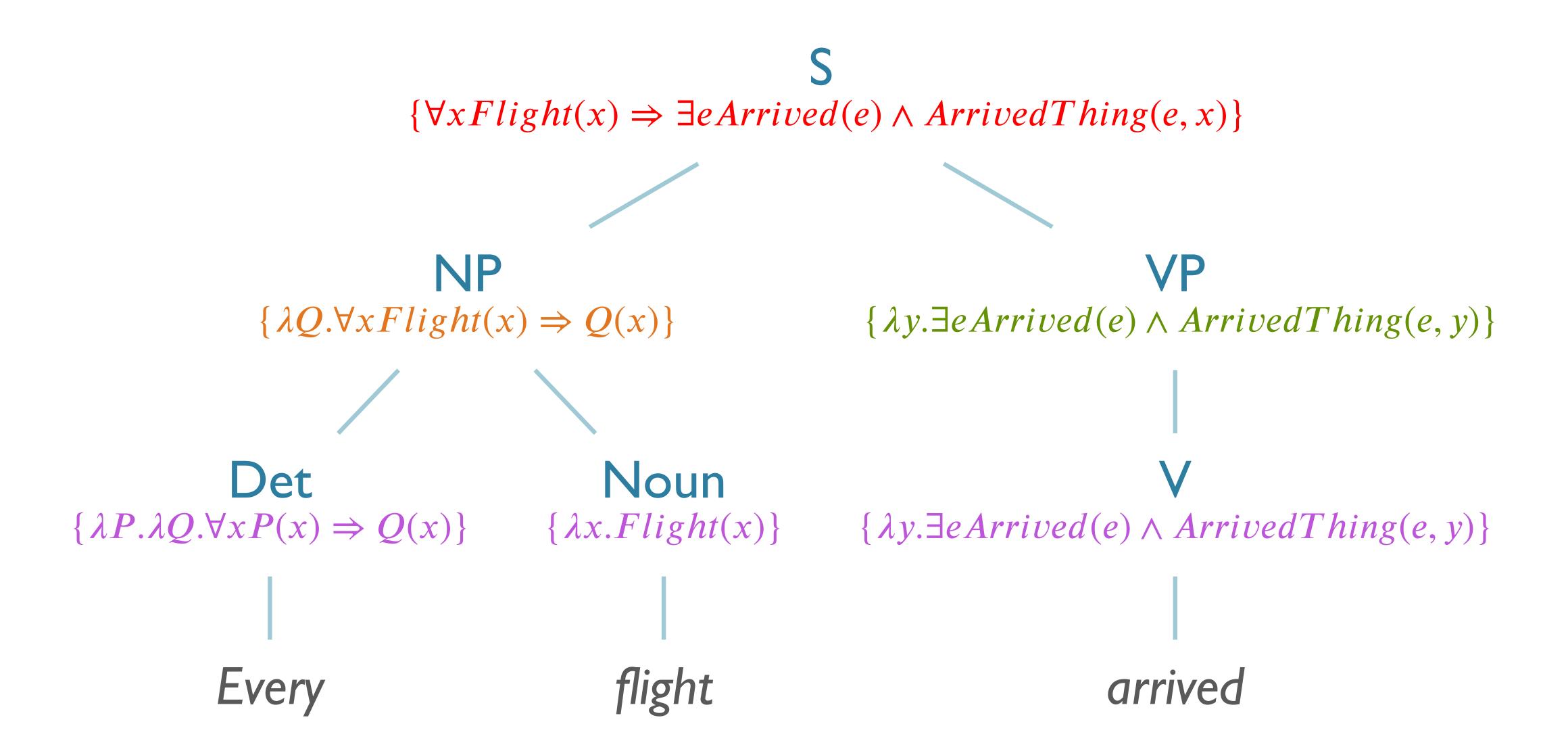
 $\begin{cases} NP.sem(VP.sem) \} \\ \\ NP \\ \\ \lambda Q. \forall xFlight(x) \Rightarrow Q(x) \} \end{cases} \begin{cases} \lambda z. \exists eArrived(e) \land ArrivedThing(e,z) \} \end{cases}$

 $\begin{cases} \forall x Flight(x) \Rightarrow \exists e Arrived(e) \land ArrivedThing(e,x) \end{cases}$ $\begin{cases} \mathsf{NP} & \mathsf{VP} \\ \{\lambda Q. \forall x Flight(x) \Rightarrow Q(x) \} \end{cases}$ $\{\lambda z. \exists e Arrived(e) \land ArrivedThing(e,z) \}$

 $\lambda Q. \forall x Flight(x) \Rightarrow Q(x)(\lambda z. \exists eArrived(e) \land ArrivedThing(e, z))$

 $\lambda Q. \forall x Flight(x) \Rightarrow Q(x) (\lambda z. \exists e Arrived(e) \land ArrivedThing(e, z))$ $\forall x Flight(x) \Rightarrow \lambda z. \exists e Arrived(e) \land ArrivedThing(e, z)(x)$ $\{\forall x Flight(x) \Rightarrow \exists e Arrived(e) \land ArrivedThing(e, x)\}$ NP $\{\lambda Q. \forall x Flight(x) \Rightarrow Q(x)\}$ $\{\lambda z. \exists e Arrived(e) \land ArrivedThing(e, z)\}$

 $\lambda Q. \forall x Flight(x) \Rightarrow Q(x) (\lambda z. \exists e Arrived(e) \land Arrived Thing(e, z))$ $\forall x Flight(x) \Rightarrow \lambda z. \exists e Arrived(e) \land Arrived Thing(e, z)(x)$ $\forall x Flight(x) \Rightarrow \exists e Arrived(e) \land Arrived Thing(e, x)$



'John booked a flight'

```
\{ \lambda P.\lambda Q.\exists x P(x) \land Q(x) \}
     Det \rightarrow 'a'
                                                                \{ \lambda P.\lambda Q. \forall x P(x) \Rightarrow Q(x) \}
  Det \rightarrow 'every'
                                                                          \{\lambda x. Flight(x)\}
  NN \rightarrow 'flight'
                               \{\lambda X.X(John)\}
NNP \rightarrow 'John'
                               \{NNP.sem\}
NP \rightarrow NNP
S \rightarrow NP VP
                               \{NP.sem(VP.sem)\}
                                                                    \{ Verb.sem(NP.sem) \}
 VP \rightarrow Verb NP
                               \{\lambda W.\lambda z. W(\exists eBooked(e) \land Booker(e,z) \land BookedThing(e,y))\}
 Verb \rightarrow `booked'
```

...we'll step through this next time.

- General approach:
 - Create complex lambda expressions with lexical items

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 - Percolate up semantics from child if non-branching
 - Apply semantics of one child to other through lambda
 - Combine elements, don't introduce new ones

Parsing with Semantics

- Implement semantic analysis in parallel with syntactic parsing
 - Enabled by this rule-to-rule compositional approach

Parsing with Semantics

- Implement semantic analysis in parallel with syntactic parsing
 - Enabled by this rule-to-rule compositional approach
- Required modifications
 - Augment grammar rules with semantics field
 - Augment chart states with meaning expression
 - Incrementally compute semantics

Sidenote: Idioms

- Not purely compositional
 - kick the bucket → die
 - tip of the iceberg → small part of the entirety
- Handling
 - Mix lexical items with constituents
 - Create idiom-specific construct for productivity
 - Allow non-compositional semantic attachments
- Extremely complex, e.g. metaphor