Computational Semantics

LING 571 — Deep Processing for NLP Shane Steinert-Threlkeld

Semantics in the News



https://apnews.com/article/supreme-court-mandatory-minimum-sentencing-drug-crimes-235b5dd23cf70bead9f8f23d659a572d

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offenders. A defendant satisfies § 3553(f)(1), as amended, if he "does not have-(A) more than 4 criminal history points, excluding any criminal history points resulting from a 1-point offense, as determined under the sentencing guidelines; (B) a prior 3-point offense, as determined under the sentencing guidelines; and (C) a prior 2-point violent offense, as determined under the sentencing guidelines." 18 U.S.C. § 3553(f)(1) (emphasis added).

The question presented is whether the "and" in 18 U.S.C. § 3553(f)(1) means "and," so that a defendant satisfies the provision so long as he does not have (A) more than 4 criminal history points, (B) a 3-point offense, and (C) a 2-point offense (as the Ninth Circuit holds), or whether the "and" means "or," so that a defendant satisfies the provision so long as he does not have (A) more than 4 criminal history points, (B) a 3- point offense, or (C) a 2-point violent offense (as the Seventh and Eighth Circuits hold).

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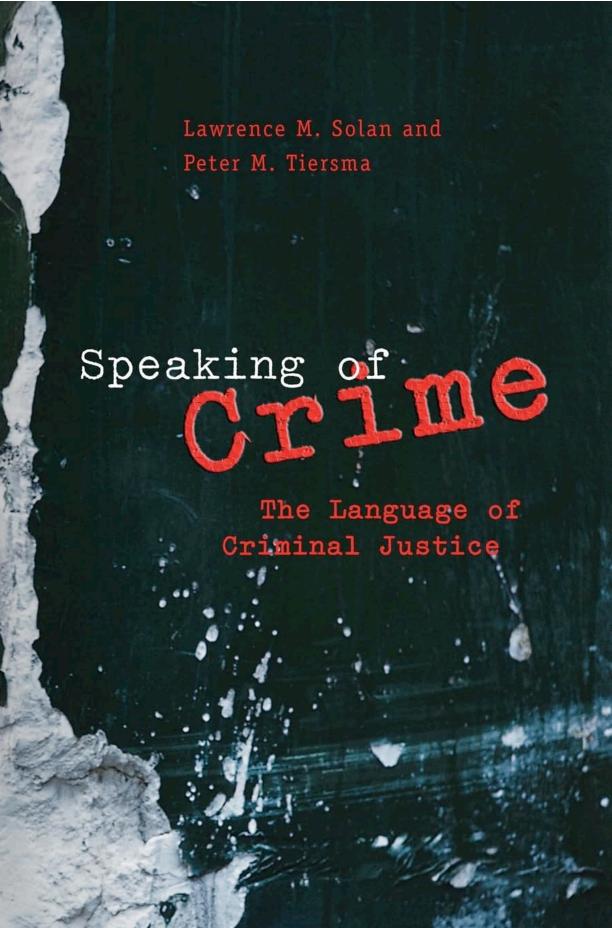
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Python Nugget of the Week

Sequential logical operators:

- An alternative here: defaultdict with default values for BP
- "or" also therefore useful for conditional assignment (e.g. x = False or 42)

Varieties of Entailment in the News

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 - "We are talking on Zoom right now."
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 - The former, but not the latter, entails that we are talking right now.
- Presuppositions (that there is a king) "project out" from negation (and other operators, like questions, conditionals, etc). Standard logical entailments do not.
 - Presuppositions must be true in order for a sentence to be true or false at all.

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- Trump's doctor when he was at the hospital with COVID-19:
 - Press: "Has he ever been on supplemental oxygen?"
 - Doc: "He hasn't had supplemental oxygen today or yesterday."

"Several students were told that the exam will be postponed."

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 - Not every student was told that the exam will be postponed.

An Interesting Example

A top baseball prospect's Southern California scholarship was lost to the pandemic

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"A prospect's scholarship": presupposes there is a scholarship Rest of headline: there is no more scholarship Complex compositional interaction between tense and presupposition

Roadmap

- First-order Logic: Syntax and Semantics
- Inference + Events
- Rule-to-rule Model
 - More lambda calculus

FOL Syntax + Semantics

Example Meaning Representation

A non-stop flight that serves Pittsburgh:

 $\exists x \ Flight(x) \land Serves(x, Pittsburgh) \land Non-stop(x)$

FOL Syntax Summary

```
Formula
                                                         Connective →
                              AtomicFormula
                                                                                         \wedge | \vee | \Rightarrow
                       Formula Connective Formula
                                                          Quantifier
                                                                                           AIB
                                                                             VegetarianFood | Maharani | ...
                      Quantifier Variable, ... Formula
                                                           Constant
                                                           Variable
                                 ¬ Formula
                                                                                        x \mid y \mid \dots
                                 (Formula)
                                                          Predicate
                                                                                   Serves | Near | ...
                                                                               LocationOf | CuisineOf | ...
AtomicFormula
                                                           Function
                            Predicate(Term,...)
                             Function(Term,...)
      Term
                                  Constant
                                  Variable
```

J&M p. 556 (<u>3rd ed. F.3</u>)

Model-Theoretic Semantics

- A "model" represents a particular state of the world
- Our language has logical and non-logical elements.
 - Logical: Symbols, operators, quantifiers, etc
 - Non-Logical: Names, properties, relations, etc

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- Properties sets of elements
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- Relations sets of tuples of elements
 - CapitalCity: {(Washington, Olympia), (Yamoussokro, Cote d'Ivoire), (Ulaanbaatar, Mongolia),...}

via J&M, p. 554

Sample Domain D

Objects

Matthew, Franco, Katie, Caroline Frasca, Med, Rio Italian, Mexican, Eclectic

a,b,c,d e,f,g h,i,j

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Frasca, Med, and Rio are noisy Noisy

Noisy={*e,f,g*}

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Relations

Likes

Matthew likes the Med

Katie likes the Med and Rio

Franco likes Frasca

Caroline likes the Med and Rio

Likes=
$$\{ \langle a,f \rangle, \langle c,f \rangle, \langle c,g \rangle, \langle b,e \rangle, \langle d,f \rangle, \langle d,g \rangle \}$$

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Noisy={*e*,*f*,*g*}

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Serves Med serves eclectic

Rio serves Mexican Frasca serves Italian

Likes=
$$\{ \langle a,f \rangle, \langle c,f \rangle, \langle c,g \rangle, \langle b,e \rangle, \langle d,f \rangle, \langle d,g \rangle \}$$

Serves={
$$\langle c, f \rangle$$
, $\langle f, i \rangle$, $\langle e, h \rangle$ }

Rule-to-Rule Model

Recap

- Meaning Representation
 - Can represent meaning in natural language in many ways
 - We are focusing on First-Order Logic (FOL)

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Principle of compositionality

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Principle of compositionality

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Lambda Calculus

- λ-expressions denote functions
- Can be nested
- Reduction = function application

Semantics Reflects Syntax

Chiasmus:

Syntax affects Semantics!





Bowie playing Tesla

The Prestige (2006)

Tesla playing Bowie

SpaceX Falcon Heavy Test Launch (2/6/2018)

Chiasmus: Syntax affects Semantics!

• "Never let a fool kiss you or a kiss fool you" (Grothe, 2002)

• "Then you should say what you mean," the March Hare went on.

"I do," Alice hastily replied; "at least—at least I mean what I say—that's the same thing, you know."

"Not the same thing a bit!" said the Hatter. "Why, you might just as well say that 'I see what I eat' is the same thing as 'I eat what I see'!"

"You might just as well say," added the March Hare, "that 'I like what I get' is the same thing as 'I get what I like'!"

"You might just as well say," added the Dormouse, which seemed to be talking in his sleep, "that 'I breathe when I sleep' is the same thing as 'I sleep when I breathe'!"

—Alice in Wonderland, Lewis Carrol

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State of known Universe: 02/05/2018

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Teslas

Things in Space

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Scope Ambiguity

- Potentially O(n!) scope interpretations ("scopings")
 - Where n=number of scope-taking operators.
 - (every, a, all, no, modals, negations, conditionals, ...)
- Different interpretations correspond to different syntactic parses!

Derivative of an alleged Groucho Marx-ism:

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- In the US, a woman gives birth every fifteen minutes.

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Thank you scope ambiguity! (Not the same as attachment ambiguity.)

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 - Source: https://www.npr.org/2021/11/02/1051720391/boston-mayor- michelle-wu-elected

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```
(ROOT
(S
(NP (NNP Boston) (NNS voters))
(VP (VBP have)
(VP (VBP have)
(NP
(NP
(NP
(NP
(NP (NNP City) (NNP Councilor) (NNP Michelle) (NNP Wu))
(PP (IN as)
(NP (NN mayor))))
(, ,)
(NP
(NP (NP (DT the) (NN city) (POS 's))
(JJ first) (NN woman))
(CC and)
(NP
(NP (NN person))
(PP (IN of)
(NP
(NP (NN color))
(VP (VBN elected)
(PP (IN to)
(NP (NN post))))))))))
(...)))
```

Integrating Semantics into Syntax

1. Pipeline System

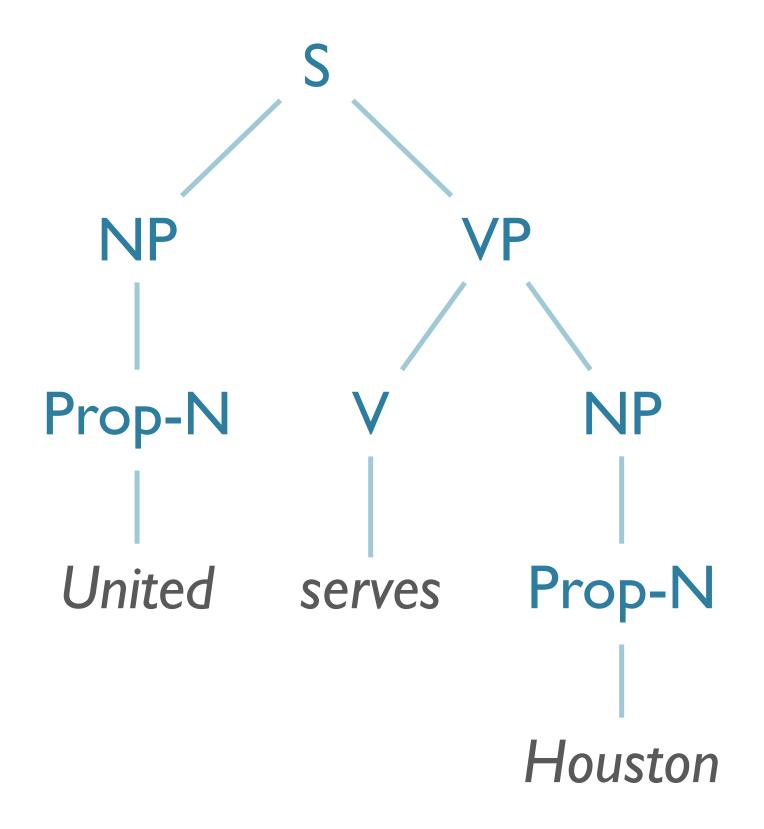
- 1. Feed parse tree and sentence to semantic analyzer
- 2. How do we know which pieces of the semantics link to which part of the analysis?
- 3. Need detailed information about sentence, parse tree
- 4. Infinitely many sentences & parse trees
- 5. Semantic mapping function per parse tree → intractable

Integrating Semantics into Syntax

Integrating Semantics into Syntax

- 2. Integrate Directly into Grammar
 - 1. This is the "rule-to-rule" approach we've been implicitly examining and will now make more explicit
 - 2. Tie semantics to finite components of grammar (rules & lexicon)
 - 3. Augment grammar rules with semantic info
 - 1. a.k.a. "attachments" specify how RHS elements compose to LHS

United serves Houston

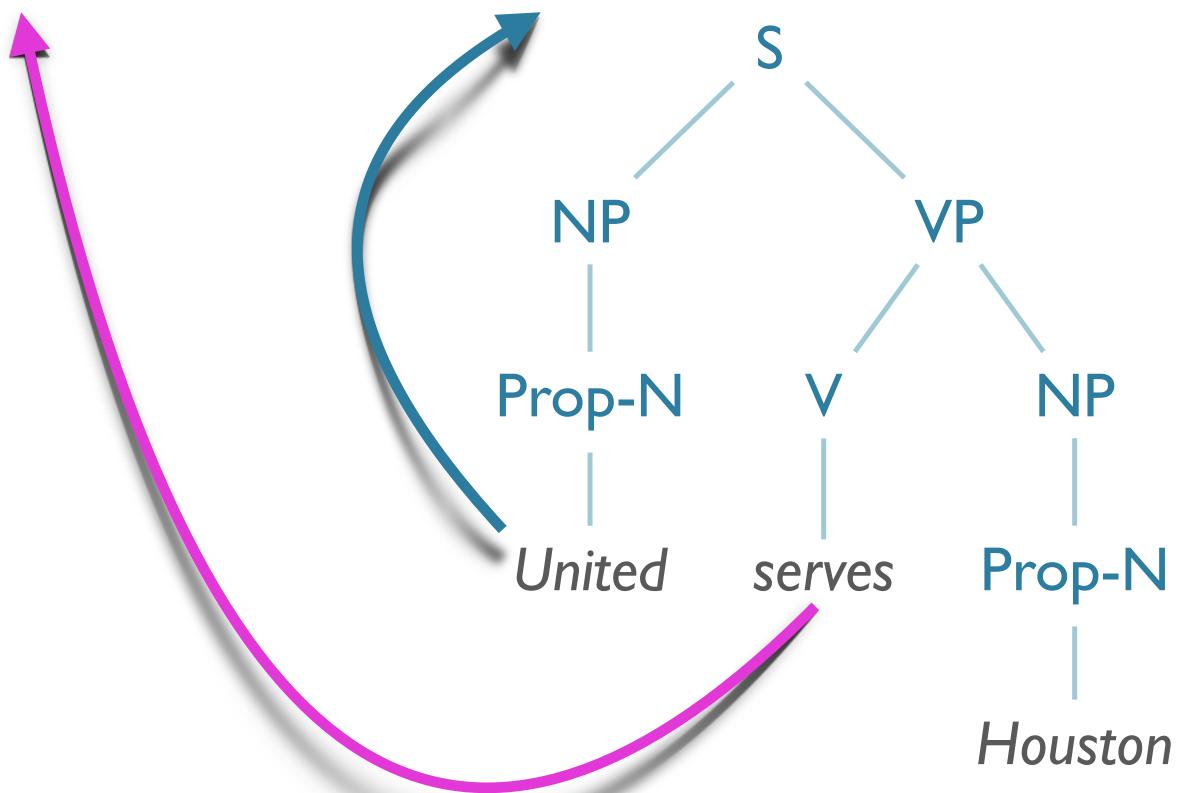


United serves Houston

 $\exists e(Serving(e) \land$ NP Prop-N NP United Prop-N serves Houston

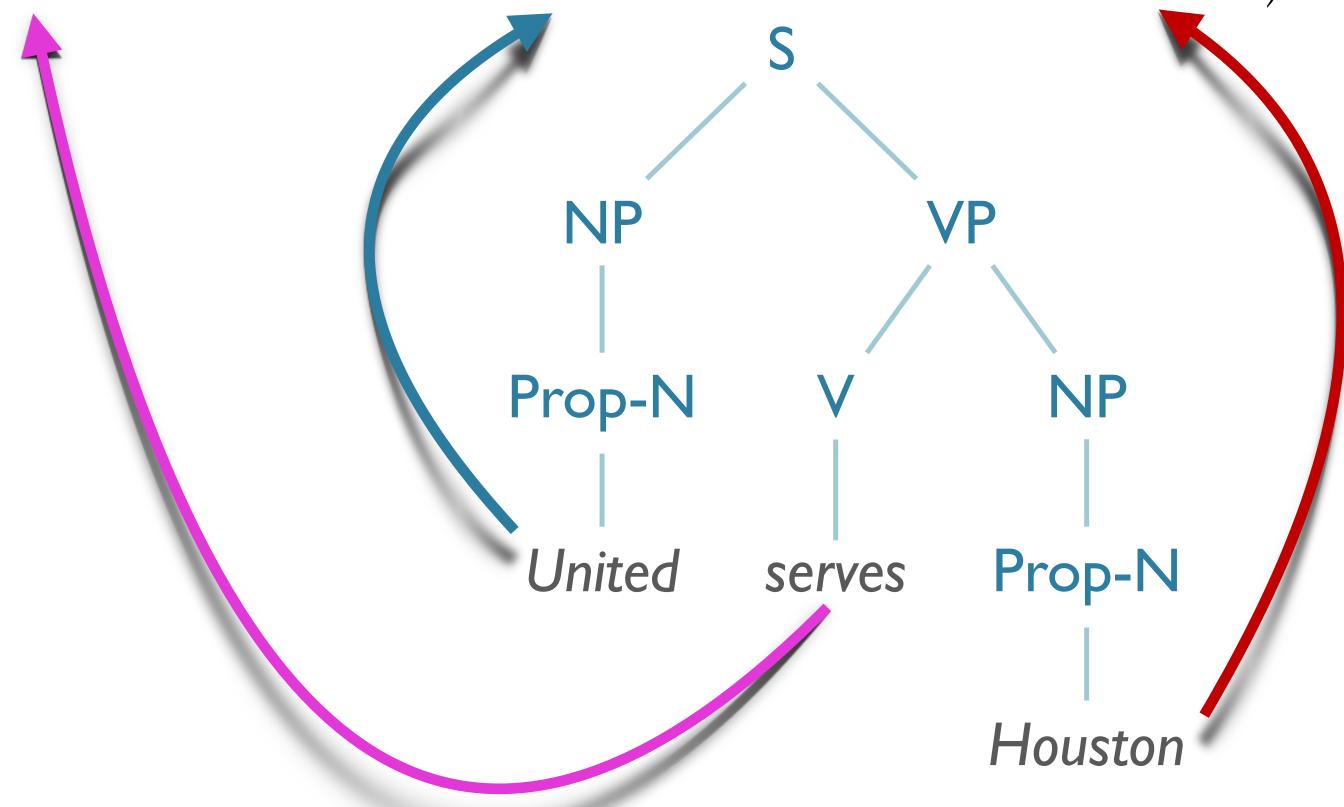
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 $\exists e(Serving(e) \land Server(e, United) \land$



United serves Houston

 $\exists e(Serving(e) \land Server(e, United) \land Served(e, Houston))$



Rule-to-rule Model

- Lambda Calculus and the Rule-to-Rule Hypothesis
 - \bullet λ -expressions can be attached to grammar rules
 - used to compute meaning representations from syntactic trees based on the principle of compositionality
 - Go up the tree, using reduction (function application) to compute meanings at non-terminal nodes

Semantic Attachments

Basic Structure:

$$A \rightarrow a_1, ..., a_n \{f(a_j.sem, ..., a_k.sem)\}$$

Semantic Function

In NLTK syntax (more later):

$$A \rightarrow a_1 \dots a_n[SEM=]$$

Attachments as SQL!

NLTK book, ch. 10

```
>>> nltk.data.show cfg('grammars/book grammars/sql0.fcfg')
% start S
S[SEM=(?np + WHERE + ?vp)] \rightarrow NP[SEM=?np] VP[SEM=?vp]
VP[SEM=(?v + ?pp)] \rightarrow IV[SEM=?v] PP[SEM=?pp]
VP[SEM=(?v + ?ap)] \rightarrow IV[SEM=?v] AP[SEM=?ap]
NP[SEM=(?det + ?n)] -> Det[SEM=?det] N[SEM=?n]
PP[SEM=(?p + ?np)] \rightarrow P[SEM=?p] NP[SEM=?np]
AP[SEM=?pp] -> A[SEM=?a] PP[SEM=?pp]
NP[SEM='Country="greece"'] -> 'Greece'
NP[SEM='Country="china"'] -> 'China'
Det[SEM='SELECT'] -> 'Which' | 'What'
N[SEM='City FROM city_table'] -> 'cities'
IV[SEM=''] -> 'are'
A[SEM=''] -> 'located'
P[SEM=''] -> 'in'
```

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PP[SEM=(?p + ?np)] \rightarrow P[SEM=?p] NP[SEM=?np]
AP[SEM=?pp] -> A[SEM=?a] PP[SEM=?pp]
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'What cities are located in China'

parses[0]: SELECT City FROM city_table WHERE Country="china"

Semantic Attachments: Options

- Why not use SQL? Python?
 - Arbitrary power but hard to map to logical form
 - No obvious relation between syntactic, semantic elements
- Why Lambda Calculus?
 - First Order Predicate Calculus (FOPC) + function application is highly expressive, integrates well with syntax
 - Can extend our existing feature-based model, using unification
 - Can 'translate' FOL to target / task / downstream language (e.g. SQL)

Semantic Analysis Approach

- Semantic attachments:
 - Each CFG production gets semantic attachment
- Semantics of a phrase is function of combining the children
 - Complex functions need to have parameters
 - Verb → 'arrived'
 - Intransitive verb, so has one argument: *subject*
 - ...but we don't have this available at the preterminal level of the tree!

Defining Representations

- Proper Nouns
- Intransitive Verbs
- Transitive Verbs
- Quantifiers

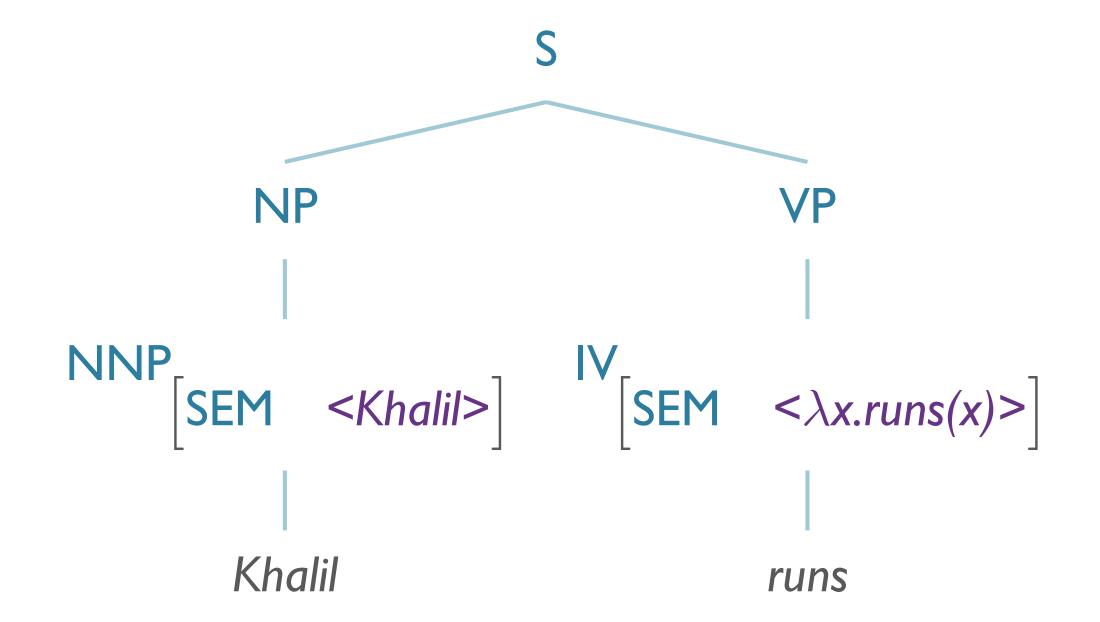
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 - NNP[SEM=<Khalil>] → 'Khalil'

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- However, we will want to apply our λ -closures left-to-right consistently.

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S[SEM=np?(vp?)] \rightarrow NP[SEM=np?] VP[SEM=vp?]
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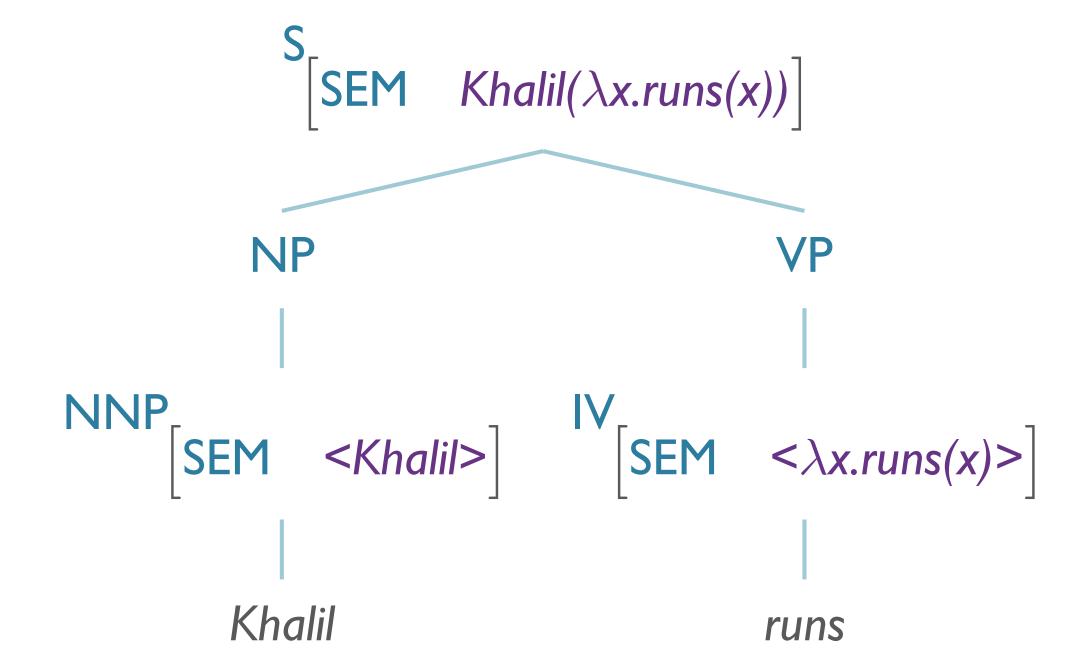
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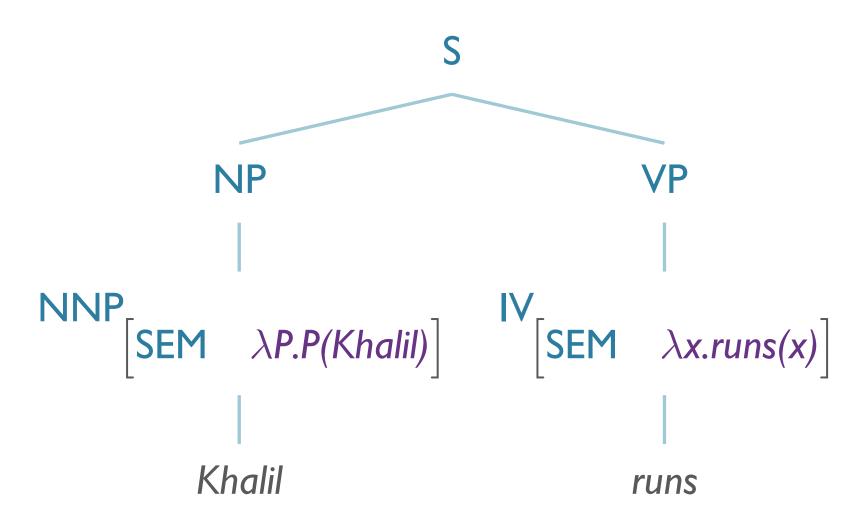
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S[SEM=np?(vp?)] \rightarrow NP[SEM=np?] VP[SEM=vp?]
```

```
[SEM | Khalil(\lambda x.runs(x))] \longrightarrow ERROR: Constant "Khalil" is not a function!
NP \qquad VP
| \qquad | \qquad | \qquad |
NNP[SEM | < Khalil >] \qquad | [SEM | < \lambda x.runs(x) >]
| \qquad | \qquad | \qquad |
Khalil \qquad runs
```

- Instead, we use a dummy predicate:
 - $\bullet \lambda Q.Q(Khalil)$
- "Generalizing to the worst case" (cf. Montague; Partee on type-shifting)
 - I.e.: this move will also be necessary for a uniform semantic treatment of NPs, which can be individual-denoting (like names) or more complex (quantifiers)

- With the dummy predicate:
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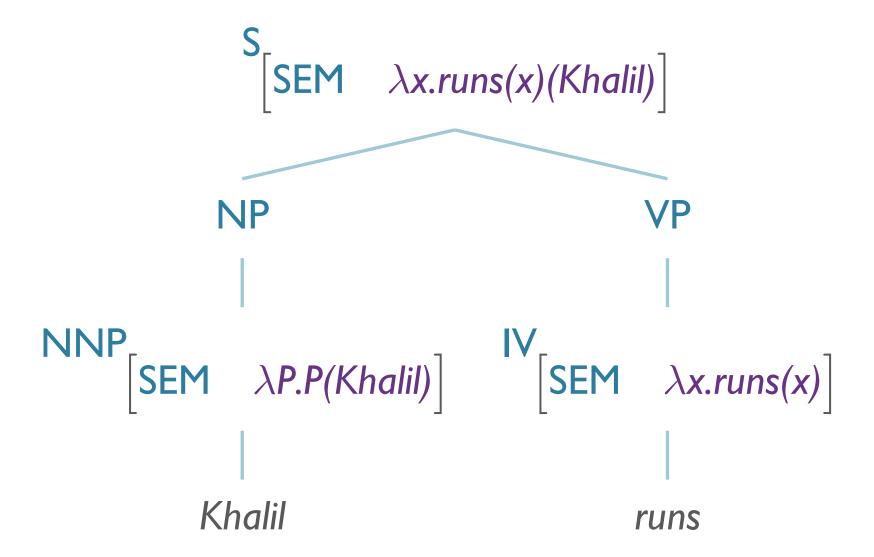
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```
\begin{bmatrix} \mathsf{SEM} & \lambda P.P(Khalil)(\lambda x.runs(x)) \end{bmatrix} \\ \mathsf{NP} & \mathsf{VP} \\ | & | & | \\ \mathsf{NNP} \\ [\mathsf{SEM} & \lambda P.P(Khalil)] & \mathsf{IV} \\ \mathsf{SEM} & \lambda x.runs(x) \end{bmatrix} \\ | & | & | \\ \mathsf{Khalil} & \mathsf{runs} \end{bmatrix}
```

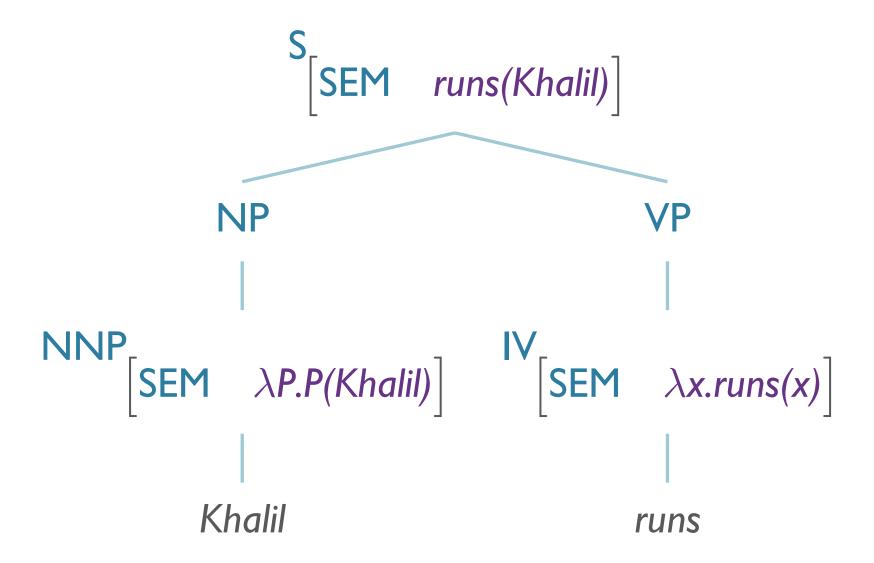
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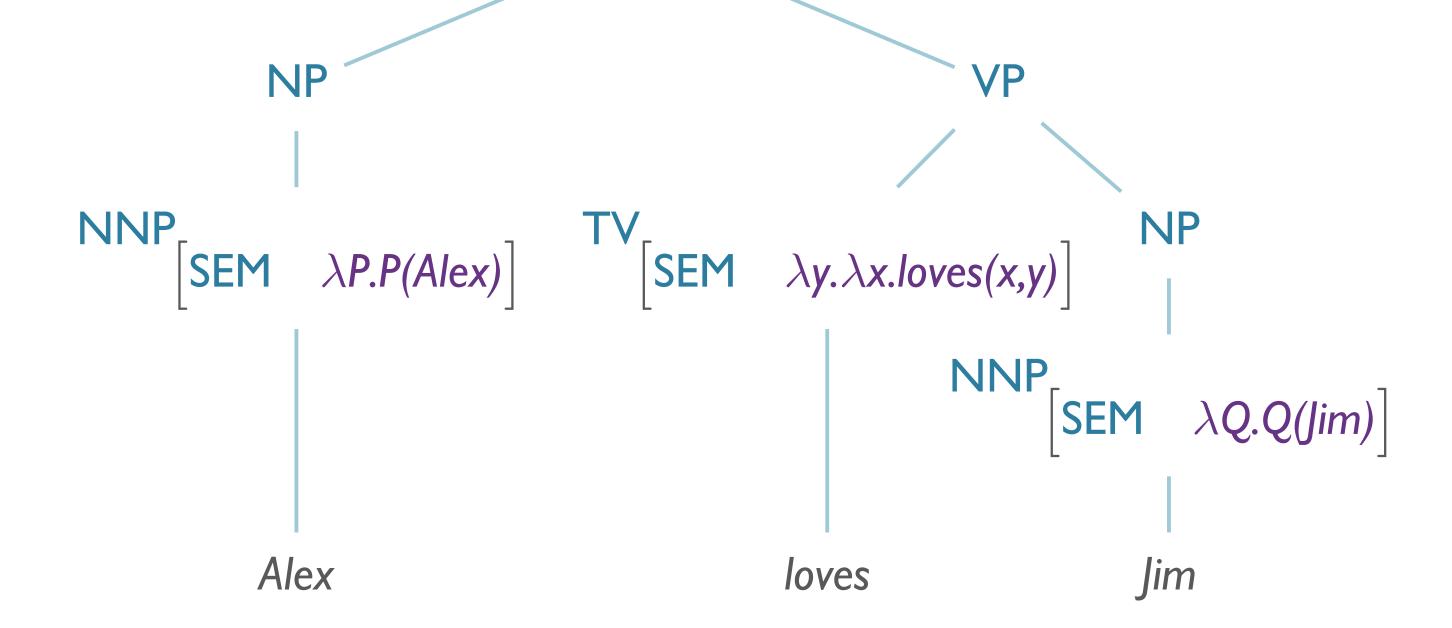


- So, if we want to say "Alex loves Jim" we would intuitively want $\lambda y.\lambda x.loves(x,y)$
- ... going in linear order, we have one arg to the left and one to the right.

• So, if we want to say "Alex loves Jim" we would want $\lambda y \cdot \lambda x \cdot loves(x, y)$

• ...but going in linear order, we have one arg to the left and one to the

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TV(NP): • $\lambda y \cdot \lambda x \cdot loves(x, y) (\lambda Q \cdot Q(Jim))$

• TV(NP): • $\lambda y \cdot \lambda x \cdot loves(x, y) (\lambda Q \cdot Q(Jim))$ • $\lambda x.loves(x,\lambda Q.Q(Jim))$

• TV(NP): • $\lambda y \cdot \lambda x \cdot loves(x, y) (\lambda Q \cdot Q(Jim))$ • $\lambda x.loves(x,\lambda Q.Q(Jim))$ ● → Error! We can't reduce Jim.

```
• TV(NP):
  • \lambda y \cdot \lambda x \cdot loves(x, y) (\lambda Q \cdot Q(Jim))
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    ● → Error! We can't reduce Jim.
• Instead: \lambda \mathbf{x} \cdot \mathbf{x} \cdot \mathbf{y} \cdot loves(\mathbf{x}, \mathbf{y}))
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 ("Continuation-passing")
```

TV(NP):

```
• \lambda \mathbf{Y} \times \mathbf{Y}(\lambda \mathbf{y}.loves(\mathbf{x}, \mathbf{y})) (\lambda \mathbf{Q}.\mathbf{Q}(\mathbf{Jim}))
```

```
• \lambda Y \times Y (\lambda y. loves(x, y)) (\lambda Q.Q(Jim)) \lambda Y \text{ takes } (\lambda Q.Q(Jim))
• \lambda x.(\lambda Q.Q(Jim)(\lambda y.loves(x,y))
```

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                                                                  \lambda Q takes (\lambda y.loves(x,y))
• \lambda x.(\lambda y.loves(x,y)(Jim))
                                                                  \lambda y takes (Jim)
• \lambda x.(loves(x, Jim))
```

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\lambda Y takes (\lambda Q.Q(Jim))
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```

- NP(VP):
 - $\lambda P.P(Alex)(\lambda x.(loves(x, Jim)))$

• TV(NP): • $\lambda \mathbf{Y} \times \mathbf{Y}(\lambda \mathbf{y}.loves(\mathbf{x}, \mathbf{y})) (\lambda \mathbf{Q}.\mathbf{Q}(\mathbf{Jim}))$ • $\lambda x.(\lambda Q.Q(Jim)(\lambda y.loves(x,y))$ • $\lambda x.(\lambda y.loves(x,y)(Jim))$ • $\lambda x. (loves(x, Jim))$ • $\lambda P.\dot{P}(Alex)(\lambda x.(loves(x,Jim)))$

• $\lambda x.(loves(x, Jim)(Alex))$

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 • \lambda P.P(Mlex)(\lambda x.(loves(x,Jim)))
  • \lambda x. (loves (x, Jim) (Alex)
 • loves(Alex, Jim)
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Converting to an Event

- "x loves y," Originally:
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- as a Neo-Davidsonian event:
 - $\lambda \mathbf{Y} \times \mathbf{Y}(\lambda \mathbf{y}.\exists \mathbf{e} \text{ love}(\mathbf{e}) \land \text{ lover}(\mathbf{e},\mathbf{x}) \land \text{ loved}(\mathbf{e},\mathbf{y}))$

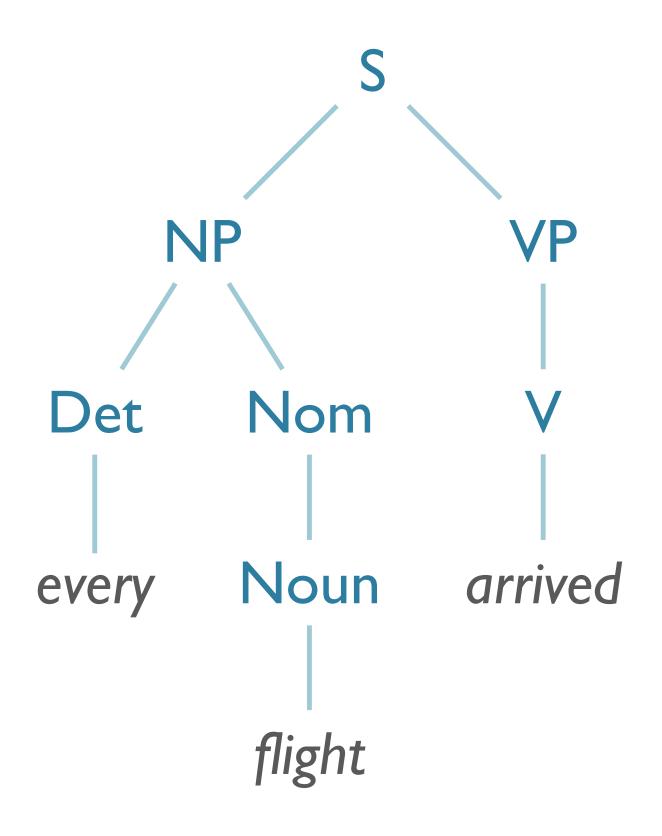
Quantifiers & Scope

Semantic Analysis Example

- Basic model
 - Neo-Davidsonian event-style model
 - Complex quantification

Example: Every flight arrived

 $\forall x \ Flight(x) \Rightarrow \exists e \ Arrived(e) \land ArrivedThing(e,x)$



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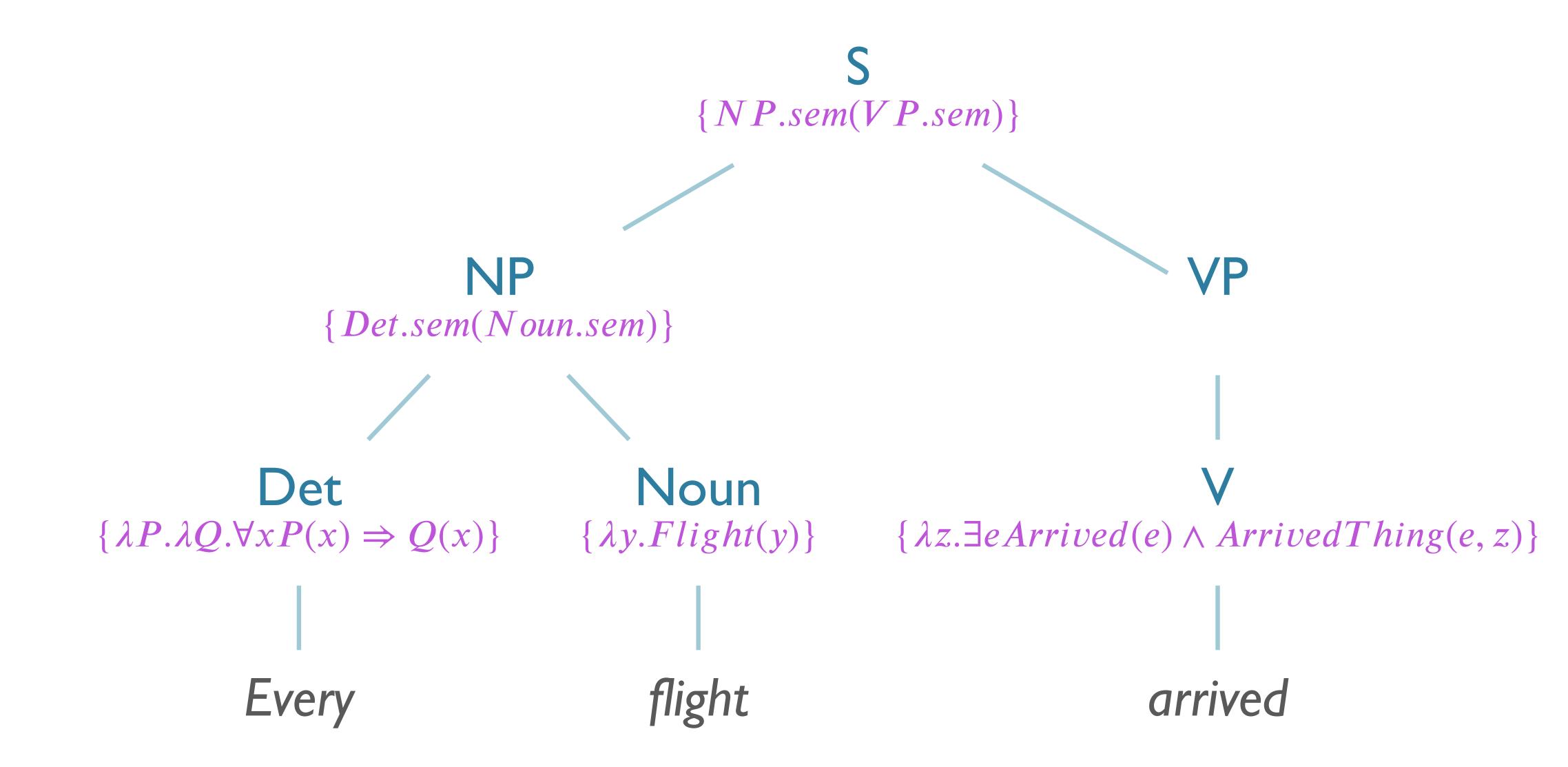
- "Every flight" is:
 - $\lambda Q. \forall x Flight(x) \Rightarrow Q(x)$
- ...so what is the representation for "every"?
 - $\bullet \quad \lambda P. \lambda Q. \forall x P(x) \Rightarrow Q(x)$

"A flight arrived"

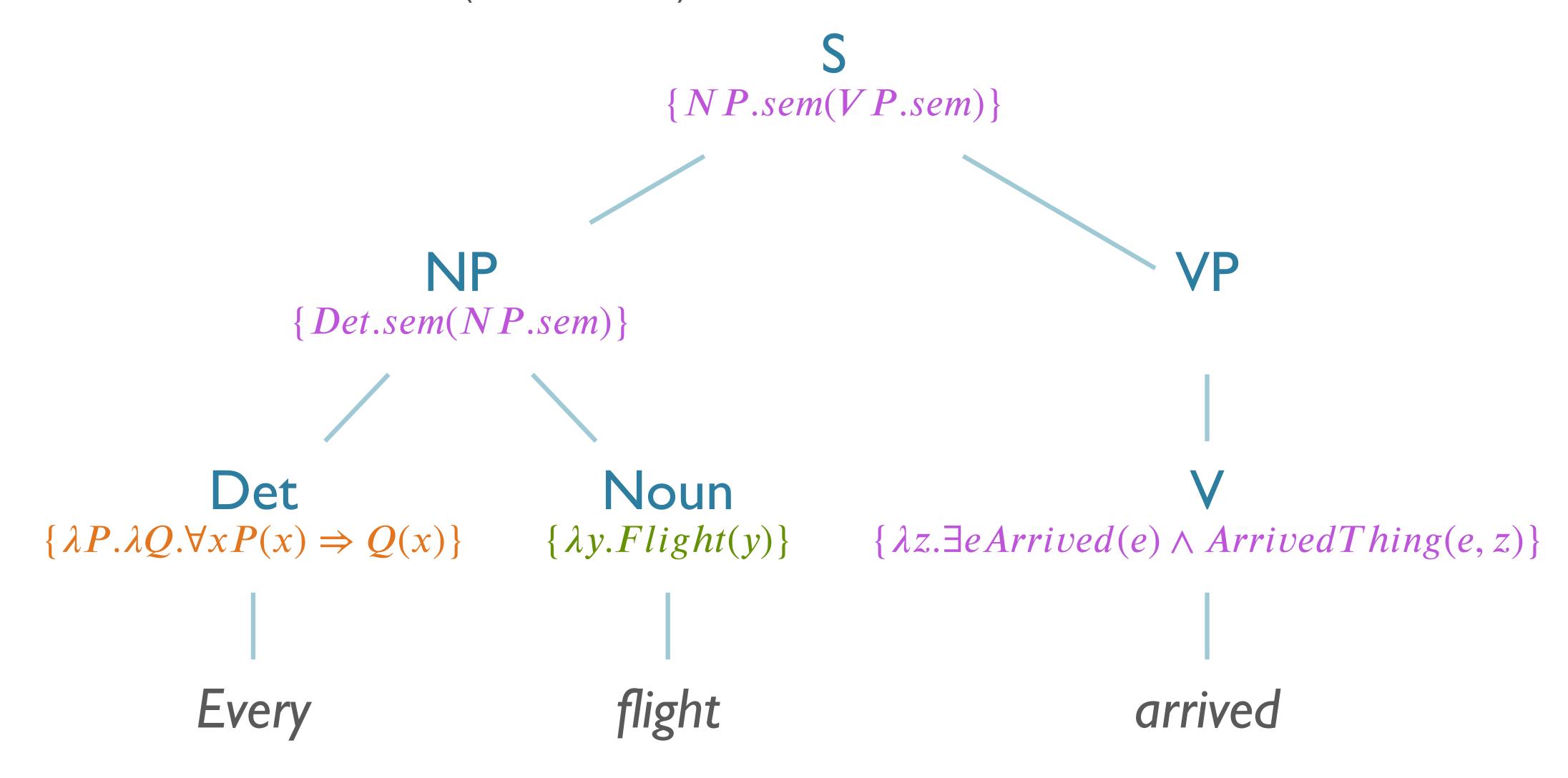
- We just need one item for truth value
 - So, start with ∃x...
 - $\lambda P.\lambda Q.\exists x P(x) \land Q(x)$

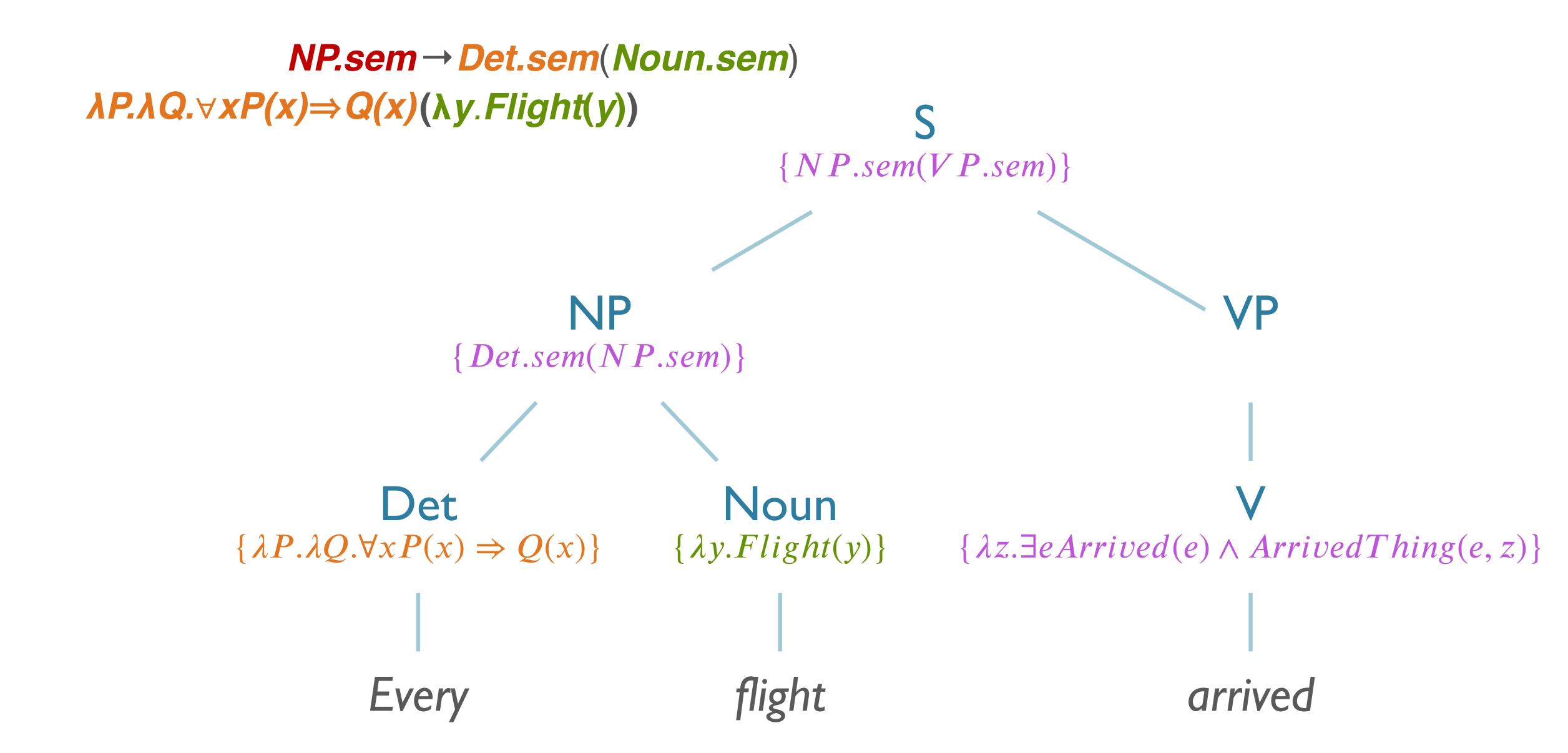
Creating Attachments

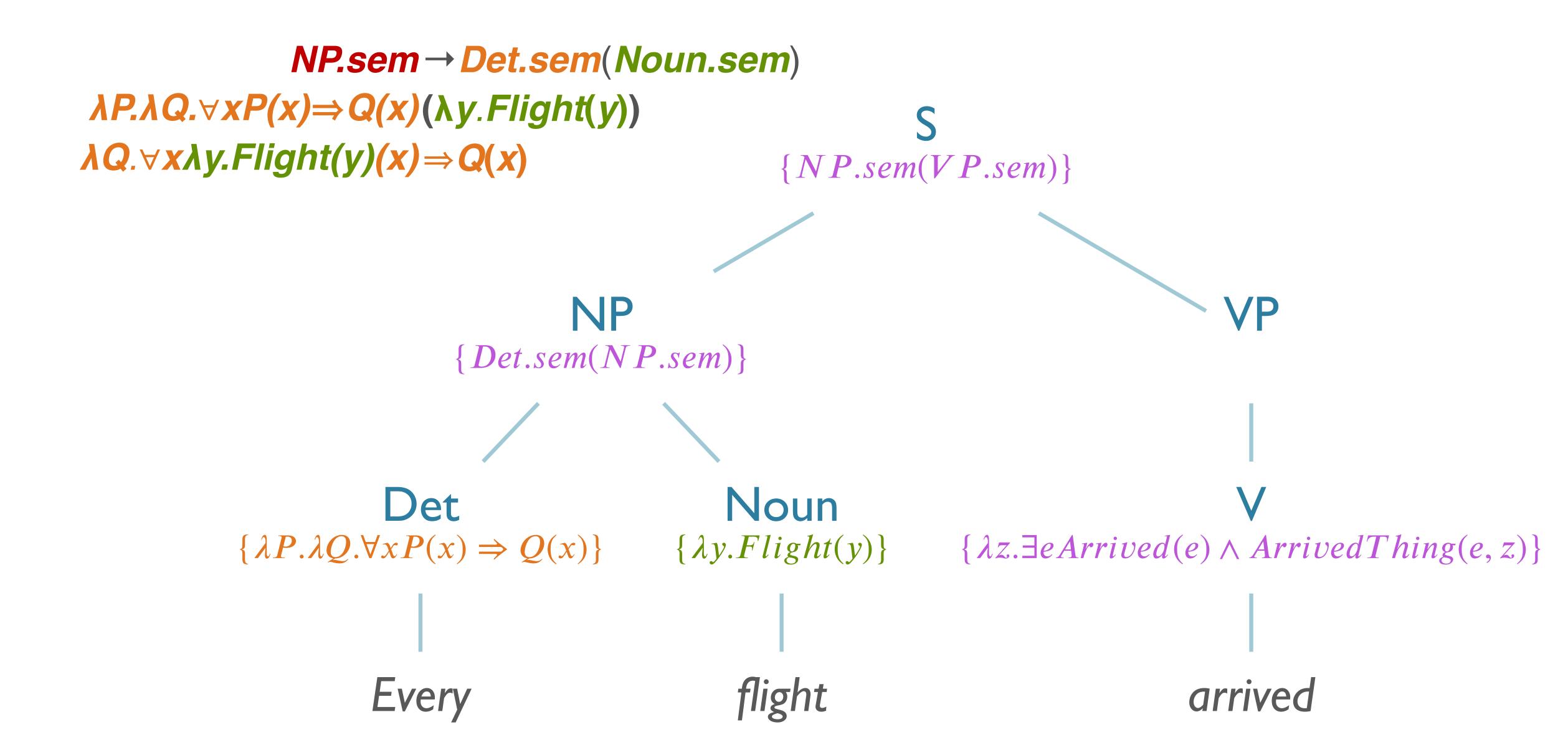
```
\{ \lambda P.\lambda Q. \forall \mathbf{x} P(\mathbf{x}) \Rightarrow Q(\mathbf{x}) \}
Det \rightarrow 'Every'
Noun → 'flight'
                                  \{ \lambda x.Flight(x) \}
                                  \{\lambda y. \exists eArrived(e) \land ArrivedThing(e, y)\}
          → 'arrived'
Verb
VP
          → Verb
                                  { Verb.sem }
Nom → Noun
                                  { Noun.sem }
          → NP VP
                                  { NP.sem(VP.sem) }
                                { Det.sem(Nom.sem) }
       → Det Nom
```

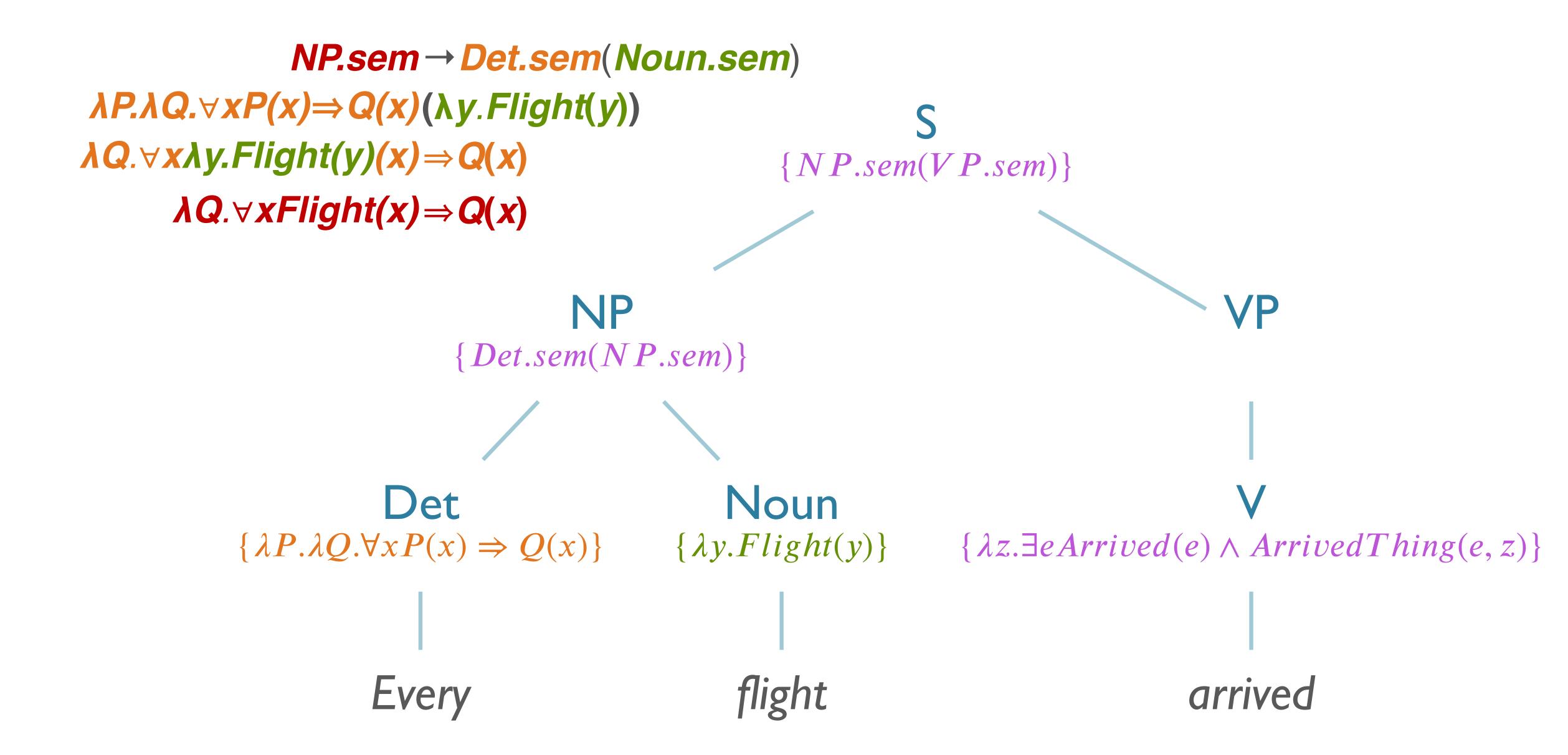


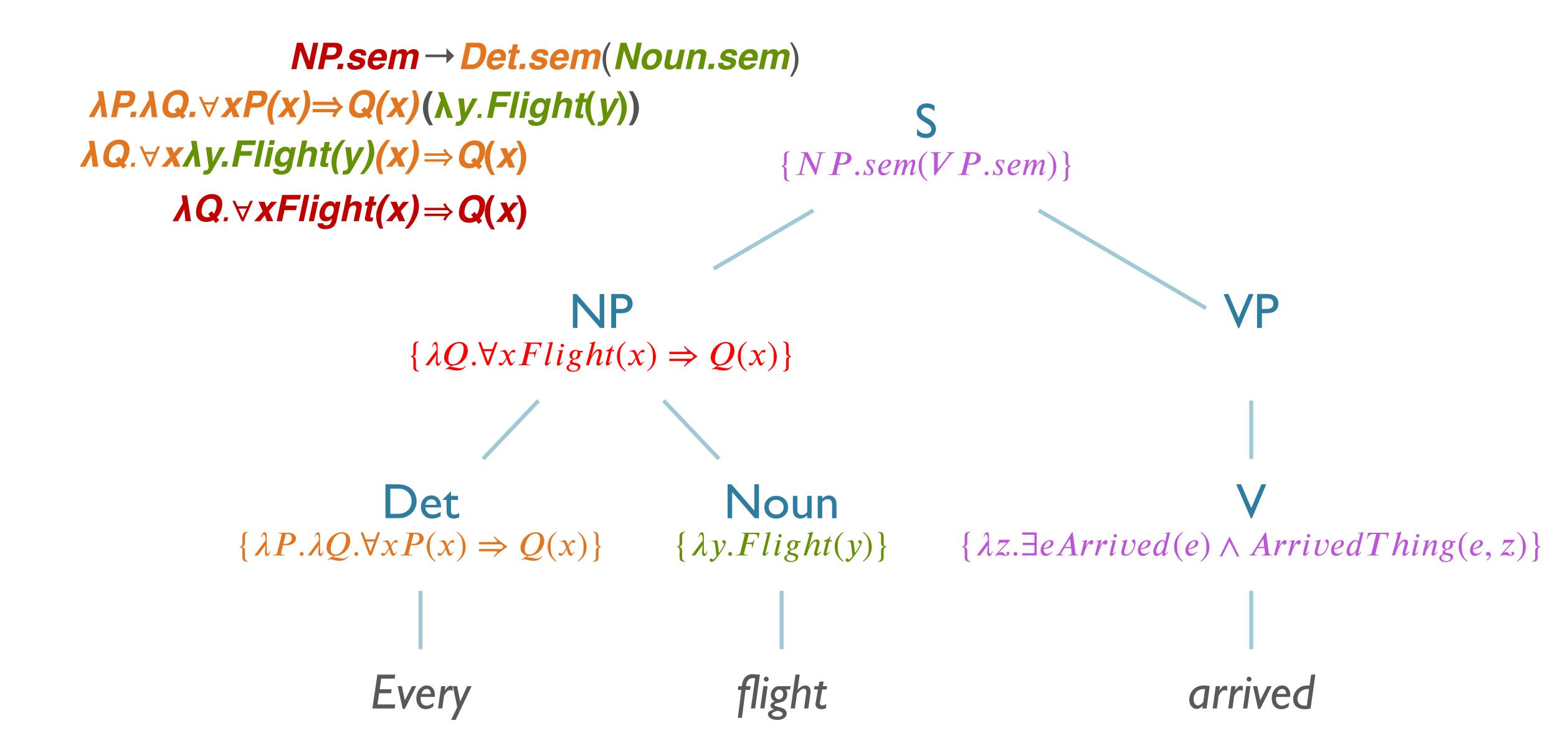
NP.sem → *Det.sem*(*Noun.sem*)

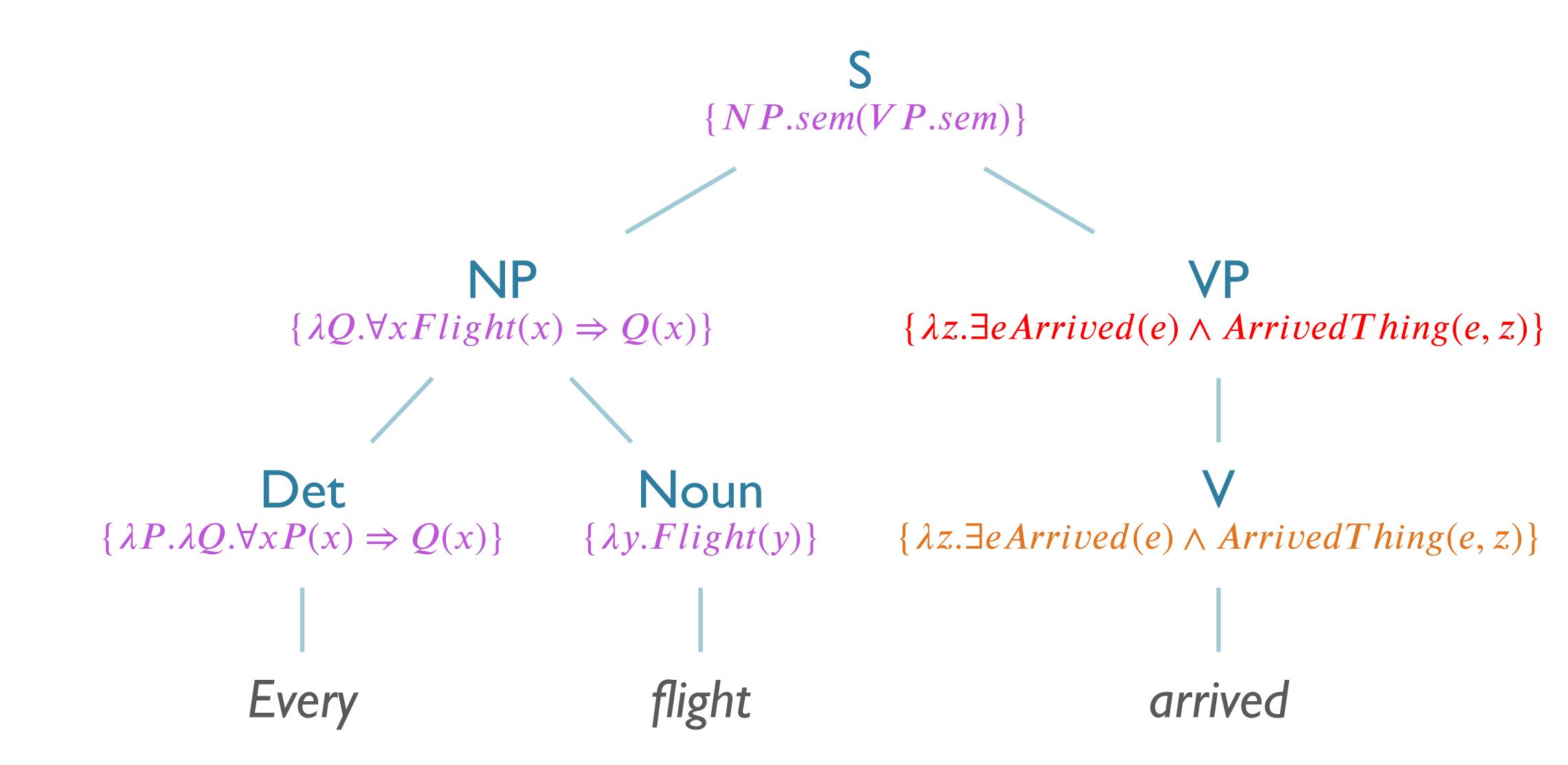


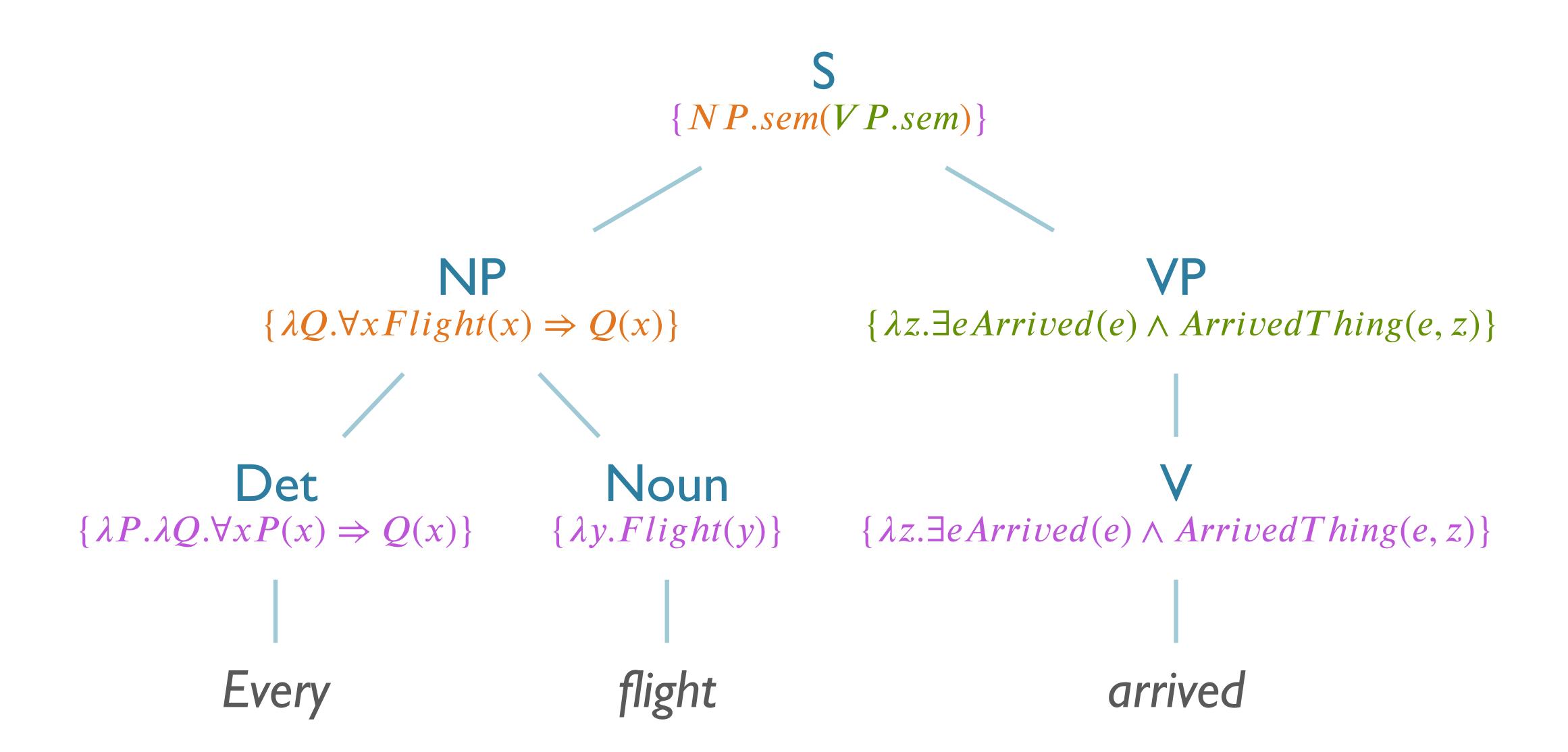




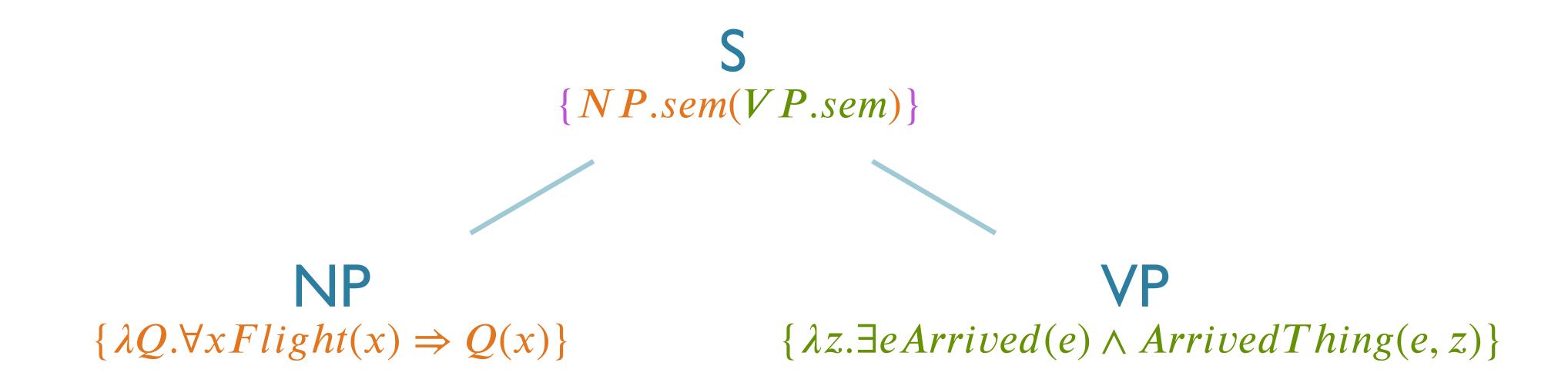








 $\{NP.sem(VP.sem)\}$ **VP** NP $\{\lambda Q. \forall x Flight(x) \Rightarrow Q(x)\}$ $\{\lambda z.\exists eArrived(e) \land ArrivedThing(e, z)\}$



 $\lambda Q. \forall x Flight(x) \Rightarrow Q(x)(\lambda z. \exists eArrived(e) \land ArrivedThing(e, z))$

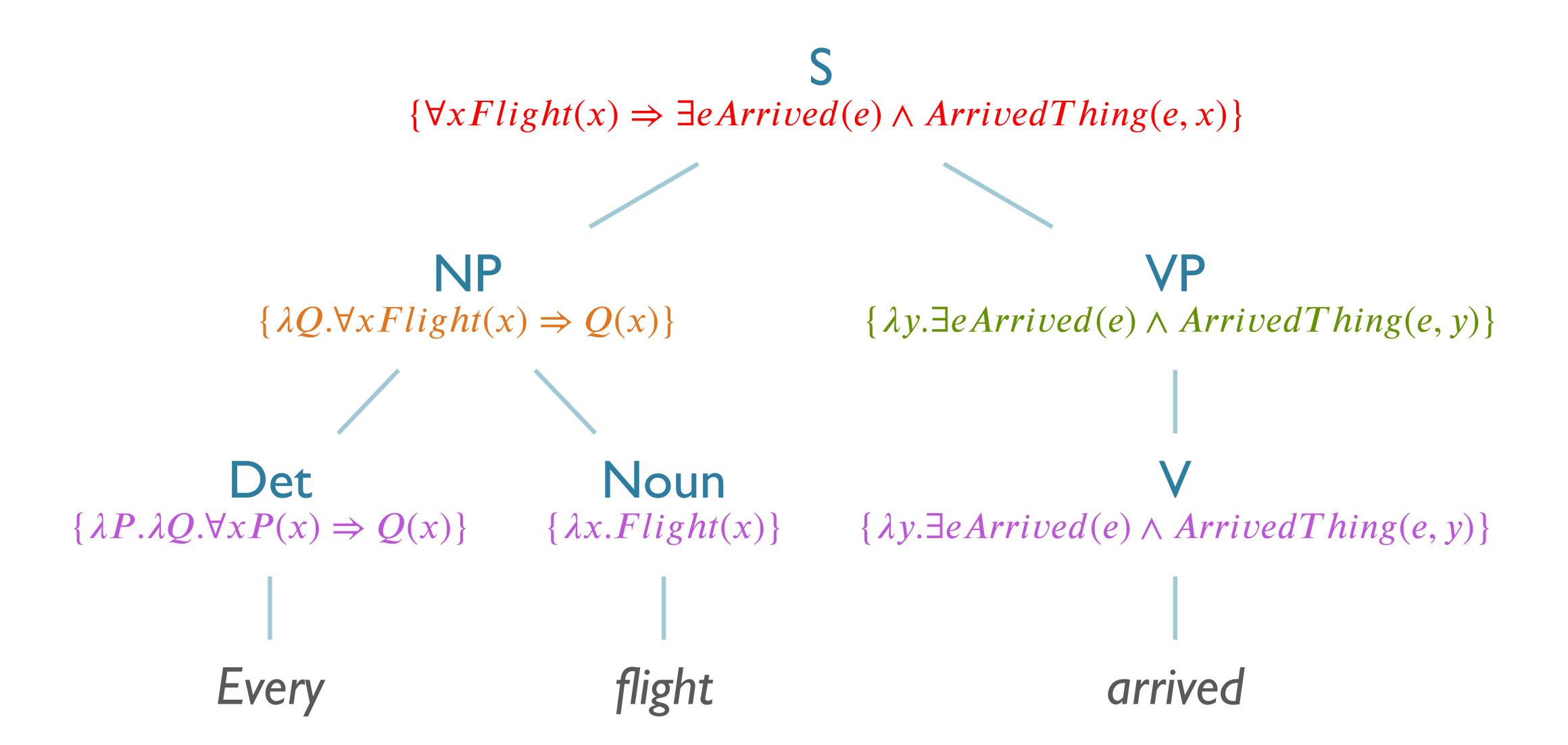
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 $\lambda Q. \forall x Flight(x) \Rightarrow Q(x)(\lambda z. \exists eArrived(e) \land ArrivedThing(e, z))$ $\forall x Flight(x) \Rightarrow \lambda z. \exists eArrived(e) \land ArrivedThing(e, z)(x)$

```
 \begin{cases} NP.sem(VP.sem) \} \\ \\ NP \\ \\ \lambda Q. \forall xFlight(x) \Rightarrow Q(x) \} \end{cases}   \{\lambda z. \exists eArrived(e) \land ArrivedThing(e,z) \}
```

```
\lambda Q. \forall x Flight(x) \Rightarrow Q(x)(\lambda z. \exists e Arrived(e) \land ArrivedThing(e, z))
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\forall x Flight(x) \Rightarrow \exists e Arrived(e) \land ArrivedThing(e, x)
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'John booked a flight'

```
\{ \lambda P. \lambda Q. \exists x P(x) \land Q(x) \}
Det \rightarrow 'a'
                               \{ \lambda P. \lambda Q. \forall x P(x) \Rightarrow Q(x) \}
Det → 'every'
NN \rightarrow 'flight'
                               \{\lambda x.Flight(x)\}
NNP → 'John'
                               \{\lambda X.X(John)\}
NP \rightarrow NNP
                               {NNP.sem}
S \rightarrow NP VP
                               {NP.sem(VP.sem)}
VP → Verb NP
                               {Verb.sem(NP.sem)}
                               \{\lambda W. \lambda z. W(\exists eBooked(e) \land Booker(e,z) \land BookedThing(e,y))\}
Verb → 'booked'
```

...we'll step through this next time.

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 - Function application
 - Combine elements, don't introduce new ones

Parsing with Semantics

- Implement semantic analysis in parallel with syntactic parsing
 - Enabled by this rule-to-rule compositional approach

Parsing with Semantics

- Implement semantic analysis in parallel with syntactic parsing
 - Enabled by this rule-to-rule compositional approach
- Required modifications
 - Augment grammar rules with semantics field
 - Augment chart states with meaning expression
 - Incrementally compute semantics

Sidenote: Idioms

- Not purely compositional
 - kick the bucket \rightarrow die
 - tip of the iceberg → small part of the entirety
- Handling
 - Mix lexical items with constituents
 - Create idiom-specific construct for productivity
 - Allow non-compositional semantic attachments
- Extremely complex, e.g. metaphor