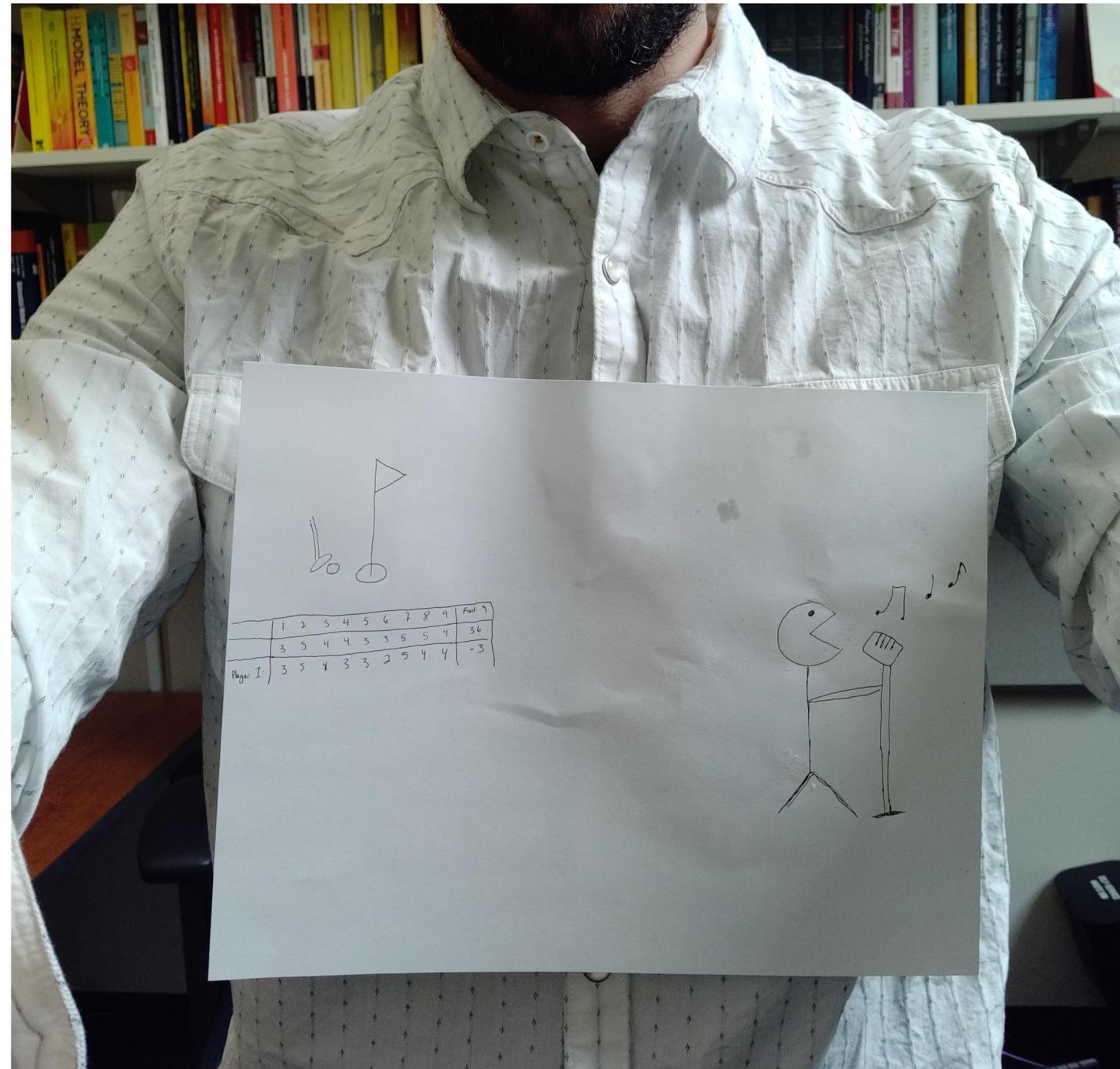


# More $\lambda$ -Calculus Lexical Semantics

LING 571 — Deep Processing Techniques for NLP  
Shane Steinert-Threlkeld

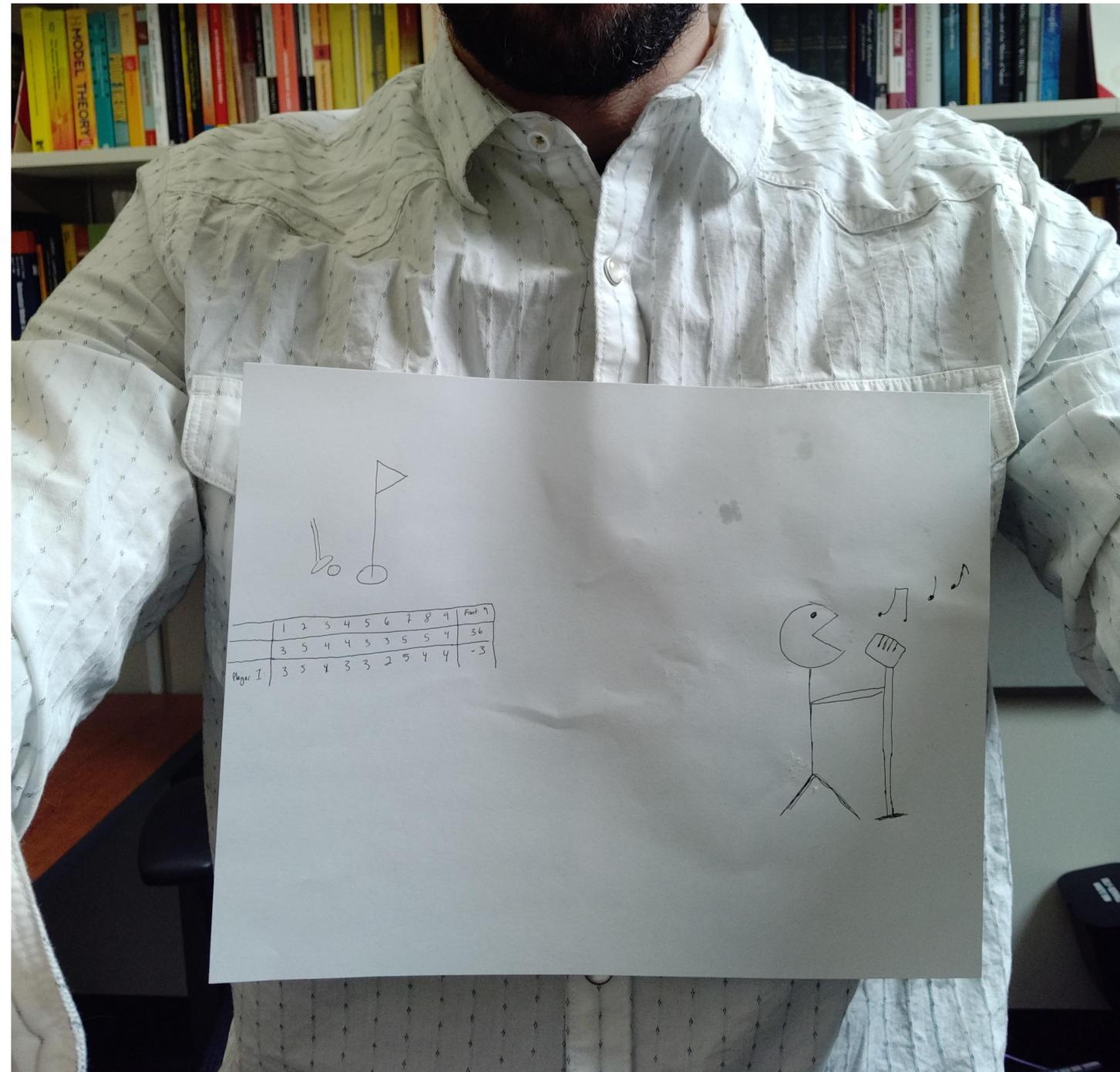
# Happy Halloween!

2021:



# Happy Halloween!

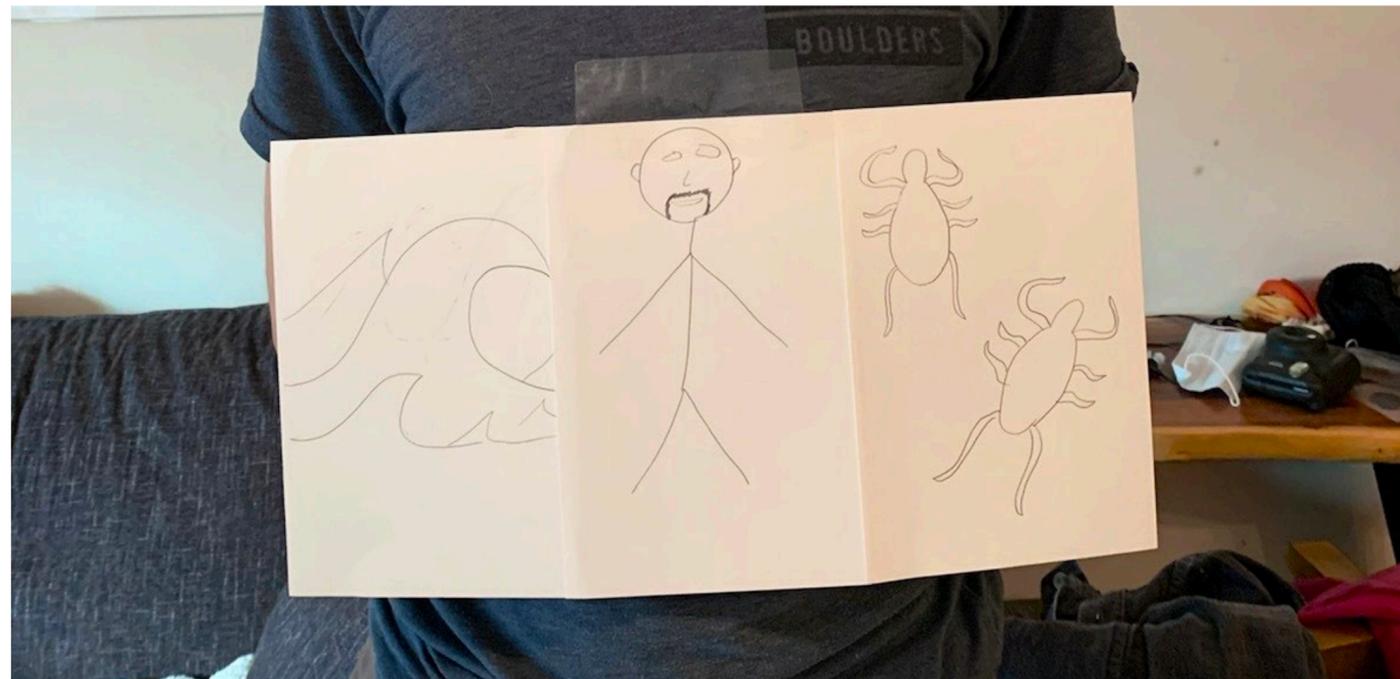
2021:



par + sing = parsing

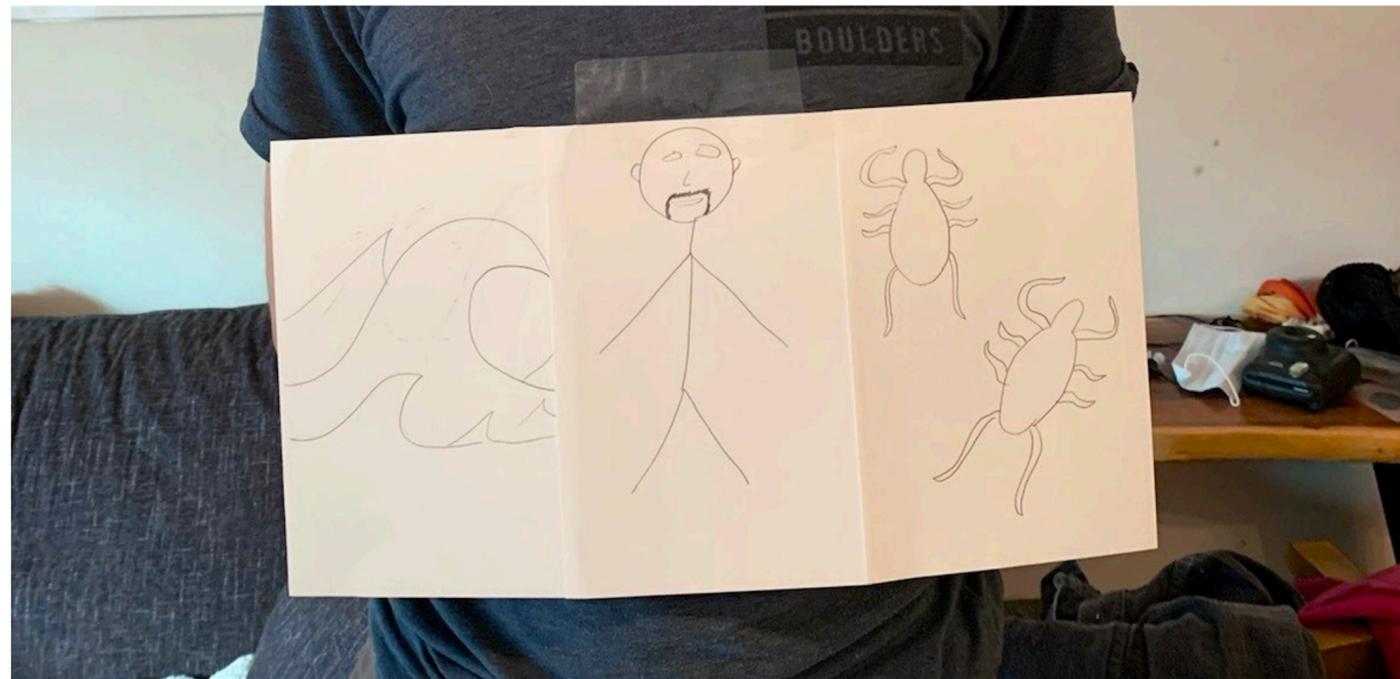
# Happy Halloween!

2020:



# Happy Halloween!

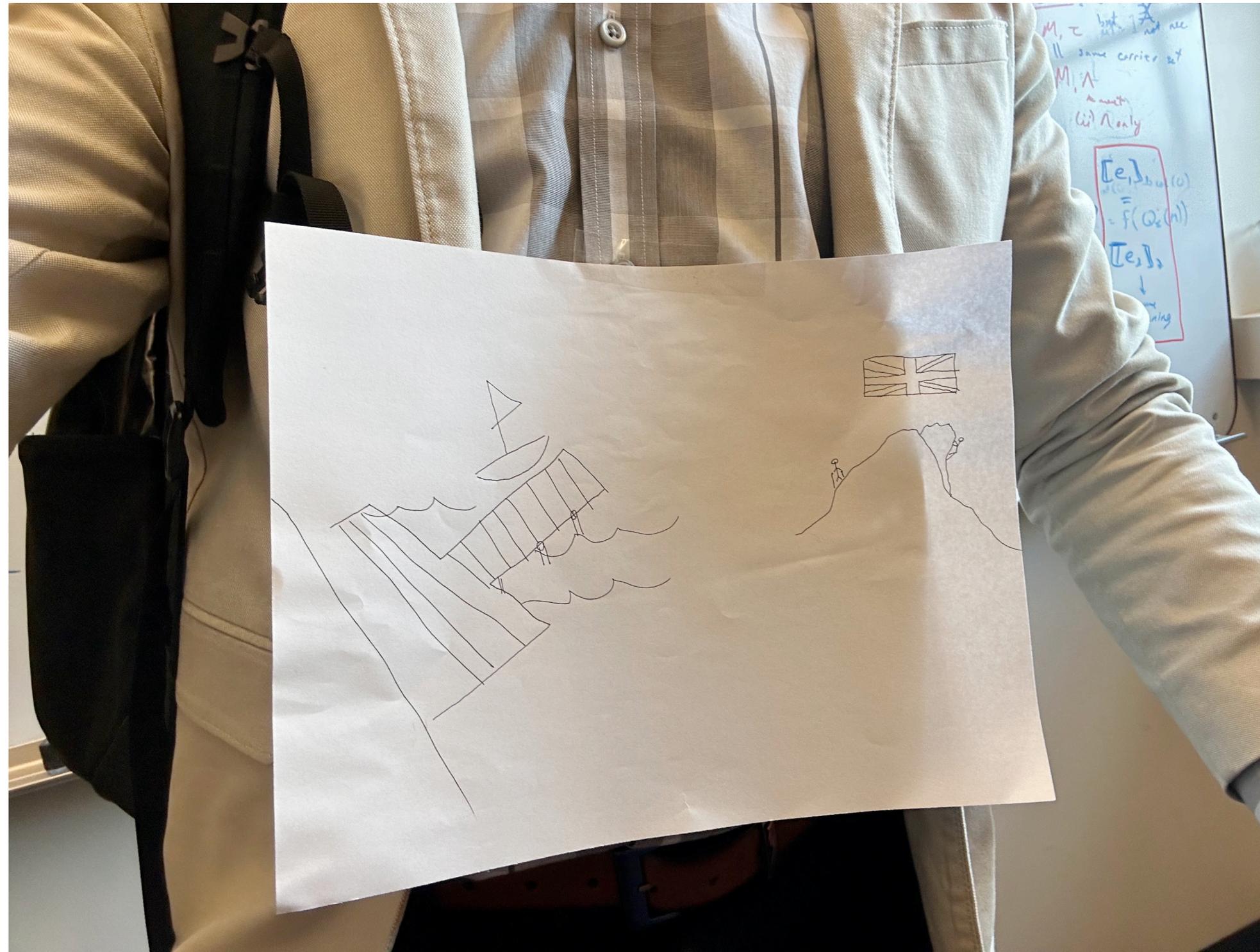
2020:



Sea + Man + Ticks = Semantics

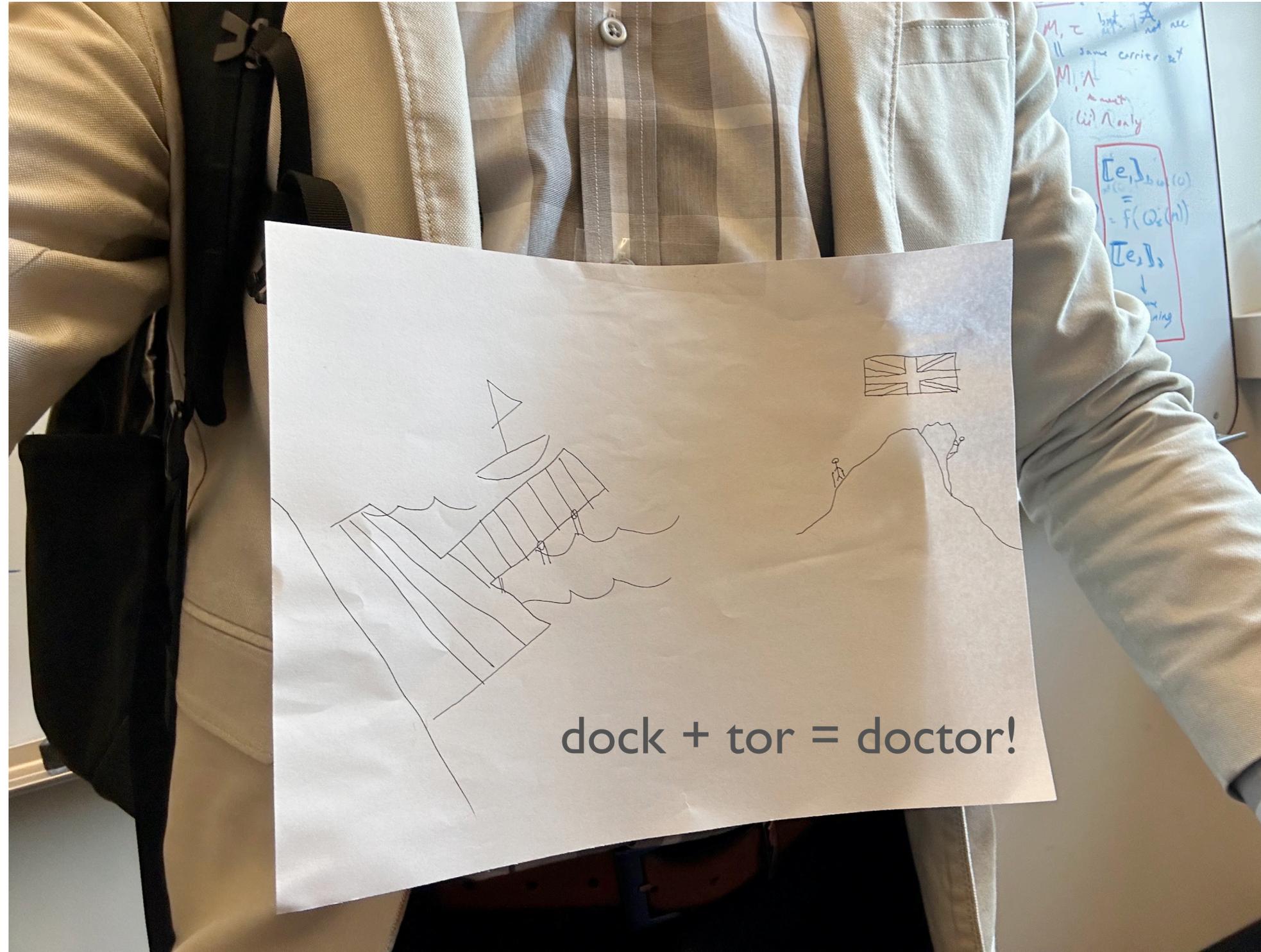
# Happy Halloween!

2023: ???



# Happy Halloween!

2023: ???

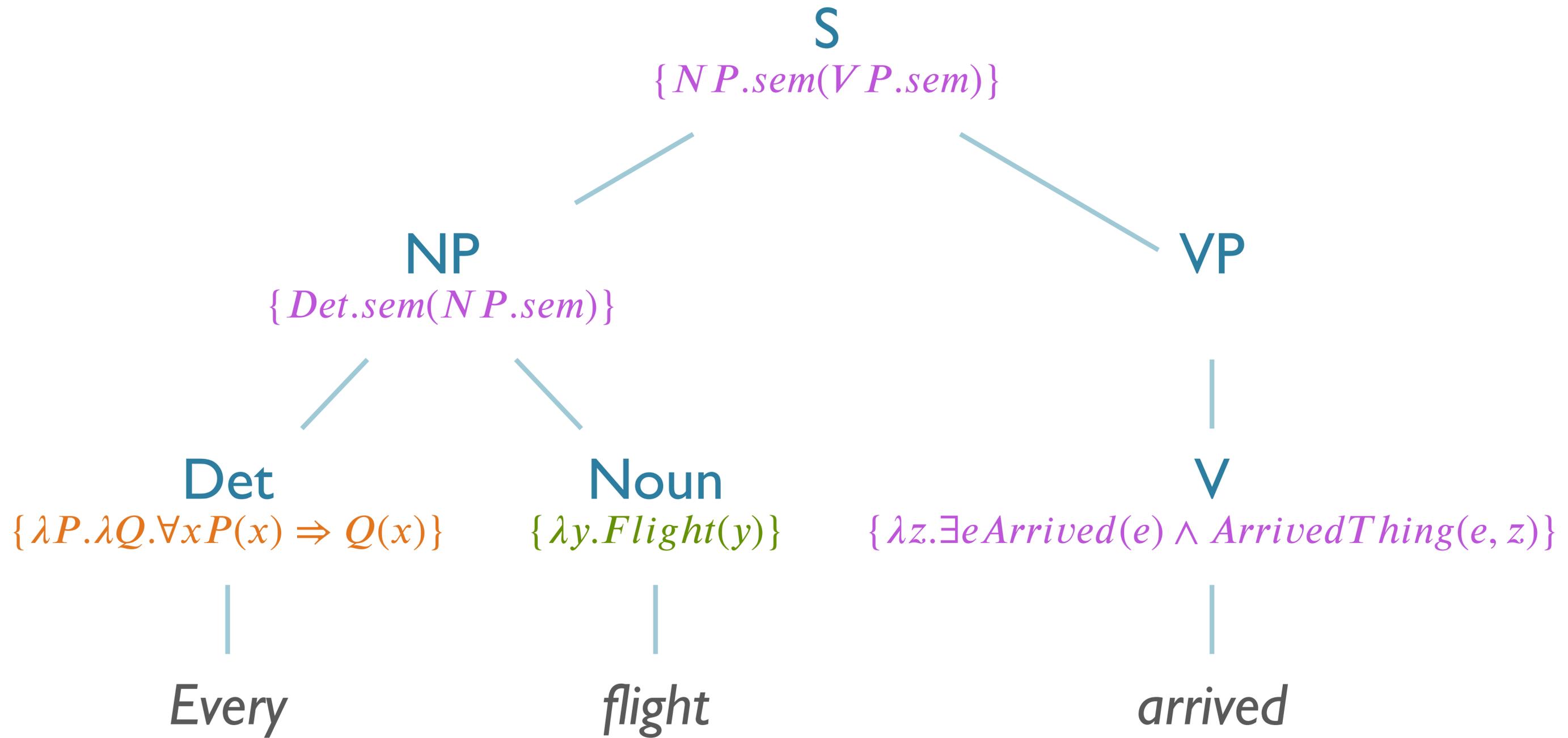


# Roadmap

- FOL Semantics
- More Lambdas
- Learning Semantic Parsers
- Lexical Semantics
  - Motivation & Definitions
  - Word Senses
  - Tasks:
    - Word sense disambiguation
    - Word sense similarity
  - **Distributional Similarity**

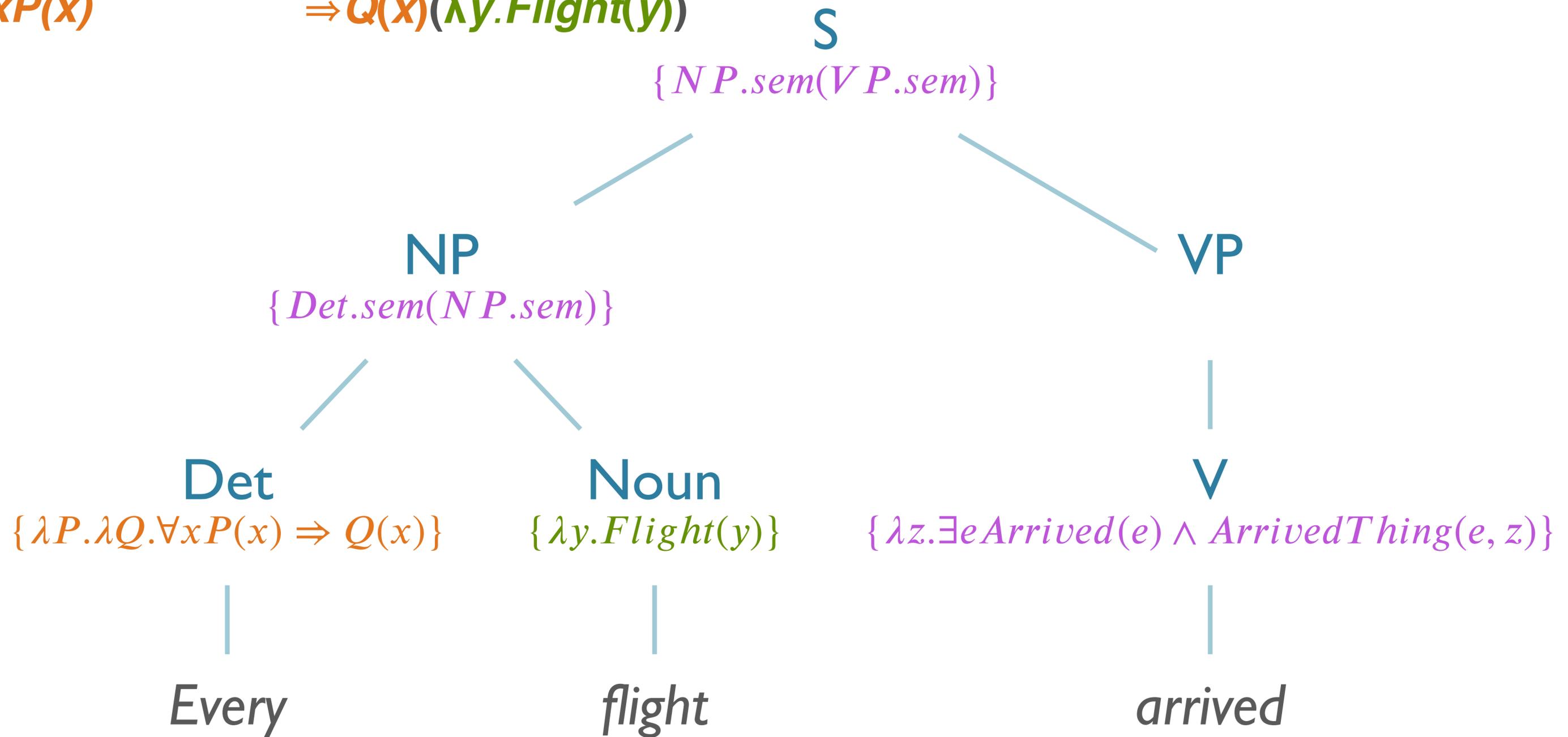
**NP**

→ **Det.sem(NP.sem)**



**NP**  
 $\lambda P.\lambda Q.\forall xP(x)$

$\rightarrow Det.sem(NP.sem)$   
 $\Rightarrow Q(x)(\lambda y.Flight(y))$

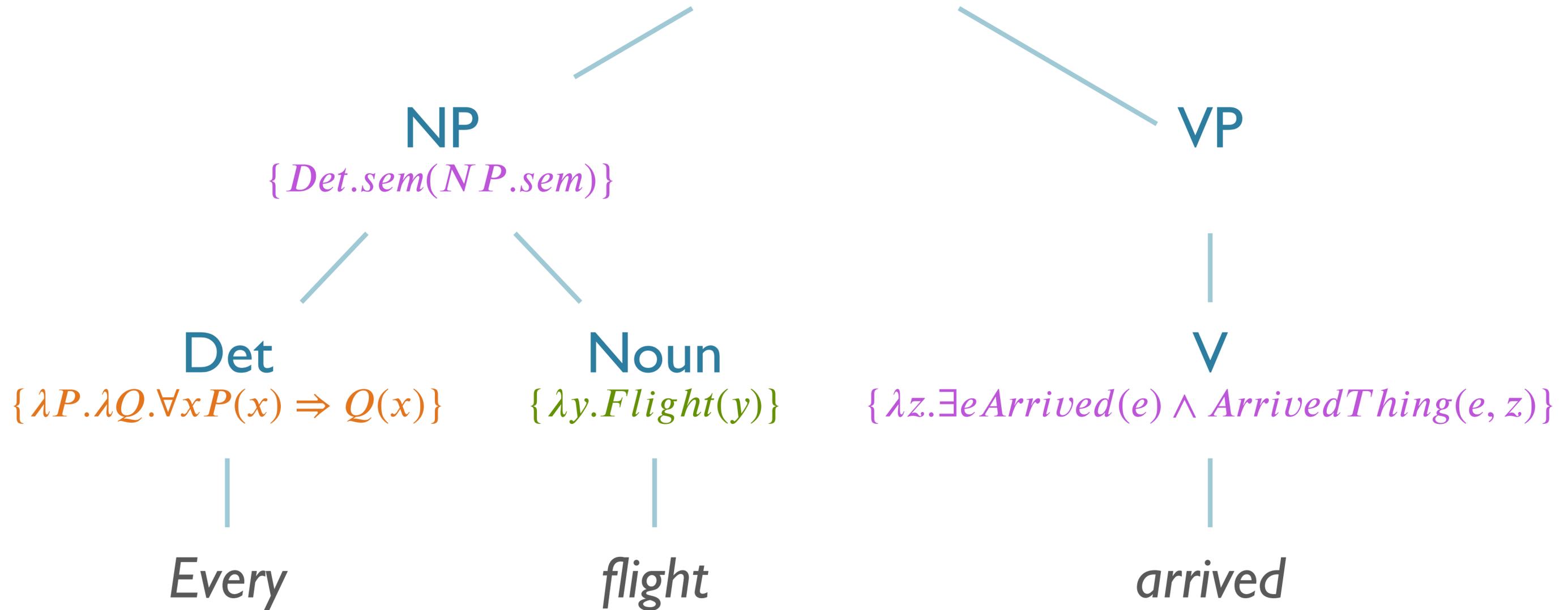


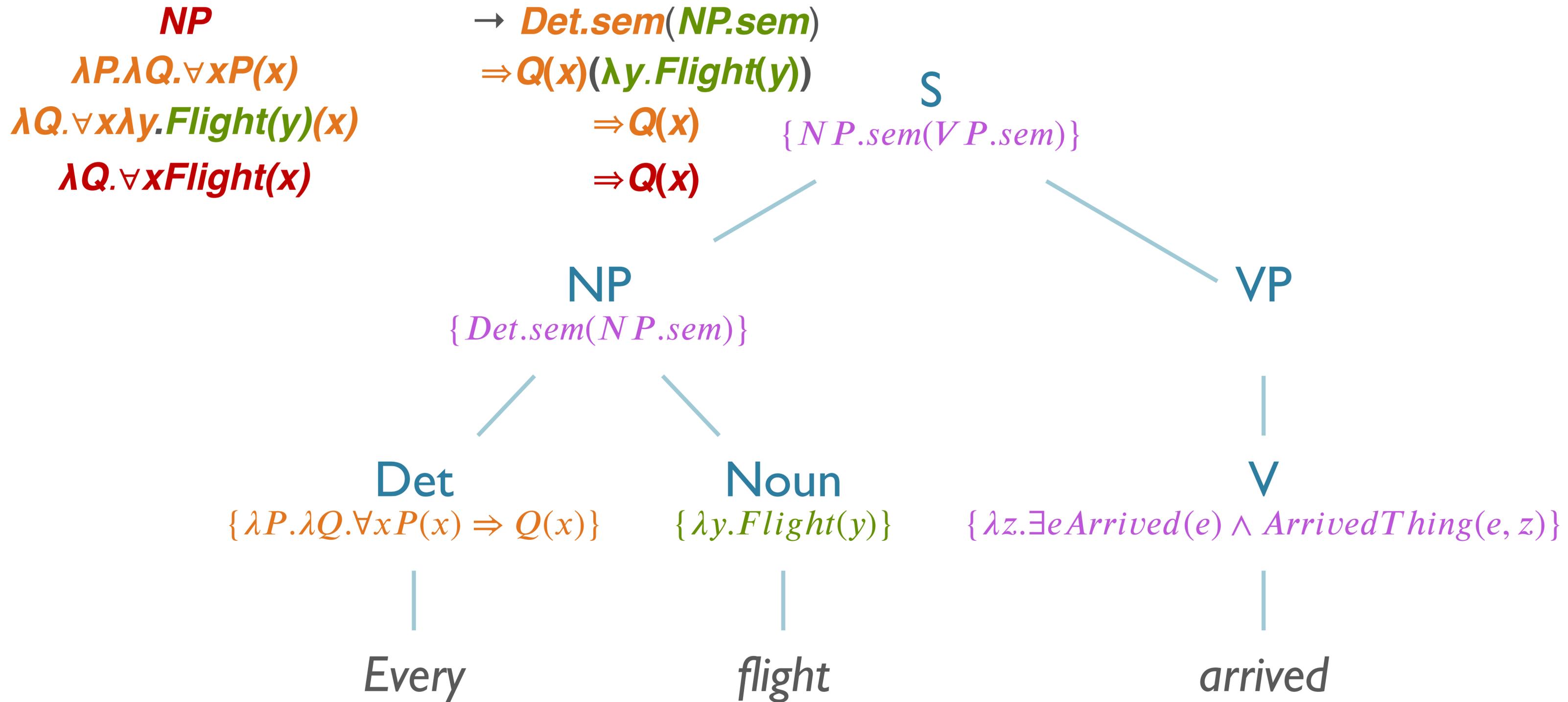
**NP**  
 $\lambda P.\lambda Q.\forall xP(x)$   
 $\lambda Q.\forall x\lambda y.Flight(y)(x)$

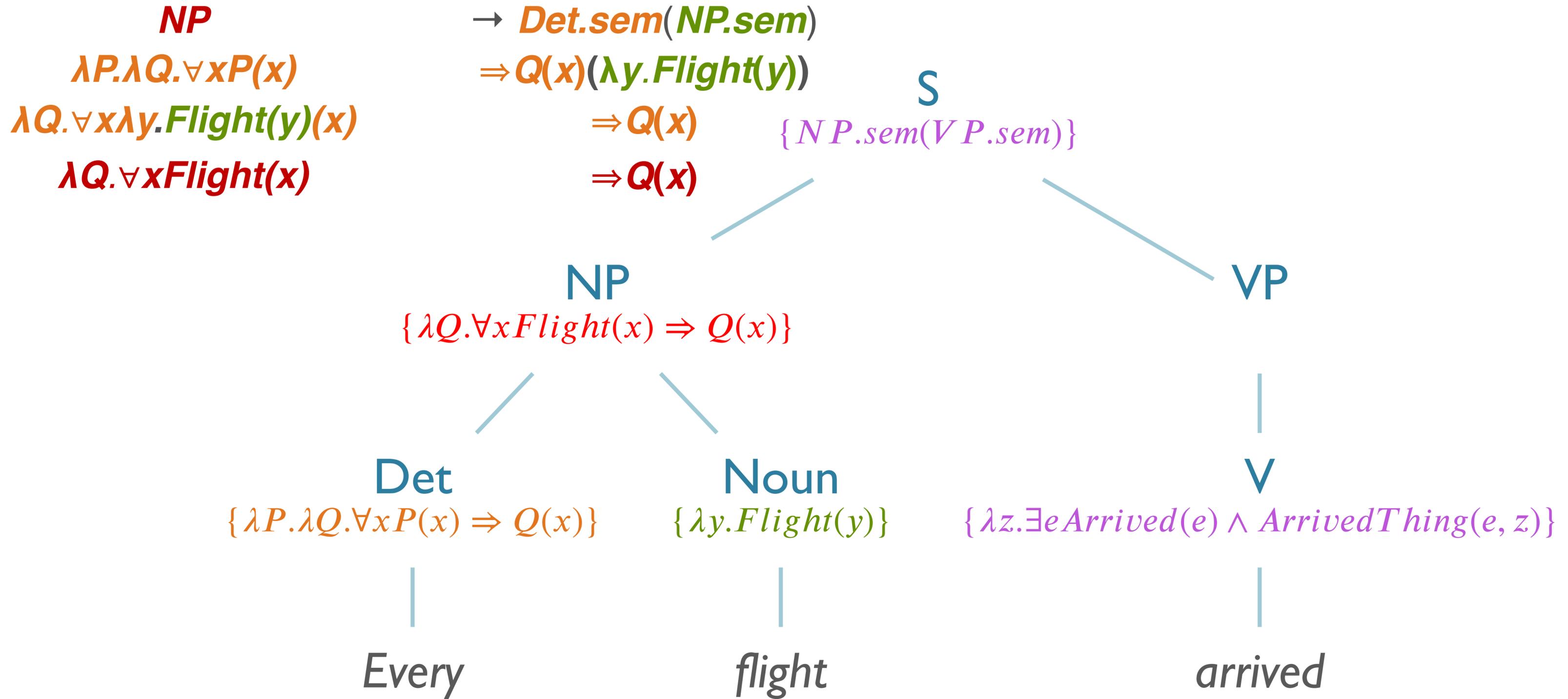
$\rightarrow Det.sem(NP.sem)$   
 $\Rightarrow Q(x)(\lambda y.Flight(y))$   
 $\Rightarrow Q(x)$

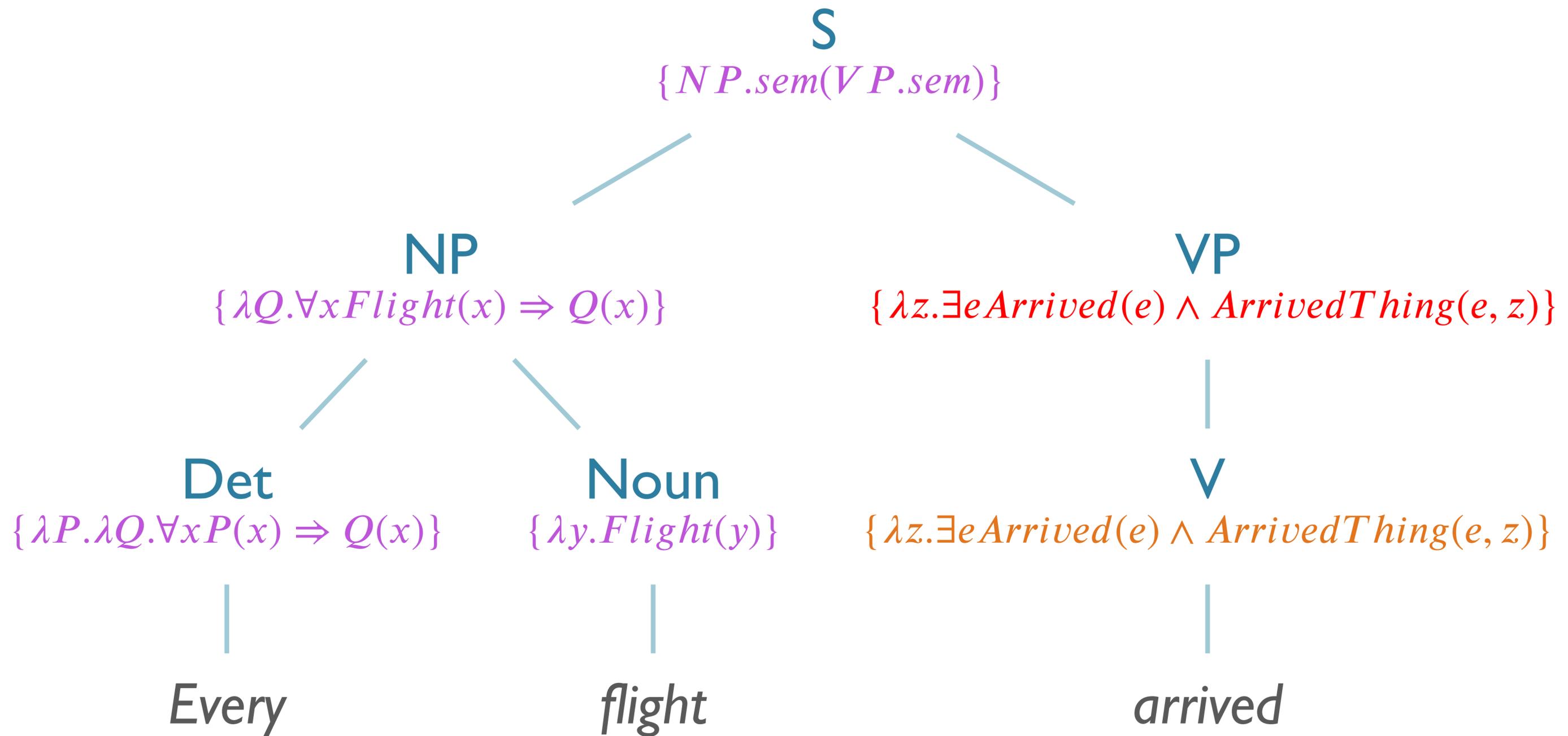
**S**

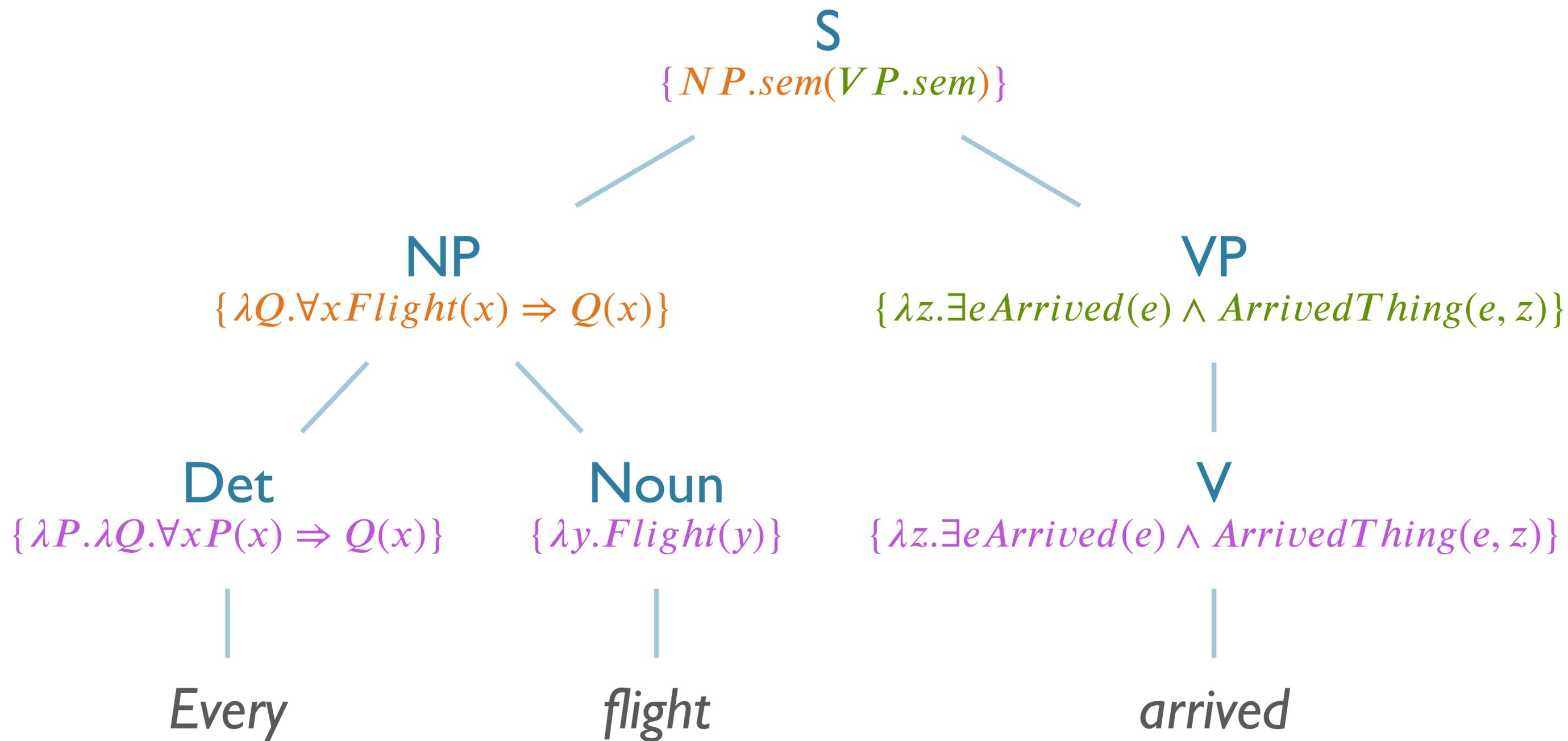
$\{NP.sem(VP.sem)\}$

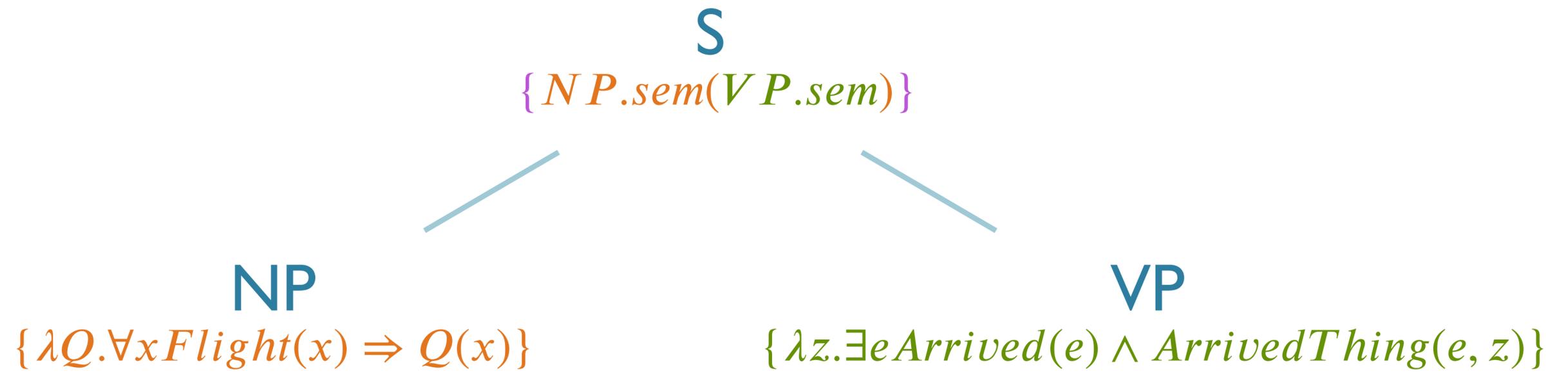


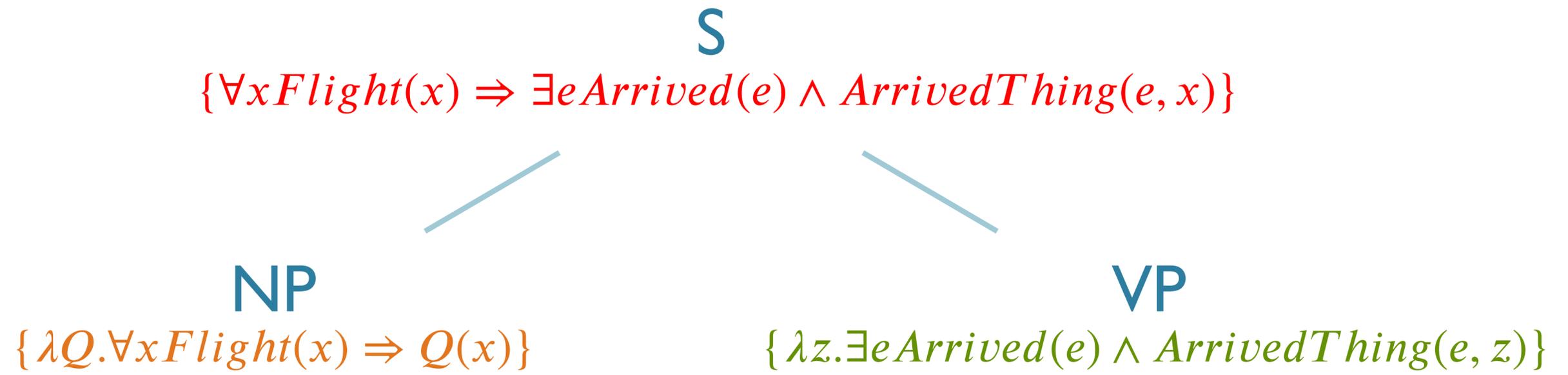


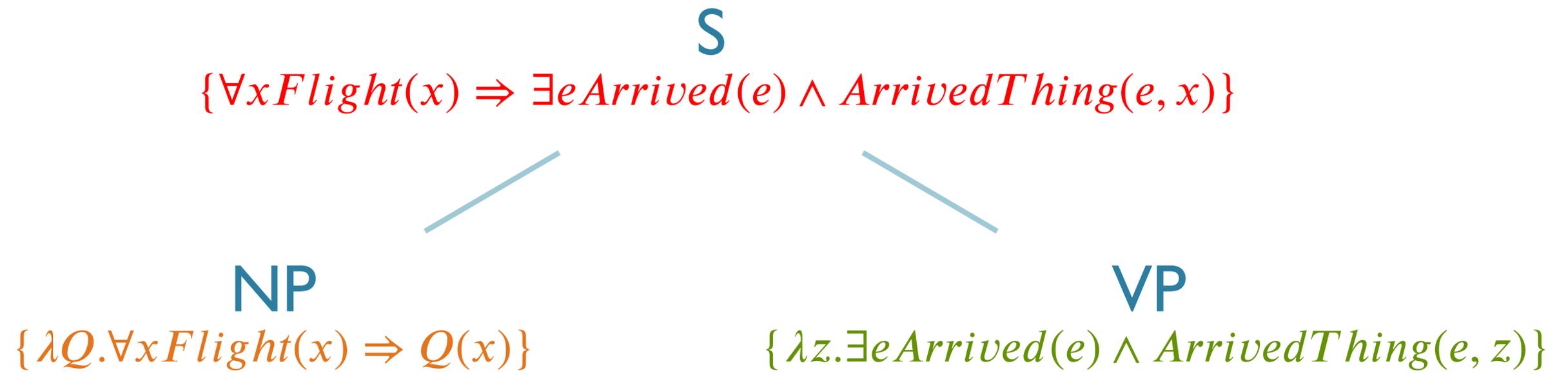




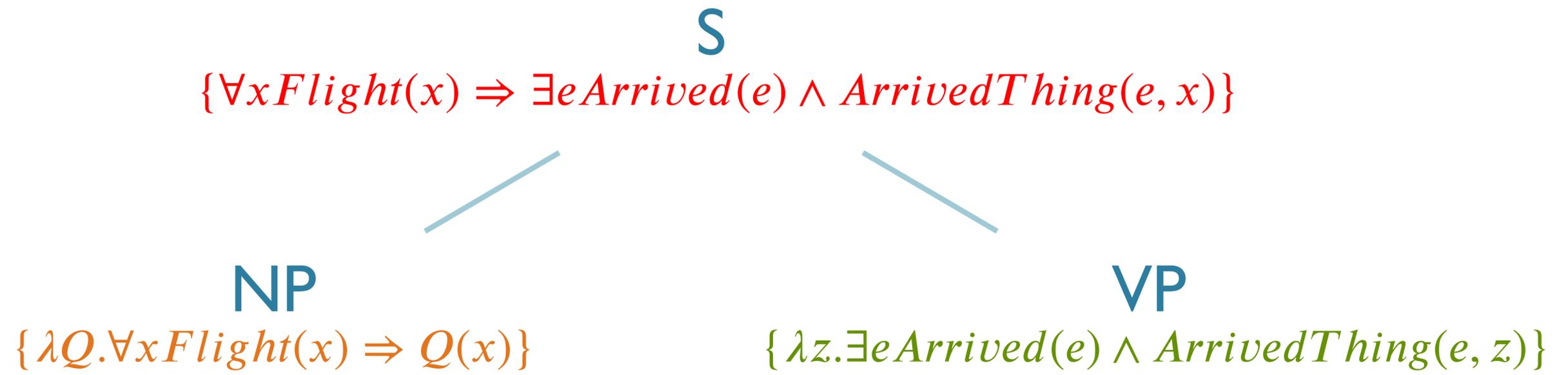






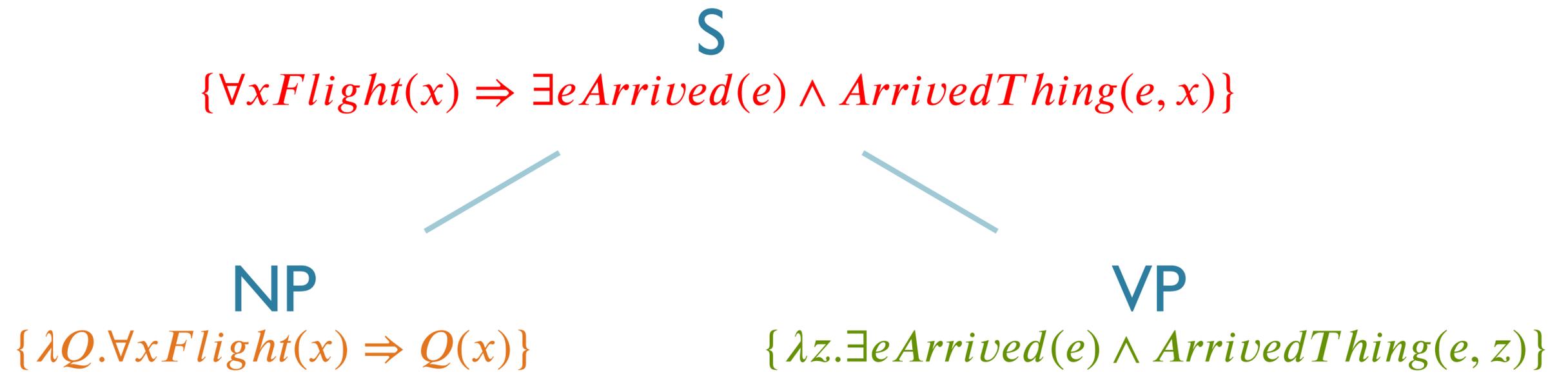


$$\lambda Q. \forall x Flight(x) \Rightarrow Q(x) \quad \Rightarrow \quad Q(x) (\lambda z. \exists e Arrived(e) \wedge ArrivedThing(e, z))$$



$$\lambda Q. \forall x Flight(x) \Rightarrow Q(x) \quad \Rightarrow Q(x) (\lambda z. \exists e Arrived(e) \wedge ArrivedThing(e, z))$$

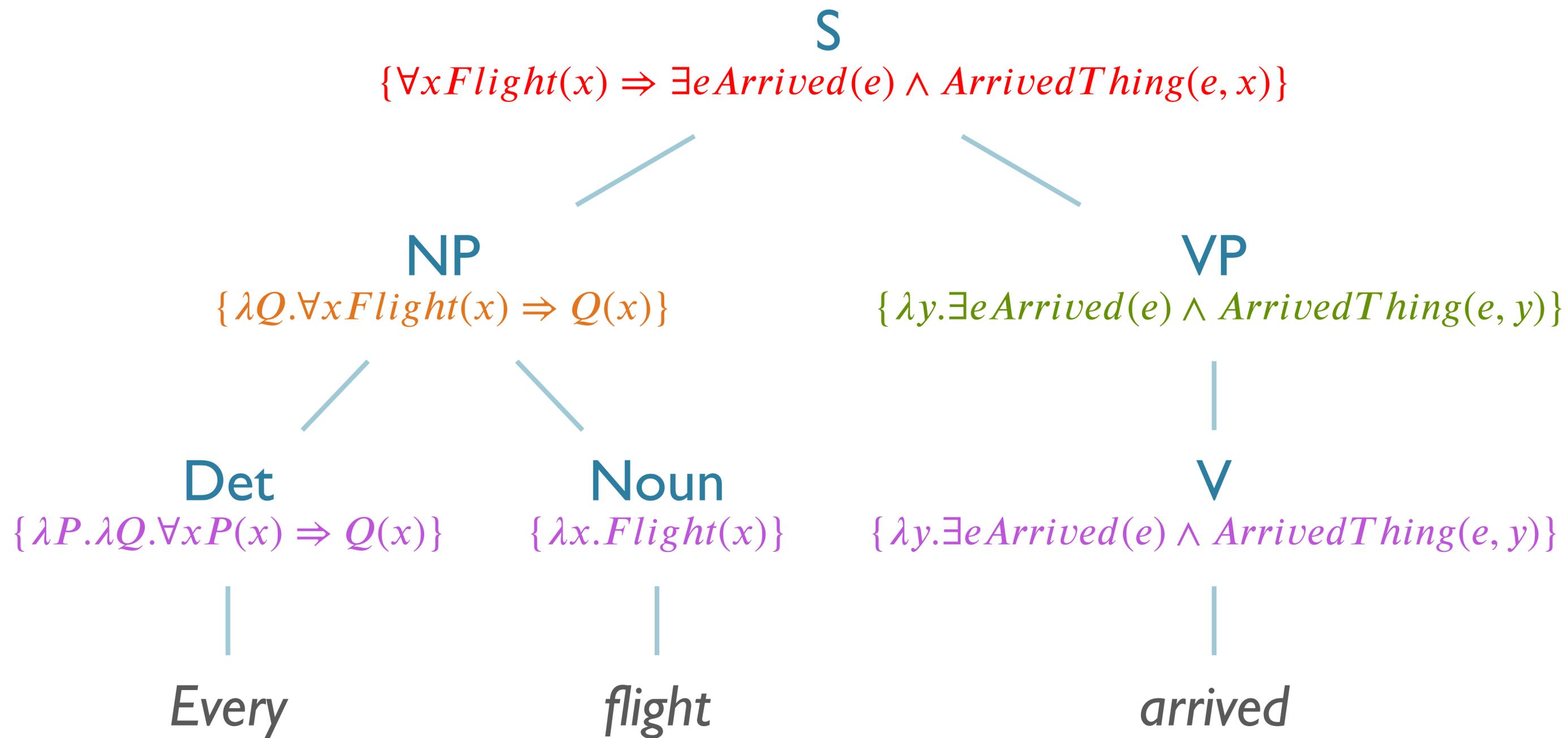
$$\forall x Flight(x) \quad \Rightarrow \lambda z. \exists e Arrived(e) \wedge ArrivedThing(e, z)(x)$$



$$\lambda Q. \forall x Flight(x) \Rightarrow Q(x) (\lambda z. \exists e Arrived(e) \wedge ArrivedThing(e, z))$$

$$\forall x Flight(x) \Rightarrow \lambda z. \exists e Arrived(e) \wedge ArrivedThing(e, z)(x)$$

$$\forall x Flight(x) \Rightarrow \exists e Arrived(e) \wedge ArrivedThing(e, x)$$



# More $\lambda$ -Calculus

# Common Nouns

- Noun -> 'restaurant'  $\{\lambda x. \mathit{Restaurant}(x)\}$
- Somewhat similar to the NNP construction
  - $\lambda var. \mathit{Predicate}(var)$

# Common Nouns

- Noun -> 'restaurant'  $\{\lambda x. \mathbf{Restaurant}(x)\}$ 
  - Somewhat similar to the NNP construction
    - $\lambda var. Predicate(var)$
- But common nouns represent *properties*, rather than *constants*
  - Meaning of the noun encoded in the predicate
  - Relate the concept of the noun to a particular instance of variable

# Negation

- “No vegetarian restaurant serves meat.”
  - $\neg(\exists x \textit{VegetarianRestaurant}(x) \wedge \textit{Serves}(x, \textit{Meat}))$

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  - $\forall x \textit{VegetarianRestaurant}(x) \Rightarrow \neg \textit{Serves}(x, \textit{Meat})$

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- “All vegetarian restaurants do not serve meat.”
  - $\forall x \text{VegetarianRestaurant}(x) \Rightarrow \neg \text{Serves}(x, \text{Meat})$
- *These are semantically equivalent!*
  - [IF P, THEN  $\neg$ Q]  $\Leftrightarrow$   $\neg$ [P AND Q]
  - $\neg\exists xP(x) \Leftrightarrow \forall x\neg P(x)$

# Negation

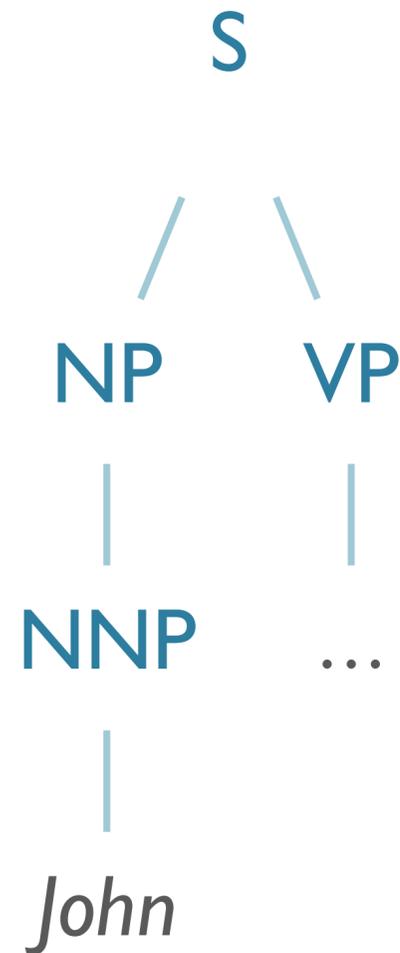
- “No vegetarian restaurant serves meat.”
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- *These are semantically equivalent!*
  - [IF P, THEN  $\neg$ Q]  $\Leftrightarrow$   $\neg$ [P AND Q]
  - $\neg\exists xP(x) \Leftrightarrow \forall x\neg P(x)$
- For NLTK, use the hyphen/minus character: ‘ - ’

# 'John booked a flight'

- Target representation:
  - $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$

# ‘John booked a flight’

- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$

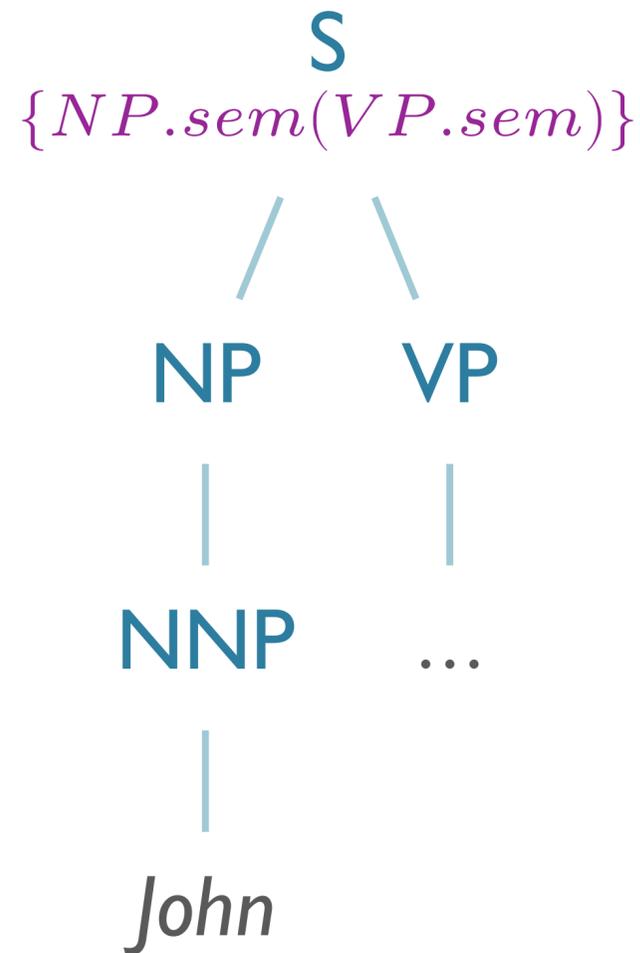


$S \rightarrow NP VP$

$\{NP.sem(VP.sem)\}$

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- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$

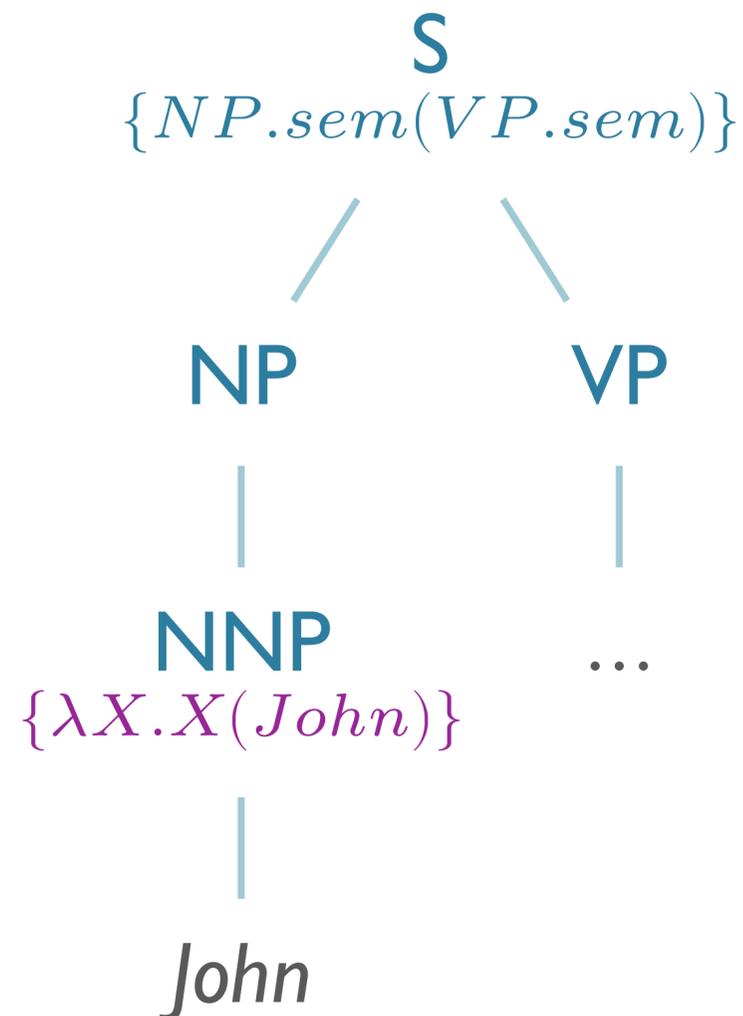


$S \rightarrow NP VP$

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$S \rightarrow NP VP$

$\{NP.sem(VP.sem)\}$

$NNP \rightarrow \textit{John}$

$\{\lambda X.X(\textit{John})\}$

$NP \rightarrow NNP$

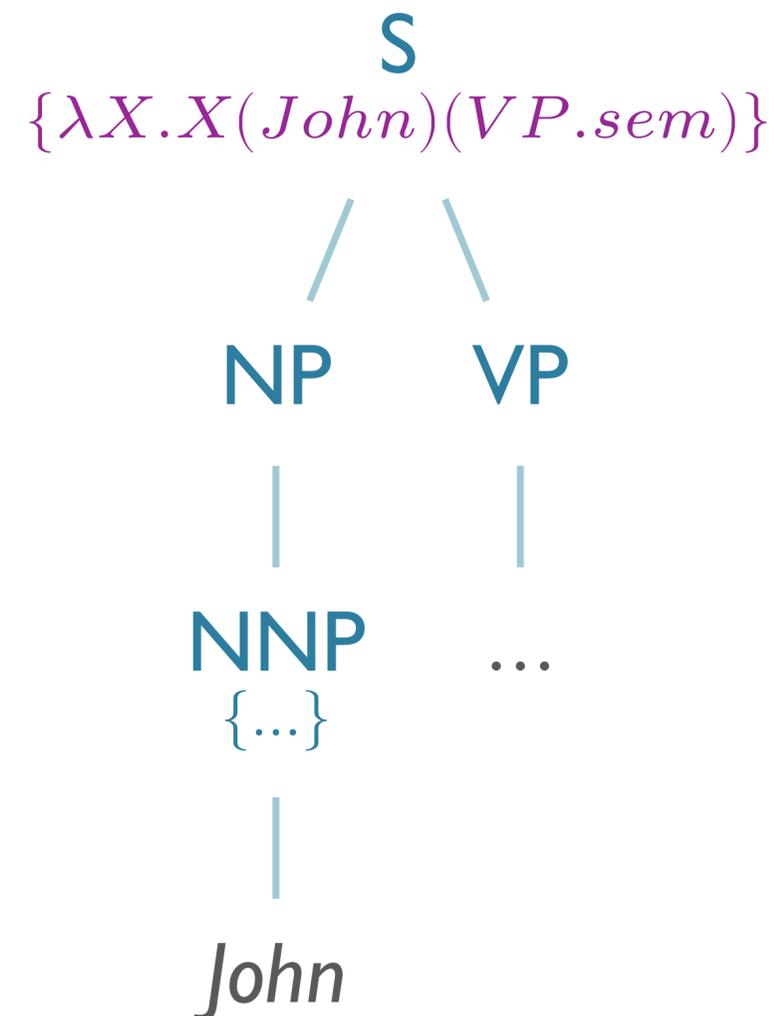
$\{NNP.sem\}$

$VP \rightarrow \textit{Verb NP}$

$\{\textit{Verb.sem}(NP.sem)\}$

# ‘John booked a flight’

- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$



$S \rightarrow NP VP$

{ $NP.sem(VP.sem)$ }

$NNP \rightarrow \textit{‘John’}$

{ $\lambda X.X(\textit{John})$ }

$NP \rightarrow NNP$

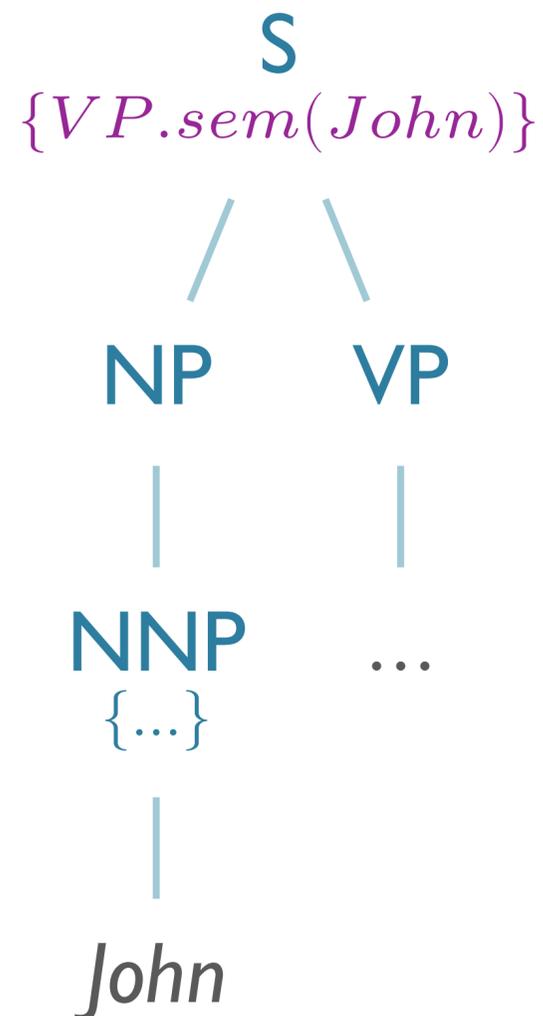
{ $NNP.sem$ }

$VP \rightarrow \textit{Verb NP}$

{ $\textit{Verb.sem}(NP.sem)$ }

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$S \rightarrow NP VP$

$\{NP.sem(VP.sem)\}$

$NNP \rightarrow \textit{John}$

$\{\lambda X.X(\textit{John})\}$

$NP \rightarrow NNP$

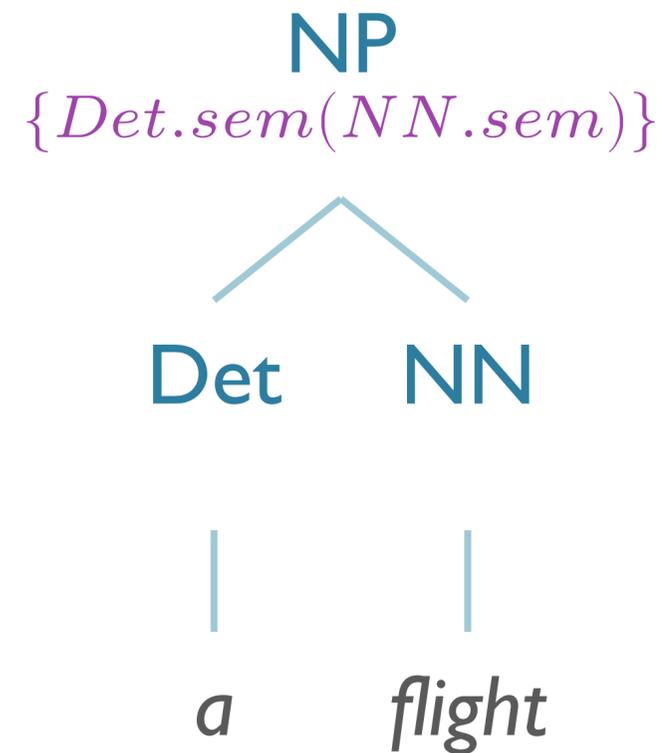
$\{NNP.sem\}$

$VP \rightarrow \textit{Verb NP}$

$\{\textit{Verb.sem}(NP.sem)\}$

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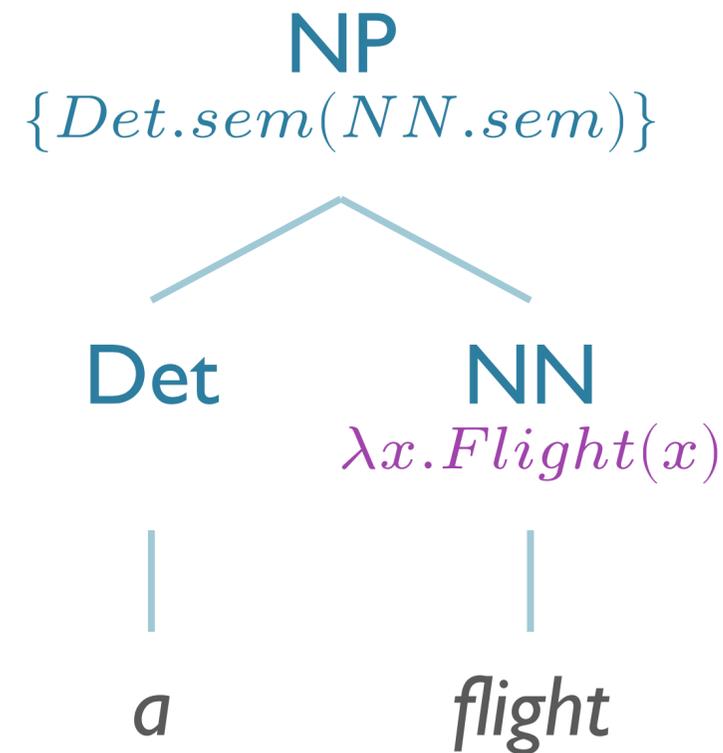


$NP \rightarrow Det\ NN$

$\{Det.sem(NN.sem)\}$

# 'John booked a flight'

- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$



$NP \rightarrow Det \ NN$

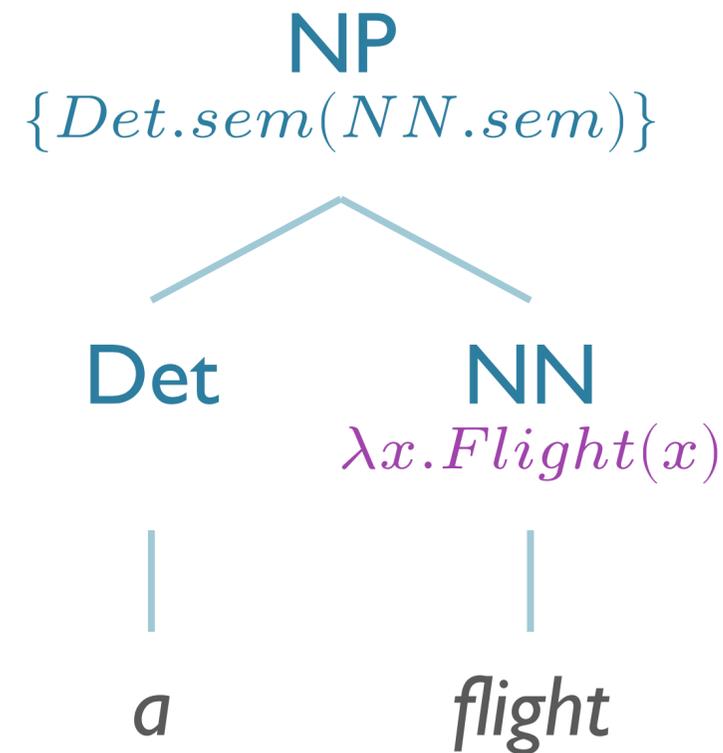
$\{Det.sem(NN.sem)\}$

$NN \rightarrow 'flight'$

$\{\lambda x.Flight(x)\}$

# ‘John booked a flight’

- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$



$\textit{NP} \rightarrow \textit{Det} \textit{NN}$

$\textit{NN} \rightarrow \textit{'flight'}$

$\textit{Det} \rightarrow \textit{'a'}$

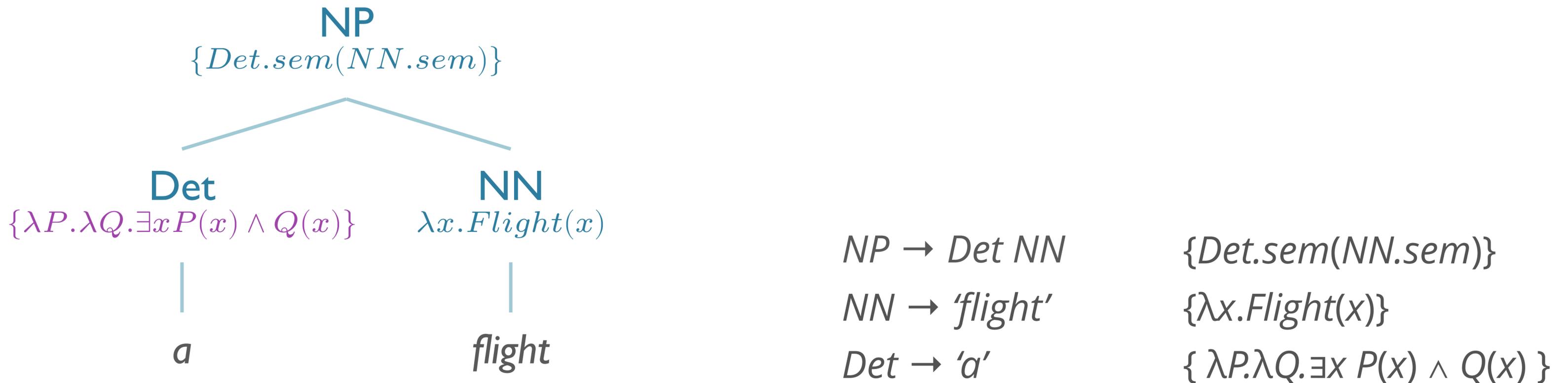
$\{ \textit{Det.sem}(\textit{NN.sem}) \}$

$\{ \lambda x. \textit{Flight}(x) \}$

$\{ \lambda P. \lambda Q. \exists x P(x) \wedge Q(x) \}$

# 'John booked a flight'

- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$



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NP  
{*Det.sem(NN.sem)*}

*NP* → *Det NN*

{*Det.sem(NN.sem)*}

*NN* → 'flight'

{ $\lambda x. \textit{Flight}(x)$ }

*Det* → 'a'

{ $\lambda P. \lambda Q. \exists x P(x) \wedge Q(x)$ }

# ‘John booked a flight’

- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$

NP

$\{ \textit{Det.sem}(\textit{NN.sem}) \}$

$\{ \lambda P. \lambda Q. \exists x P(x) \wedge Q(x) (\lambda x. \textit{Flight}(x)) \}$

$NP \rightarrow \textit{Det NN}$

$NN \rightarrow \textit{'flight'}$

$\textit{Det} \rightarrow \textit{'a'}$

$\{ \textit{Det.sem}(\textit{NN.sem}) \}$

$\{ \lambda x. \textit{Flight}(x) \}$

$\{ \lambda P. \lambda Q. \exists x P(x) \wedge Q(x) \}$

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NP

$\{ \textit{Det.sem}(\textit{NN.sem}) \}$

$\{ \lambda P. \lambda Q. \exists x P(x) \wedge Q(x) (\lambda x. \textit{Flight}(x)) \}$

$\{ \lambda Q. \exists x (\lambda x. \textit{Flight}(x))(x) \wedge Q(x) \}$

$NP \rightarrow \textit{Det NN}$

$NN \rightarrow \textit{'flight'}$

$\textit{Det} \rightarrow \textit{'a'}$

$\{ \textit{Det.sem}(\textit{NN.sem}) \}$

$\{ \lambda x. \textit{Flight}(x) \}$

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NP

$\{ \textit{Det.sem}(\textit{NN.sem}) \}$

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$\{ \lambda Q. \exists x (\lambda x. \textit{Flight}(x))(x) \wedge Q(x) \}$

$\{ \lambda Q. \exists x \textit{Flight}(x) \wedge Q(x) \}$

$NP \rightarrow \textit{Det NN}$

$NN \rightarrow \textit{'flight'}$

$\textit{Det} \rightarrow \textit{'a'}$

$\{ \textit{Det.sem}(\textit{NN.sem}) \}$

$\{ \lambda x. \textit{Flight}(x) \}$

$\{ \lambda P. \lambda Q. \exists x P(x) \wedge Q(x) \}$

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NP

$\{ \textit{Det.sem}(\textit{NN.sem}) \}$

$\{ \lambda P. \lambda Q. \exists x P(x) \wedge Q(x) (\lambda x. \textit{Flight}(x)) \}$

$\{ \lambda Q. \exists x (\lambda x. \textit{Flight}(x))(x) \wedge Q(x) \}$

$\{ \lambda Q. \exists x \textit{Flight}(x) \wedge Q(x) \}$

$NP \rightarrow \textit{Det NN}$

$NN \rightarrow \textit{'flight'}$

$\textit{Det} \rightarrow \textit{'a'}$

$\textit{'a flight'}$

$\{ \textit{Det.sem}(\textit{NN.sem}) \}$

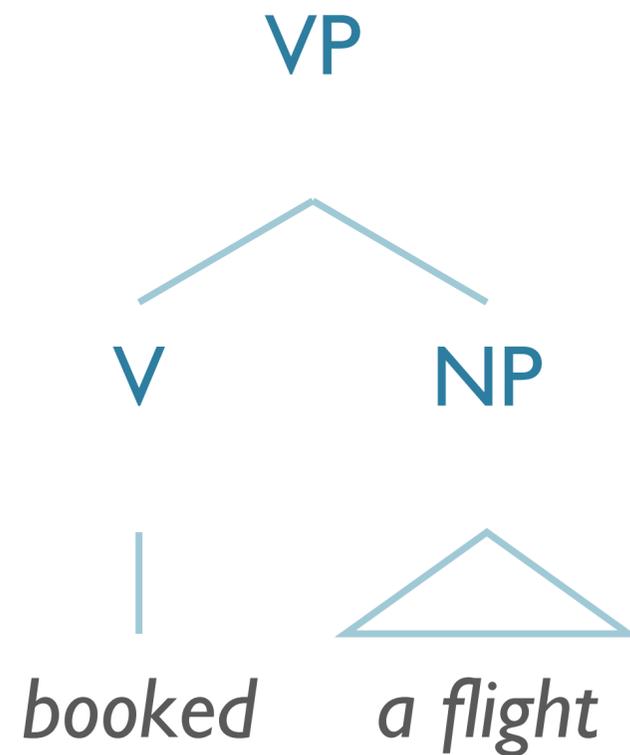
$\{ \lambda x. \textit{Flight}(x) \}$

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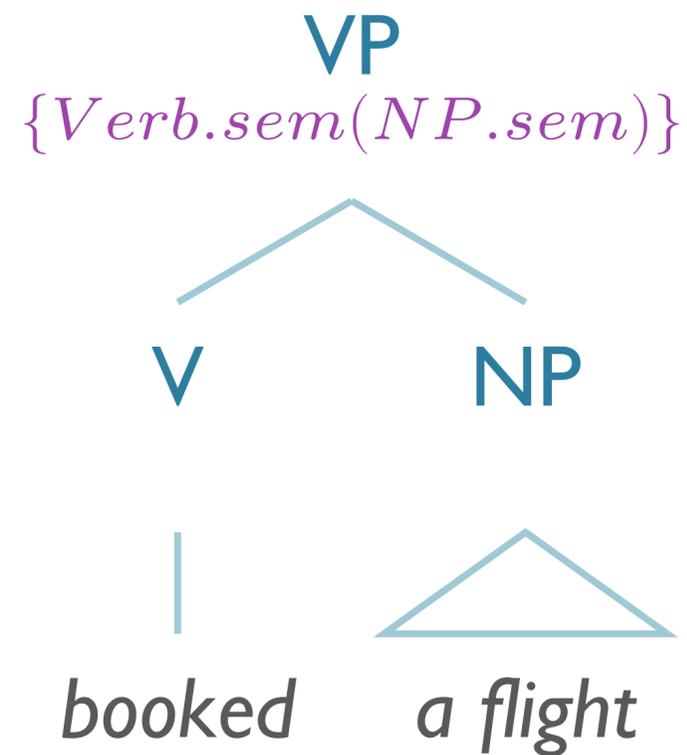


$VP \rightarrow \textit{Verb NP}$   
'a flight'

$\{\textit{Verb.sem}(\textit{NP.sem})\}$   
 $\{\lambda Q. \exists x \textit{Flight}(x) \wedge Q(x)\}$

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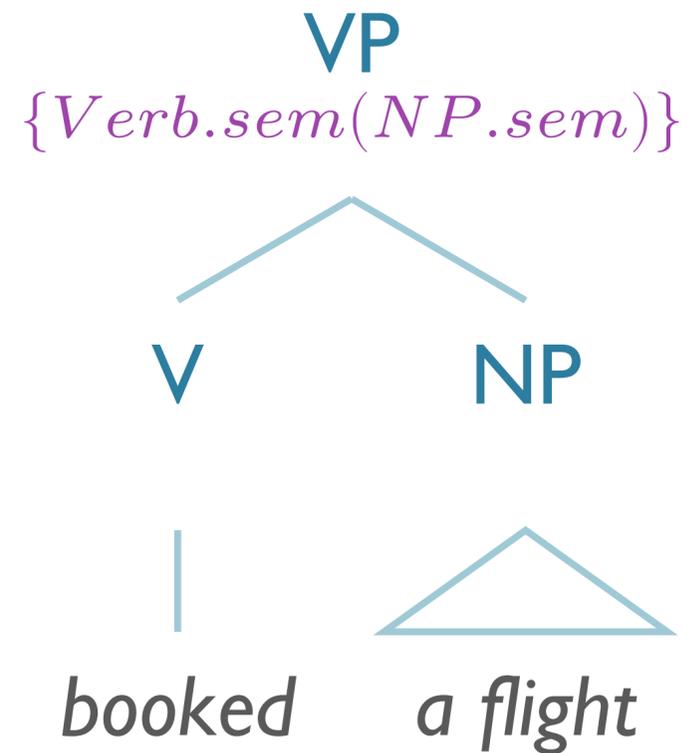


$VP \rightarrow \textit{Verb NP}$   
'a flight'

{*Verb.sem(NP.sem)*}  
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Verb  $\rightarrow$  'booked'

$\{\lambda W.\lambda z.W(\lambda y.\exists e \textit{Booked}(e) \wedge \textit{Booker}(e,z) \wedge \textit{BookedThing}(e,y))\}$

VP  $\rightarrow$  Verb NP

$\{\textit{Verb.sem}(\textit{NP.sem})\}$

'a flight'

$\{\lambda Q.\exists x \textit{Flight}(x) \wedge Q(x)\}$

# 'John booked a flight'

- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$

*Verb.sem(NP.sem)*

# ‘John booked a flight’

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*Verb.sem(NP.sem)*

$\lambda W. \lambda z. W(\lambda y. \exists e \textit{Booked}(e) \wedge \textit{Booker}(e, z) \wedge \textit{BookedThing}(e, y)) (\lambda Q. \exists x \textit{Flight}(x) \wedge Q(x))$

# ‘John booked a flight’

- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$

*Verb.sem(NP.sem)*

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*Verb.sem(NP.sem)*

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$\lambda z. (\lambda Q. \exists x \textit{Flight}(x) \wedge Q(x)) (\lambda y. \exists e \textit{Booked}(e) \wedge \textit{Booker}(e, z) \wedge \textit{BookedThing}(e, y))$

$\lambda z. \exists x \textit{Flight}(x) \wedge (\lambda y. \exists e \textit{Booked}(e) \wedge \textit{Booker}(e, z) \wedge \textit{BookedThing}(e, y))(x)$

# ‘John booked a flight’

- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$

*Verb.sem(NP.sem)*

$\lambda W. \lambda z. W(\lambda y. \exists e \textit{Booked}(e) \wedge \textit{Booker}(e, z) \wedge \textit{BookedThing}(e, y)) (\lambda Q. \exists x \textit{Flight}(x) \wedge Q(x))$

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*Verb.sem(NP.sem)*

$\lambda W. \lambda z. W(\lambda y. \exists e \textit{Booked}(e) \wedge \textit{Booker}(e, z) \wedge \textit{BookedThing}(e, y)) (\lambda Q. \exists x \textit{Flight}(x) \wedge Q(x))$

$\lambda z. (\lambda Q. \exists x \textit{Flight}(x) \wedge Q(x)) (\lambda y. \exists e \textit{Booked}(e) \wedge \textit{Booker}(e, z) \wedge \textit{BookedThing}(e, y))$

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# 'John booked a flight'

- $\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$

S  
{*VP.sem(John)*}

NP

NNP  
{...}

John

VP

...

S

'booked a flight'

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# 'John booked a flight'

<i>Det</i> → 'a'	$\{ \lambda P. \lambda Q. \exists x P(x) \wedge Q(x) \}$
<i>Det</i> → 'every'	$\{ \lambda P. \lambda Q. \forall x P(x) \Rightarrow Q(x) \}$
<i>NN</i> → 'flight'	$\{ \lambda x. Flight(x) \}$
<i>Verb</i> → 'booked'	$\{ \lambda W. \lambda z. W(\lambda y. \exists e Booked(e) \wedge Booker(e, z) \wedge BookedThing(e, y)) \}$
<i>NNP</i> → 'John'	$\{ \lambda X. X(John) \}$
<i>NP</i> → <i>NNP</i>	$\{ NNP.sem \}$
<i>NP</i> → <i>Det NN</i>	$\{ Det.sem(NN.sem) \}$
<i>S</i> → <i>NP VP</i>	$\{ NP.sem(VP.sem) \}$
<i>VP</i> → <i>Verb NP</i>	$\{ Verb.sem(NP.sem) \}$

# 'John booked no flight'

- $\neg(\exists x \textit{Flight}(x) \wedge (\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x)))$
- $\forall x \textit{Flight}(x) \Rightarrow \neg(\exists e \textit{Booked}(e) \wedge \textit{Booker}(e, \textit{John}) \wedge \textit{BookedThing}(e, x))$

# 'John booked no flight'

<i>Det</i> → 'no'	$\{ \lambda P. \lambda Q. \neg \exists x P(x) \wedge Q(x) \}$
<i>Det</i> → 'a'	$\{ \lambda P. \lambda Q. \exists x P(x) \wedge Q(x) \}$
<i>Det</i> → 'every'	$\{ \lambda P. \lambda Q. \forall x P(x) \Rightarrow Q(x) \}$
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# *Other Lambda Calculus*

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  - “red” =  $\lambda P \lambda x(\text{red}(x) \wedge P(x))$
- Any issues?
  - Non-intersective adjectives (e.g. ‘skillful’, ‘alleged’, ‘fake’)

# Definite Article

- $a = \lambda P.\lambda Q.\exists x(P(x) \wedge Q(x))$
- $the = \lambda P.\lambda Q.\exists x(P(x) \wedge \forall y(P(y) \Leftrightarrow x=y) \wedge Q(x))$
- Roughly: “The P Q”: there is a *unique* P, which is also Q
  - Unique:  $x$  is P, and anything else that is also P is equal to  $x$

# Definite Article

- $the = \lambda P.\lambda Q.\exists x(P(x) \wedge \forall y(P(y) \Leftrightarrow x=y) \wedge Q(x))$
- Bertrand Russell, "[On Denoting](#)" (1905).
- The definite article isn't exactly the same as a constant (like "John")
- Rather, it picks out a set of items from a set (the generic NN), and makes a strong assertion:
  - A) The book arrived.
  - B) A book arrived.
  - $A \models B$ , but  $B \not\models A$

# Definite Article + Presupposition

- “The slides for Monday are amazing.”
  - $\sim$ > there are slides for Monday.
- “The slides for Monday are not amazing.”
  - $\sim$ > there are slides for Monday.
- The P Q: *presupposes* that there is a unique P, does not *assert* it [Strawson 1950, ...]
  - If there is no P, “The P Q” is *neither true nor false*

# Learning Semantic Parsers

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# Learning to Map Sentences to Logical Form: Structured Classification with Probabilistic Categorical Grammars

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Luke S. Zettlemoyer and Michael Collins

MIT CSAIL

lsz@csail.mit.edu, mcollins@csail.mit.edu

## Abstract

This paper addresses the problem of mapping natural language sentences to lambda-calculus encodings of their meaning. We describe a learning algorithm that takes as input a training set of sentences labeled with expressions in the lambda calculus. The algorithm induces a grammar for the problem, along with a log-linear model that represents a distribution over syntactic and semantic analyses conditioned on the input sentence. We apply the method to the task of learning natural language interfaces to databases and show that the learned parsers outperform previous methods in two benchmark database domains.

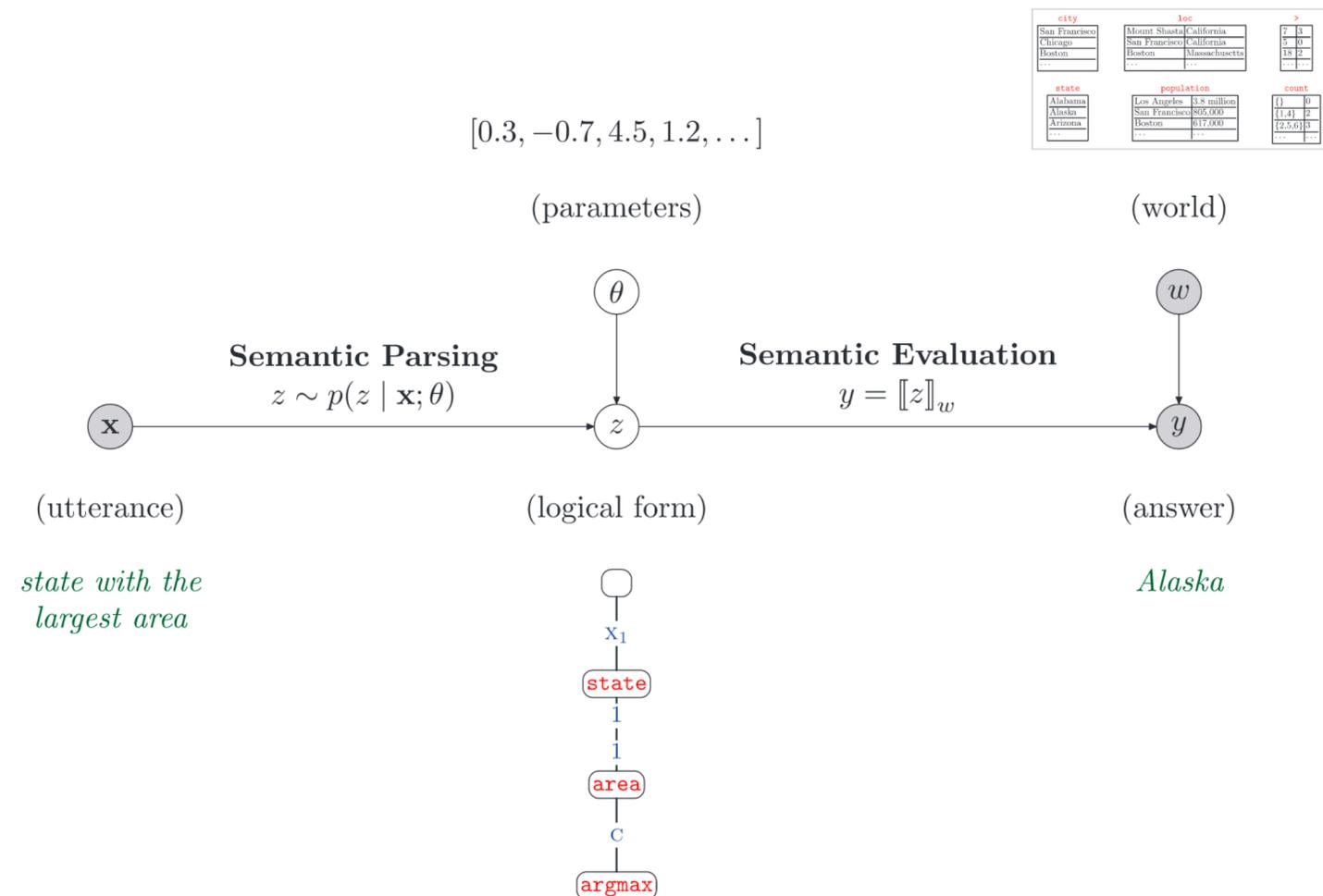
Supervised learning:

- Sentences labeled with logical forms
- Induce grammar
- Plus semantic attachments
- Score analyses of ambiguous sentences with log-linear model

# Learning from Denotations

Liang, Jordan, and Klein

Learning Dependency-Based Compositional Semantics



Learn semantic representations as *latent variables* for downstream task (QA, conversation, ...)

**Figure 2**

Our statistical methodology consists of two steps: (i) semantic parsing ( $p(z | x; \theta)$ ): an utterance  $x$  is mapped to a logical form  $z$  by drawing from a log-linear distribution parametrized by a vector  $\theta$ ; and (ii) evaluation ( $\llbracket z \rrbracket_w$ ): the logical form  $z$  is evaluated with respect to the world  $w$  (database of facts) to deterministically produce an answer  $y$ . The figure also shows an example configuration of the variables around the graphical model. Logical forms  $z$  are represented as labeled trees. During learning, we are given  $w$  and  $(x, y)$  pairs (shaded nodes) and try to infer the latent logical forms  $z$  and parameters  $\theta$ .

[Liang et al 2011](#)

# Resources

- Datasets
  - General:
    - Abstract Meaning Representations: [LDC2017T10](#)
    - Minimal Recursion Semantics: [DeepBank](#)
  - SQL:
    - Spider: <https://yale-lily.github.io/spider>
    - SParC: <https://yale-lily.github.io/sparc>

# Resources: Knowledge Graphs

- R.I.P. Freebase
  - Used by Google Knowledge Graph, then bought and killed
  - [they have [an API](#) with 100,000 queries/day for free]
- BUT: data moved to [Wikidata](#)

# Lexical Semantics

# All these lambdas have me feeling...



Nobody has responded yet.

Hang tight! Responses are coming in.

# Compositional vs Lexical Semantics

## Foreword

In the spring of 1976, Terry Parsons and Barbara Partee taught a course on Montague grammar, which I attended. On the second to the final day of class, Terry went around the room asking the students if there were any questions at all that remained unanswered, and promised to answer them on the last day of class. I asked if he really meant ANY question at all, which he emphatically said that he meant. As I had encountered a few questions in my lifetime that remained at least partially unresolved, I decided to ask one of them. What is life? What is the meaning of life? After all, Barbara and Terry had promised to provide answers to any question at all.

On the final day of class Barbara wore her Montague grammar T-shirt, and she and Terry busied themselves answering our questions. At long last, they came to my question. I anticipated a protracted and involved answer, but their reply was crisp and succinct. First Barbara, chalk in hand, showed me the meaning of life.

^life'

Terry then stepped up and showed me what life really is.

^^life'

As we were asked to show on a homework assignment earlier in the year, this is equivalent to: life'.

Leaving me astounded that I had been living in such darkness for all these years, the class then turned to the much stickier problem of pronouns.

[Carlson 1980](#)

# Lexical Semantics

- Thus far: POS → *Word* {sem}
  - Can compose larger semantic formulae bottom-up this way
  - ...but we haven't really discussed what a "word" is, semantically.

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  - ...but we haven't really discussed what a "word" is, semantically.
- Lexical semantics:
  - How do we formally discuss what a "word" is?
  - How do we relate words to one another?
  - How do we differentiate/relate linked senses?

# What is a Plant?

# What is a Plant?

- There are more kinds of **plants** and animals in the rainforests than anywhere else on Earth. Over half of the millions of known species of **plants** and animals live in the rainforest. Many are found nowhere else. There are even **plants** and animals in the rainforest that we have not yet discovered.

# What is a Plant?

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- The Paulus company was founded in 1938. Since those days the product range has been the subject of constant expansions and is brought up continuously to correspond with the state of the art. We're engineering, manufacturing, and commissioning world-wide ready-to-run **plants** packed with our comprehensive know-how.

# Lexical Semantics

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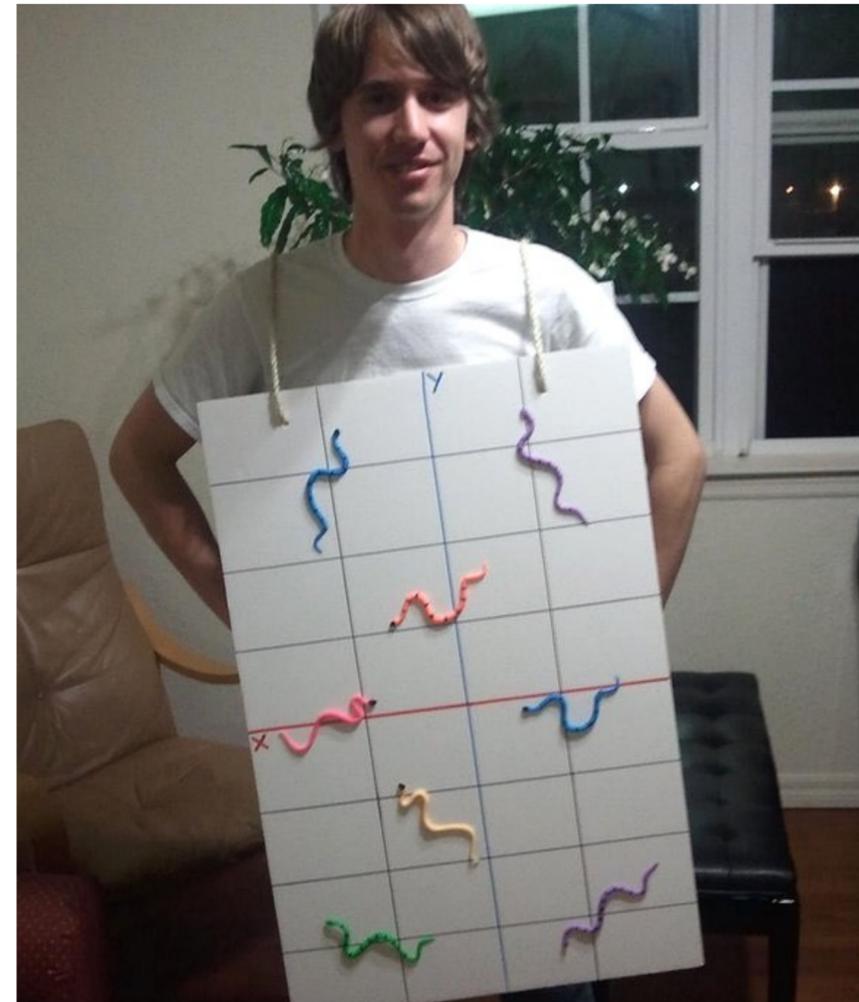
...by way of dad-joke Halloween costumes. 🎃

# Lexical Semantics

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*A Ceiling Fan*



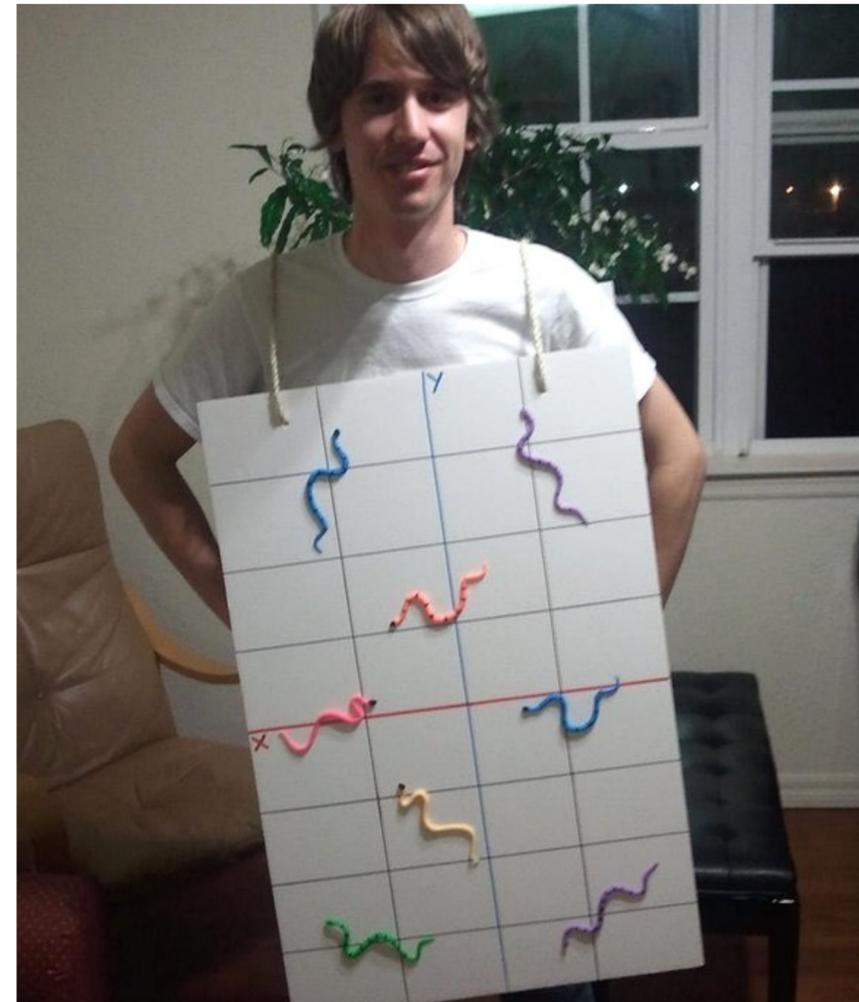
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# Lexical Semantics

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*Snakes on a Plane*

(Painful) Examples of **Homonymy**

# Sources of Confusion

Homonymy

# Sources of Confusion

Homonymy  
Polysemy

# Sources of Confusion

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Synonymy

# Sources of Confusion

Homonymy  
Polysemy  
Synonymy  
Antonymy

# Sources of Confusion

Homonymy

Polysemy

Synonymy

Antonymy

[Hypo/Hyper]-nymy

# Sources of Confusion: Homonymy

- Words have same form but different meanings
  - Generally same POS, but unrelated meaning
    - bank<sub>1</sub> (side of river)
    - bank<sub>2</sub> (financial institution)

# Sources of Confusion: Homonymy

- Different types of Homonymy:
  - **Homophones**: same phonology, different orthographic form
    - two
    - to
    - too
  - **Homographs**: Same orthography, different phonology:
    - “*lead*” (metal)
    - “*lead*” (take somewhere)

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  - **Homographs**: Same orthography, different phonology:
    - “lead” (metal)
    - “lead” (take somewhere)
- Why do we care?
  - Problem for applications: TTS, ASR transcription, IR

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- Multiple RELATED senses
  - e.g. bank: money, organ, blood

# Sources of Confusion: Polysemy

- Multiple RELATED senses
  - e.g. bank: money, organ, blood
- Big issue in lexicography
  - Number of senses
  - Relations between senses
  - Differentiation

# Sources of Confusion: Polysemy

- Example: *[[serve]]*
  - *serve breakfast*
  - *serve Philadelphia*
  - *serve time*

# Sources of Confusion: Synonymy

- (near) identical meaning
- Substitutability
  - Maintains propositional meaning

# Sources of Confusion: Synonymy

- Issues:
  - Also has polysemy!
    - Shades of meaning - other associations
      - *price* vs. *fare*
      - *big* vs. *large*
      - *water* vs. *H<sub>2</sub>O*
  - Collocational constraints
    - e.g. *babbling brook* vs. *\*babbling river*
  - Register:
    - social factors: e.g. politeness, formality

# Sources of Confusion: Antonymy

- Opposition
- Typically ends of a scale
  - *fast* vs. *slow*
  - *big* vs. *little*
- Can be hard to distinguish automatically from synonyms

# Sources of Confusion: Hyponymy

- `instanceOf(x, y)` relations:
- More General (*hypernym*) vs. more specific (*hyponym*)
  - *dog* vs. *golden retriever*
  - *fruit* vs. *mango*
- Organize as ontology/taxonomy

# Word Sense Disambiguation

- Application of lexical semantics
- Goal: given a word ***in context***, identify the appropriate sense
  - e.g. plants and animals in the rainforest
- Crucial for real syntactic & semantic analysis
  - Correct sense can determine
    - Available syntactic structure
    - Available thematic roles, correct meaning...

# Robust Disambiguation

- More to semantics than predicate-argument structure
  - Select sense where predicates underconstrain
- Learning approaches
  - Supervised, bootstrapped, unsupervised
- Knowledge-based approaches
  - Dictionaries, taxonomies
- Contexts for sense selection

There are more kinds of **plants** and animals in the rainforests than anywhere else on Earth. Over half of the millions of known species of **plants** and animals live in the rainforest. Many are found nowhere else. There are even **plants** and animals in the rainforest that we have not yet discovered.

### ***Biological Example***

The Paulus company was founded in 1938. Since those days the product range has been the subject of constant expansions and is brought up continuously to correspond with the state of the art. We're engineering, manufacturing and commissioning world-wide ready-to-run **plants** packed with our comprehensive know-how. Our Product Range includes pneumatic conveying systems for carbon, carbide, sand, lime and many others. We use reagent injection in molten metal for the...

### ***Industrial Example***

Label the First Use of "Plant"

# Roadmap

- Lexical Semantics
  - Motivation & Definitions
  - Word Senses
  - Tasks:
    - **Word sense disambiguation**
    - Word sense similarity
  - Distributional Similarity

# Disambiguation: Features

- Part of Speech
  - Of word and neighbors

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- Morphologically simplified form
- Words in neighborhood
  - How big is “neighborhood?”
  - Is there a single optimal size? Why?

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  - Demonstrate real impact of technique in system
  - Difficult, expensive, still application specific
- Typically intrinsic, sense-based
  - Accuracy, precision, recall
  - SENSEVAL/SEMEVAL: all words, lexical sample

# WSD Evaluation

- Baseline:
  - Most frequent sense

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- Baseline:
  - Most frequent sense
- Ceiling:
  - Human inter-rater agreement
    - 75-80% fine
    - 90% coarse

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- Synonymy:
  - True propositional substitutability is rare, slippery
- Word similarity (semantic distance)
  - Looser notion, more flexible

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- Approaches:
  - Distributional
  - Thesaurus-based

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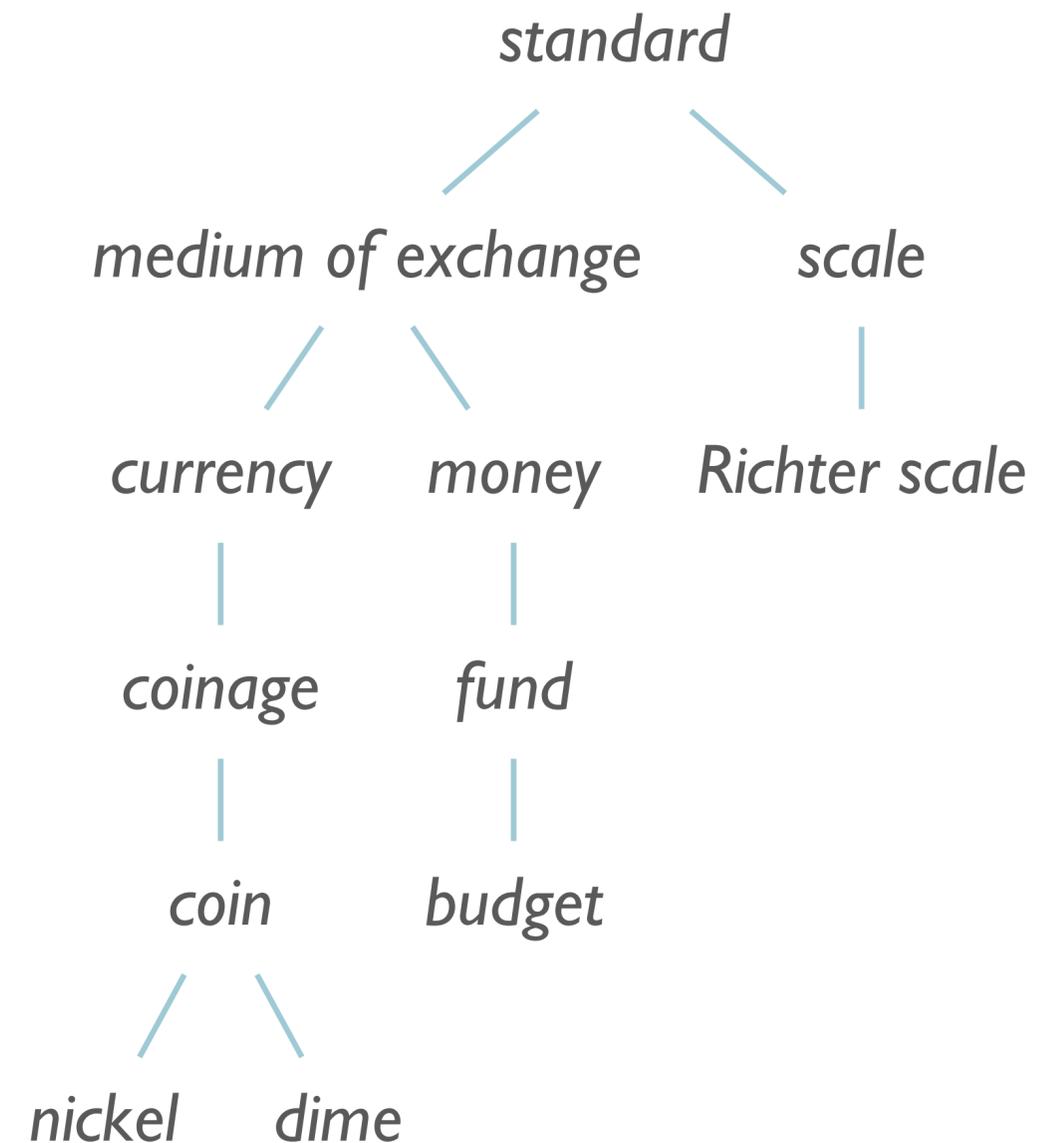
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- Related:
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  - *coin, budget*

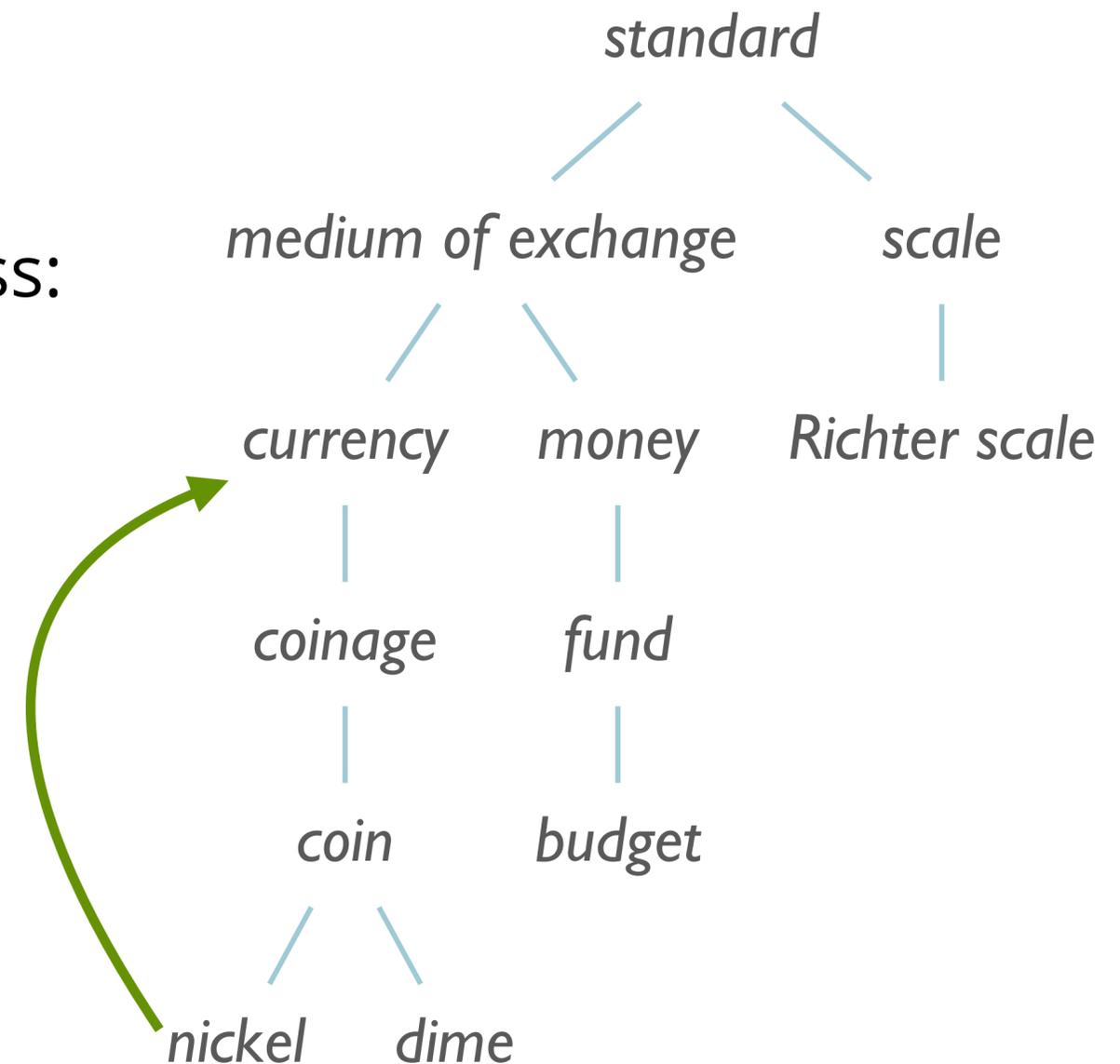
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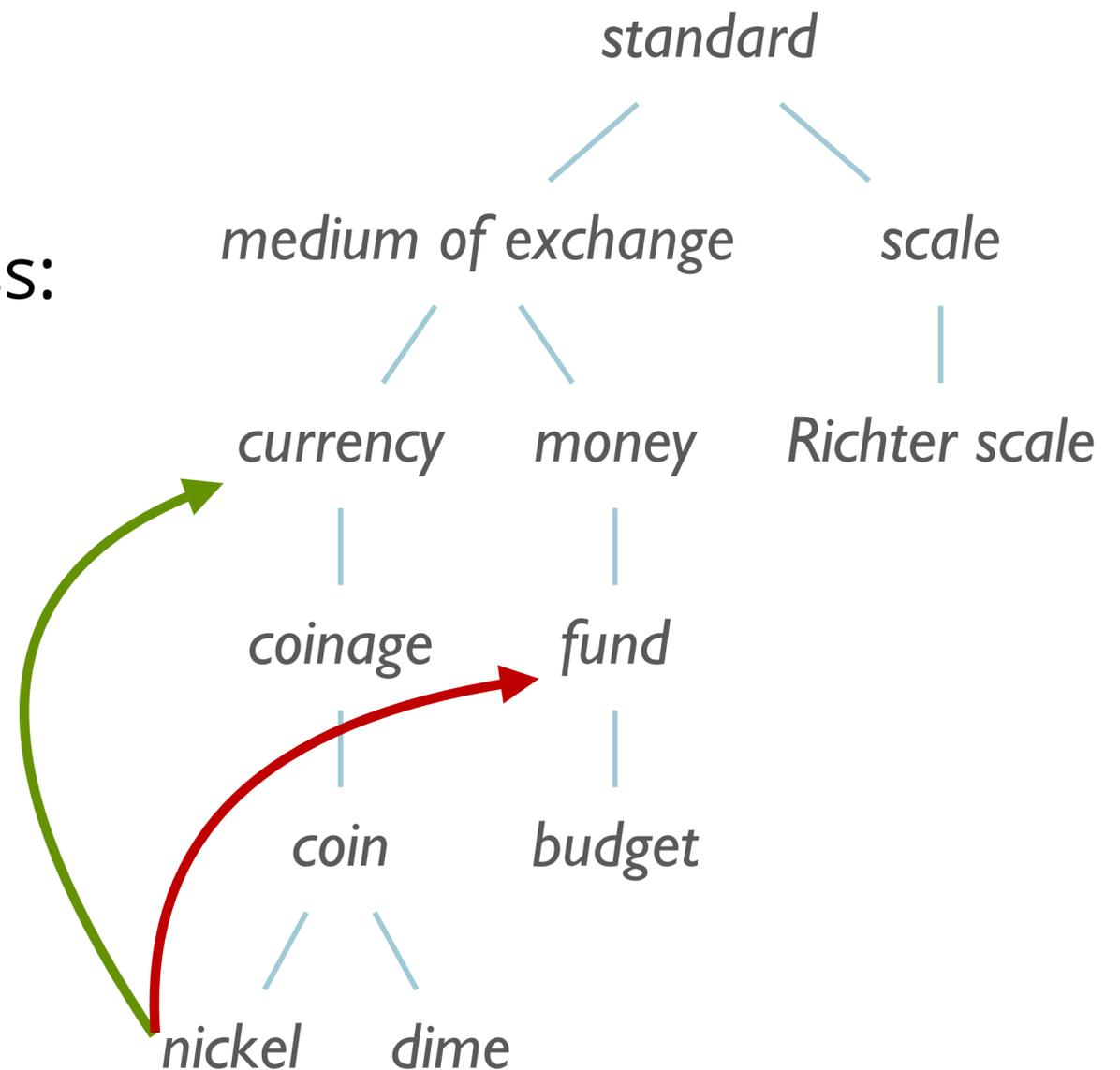
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- Tezguino: corn-based alcoholic beverage. (From [Lin, 1998a](#))

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  - 'Company' = context
- Word represented by context feature vector
  - Many alternatives for vector
- Initial representation:
  - 'Bag of words' binary feature vector
  - Feature vector length  $N$ , where  $N$  is size of vocabulary
    - $f_i=1$  if  $word_i$  within window size  $w$  of  $word_0$

# Context Feature Vector

	arts	boil	data	function	large	sugar	summarized	water
Apricot	0	1	0	0	1	1	0	1
Pineapple	0	1	0	0	1	1	0	1
Digital	0	0	1	1	1	0	1	0
Information	0	0	1	1	1	0	1	0

# Distributional Similarity Questions

- What is the right neighborhood?
  - What is the context?
- How should we weight the features?
- How can we compute similarity between vectors?